4751 (C1) Introduction to Advanced Mathematics

## Section A

| 1 | $[v=][ \pm] \sqrt{\frac{2 E}{m}} \mathrm{www}$ | 3 | M2 for $v^{2}=\frac{2 E}{m}$ or for $[v=][ \pm] \sqrt{\frac{E}{\frac{1}{2} m}}$ or M1 for a correct constructive first step and M 1 for $v=[ \pm] \sqrt{k}$ ft their $v^{2}=k$; if M0 then SC1 for $\sqrt{ } E / 1 / 2 m$ or $\sqrt{2 E} / m$ etc | 3 |
| :---: | :---: | :---: | :---: | :---: |
| 2 | $\frac{3 x-4}{x+1}$ or $3-\frac{7}{x+1}$ www as final answer | 3 | $\begin{aligned} & \text { M1 for }(3 x-4)(x-1) \\ & \text { and M1 for }(x+1)(x-1) \end{aligned}$ | 3 |
| 3 | (i) 1 <br> (ii) $1 / 64 \mathrm{www}$ | $\begin{array}{\|l} 1 \\ 3 \end{array}$ | M1 for dealing correctly with each of reciprocal, square root and cubing (allow 3 only for $1 / 64$ ) eg M2 for 64 or -64 or $1 / \sqrt{ } 4096$ or $1 / 4^{3}$ or M1 for $1 / 16^{3 / 2}$ or $4^{3}$ or $-4^{3}$ or $4^{-3}$ etc | 4 |
| 4 | $\begin{aligned} & 6 x+2(2 x-5)=7 \\ & 10 x=17 \\ & \\ & x=1.7 \text { o.e. isw } \\ & y=-1.6 \text { o.e } . \text { isw } \end{aligned}$ | M1 <br> M1 <br> A1 <br> A1 | for subst or multn of eqns so one pair of coeffts equal (condone one error) simplification (condone one error) or appropriate addn/subtn to eliminate variable allow as separate or coordinates as requested graphical soln: M0 | 4 |
| 5 | (i) $-4 / 5$ or -0.8 o.e. <br> (ii) $(15,0)$ or 15 found www | 2 3 | M1 for $4 / 5$ or 4/-5 or 0.8 or $-4.8 / 6$ or correct method using two points on the line (at least one correct) (may be graphical) or for $-0.8 x$ o.e. <br> M1 for $y=$ their (i) $x+12$ o.e. or $4 x+5 y$ $=k$ and $(0,12)$ subst and M1 for using $y$ $=0$ eg $-12=-0.8 x$ or $f t$ their eqn <br> or M1 for given line goes through ( 0 , 4.8) and ( 6,0 ) and M1 for $6 \times 12 / 4.8$ graphical soln: allow M1 for correct required line drawn and M1 for answer within 2 mm of $(15,0)$ | 5 |


| 6 | $\begin{aligned} & \mathrm{f}(2) \text { used } \\ & 2^{3}+2 k+7=3 \\ & k=-6 \end{aligned}$ | M1 <br> M1 <br> A1 | or division by $x-2$ as far as $x^{2}+2 x$ obtained correctly or remainder $3=2(4+k)+7$ o.e. 2 nd M1 dep on first | 3 |
| :---: | :---: | :---: | :---: | :---: |
| 7 | (i) 56 <br> (ii) -7 or ft from -their (i)/8 | $2$ $2$ | M1 for $\frac{8 \times 7 \times 6}{3 \times 2 \times 1}$ or more simplified <br> M1 for 7 or ft their (i)/8 or for $56 \times(-1 / 2)^{3}$ o.e. or ft ; condone $x^{3}$ in answer or in M1 expression; 0 in qn for just Pascal's triangle seen | 4 |
| 8 | (i) $5 \sqrt{3}$ <br> (ii) common denominator $=$ $\begin{aligned} & (5-\sqrt{ } 2)(5+\sqrt{ } 2) \\ & =23 \\ & \text { numerator }=10 \end{aligned}$ | 2 <br> M1 <br> A1 <br> B1 | M1 for $\sqrt{48}=4 \sqrt{ } 3$ allow M1A1 for $\frac{5-\sqrt{2}}{23}+\frac{5+\sqrt{2}}{23}$ allow 3 only for 10/23 | 5 |
| 9 | $\begin{aligned} & \text { (i) } n=2 m \\ & 3 n^{2}+6 n=12 m^{2}+12 m \text { or } \\ & =12 m(m+1) \end{aligned}$ <br> (ii) showing false when $n$ is odd e.g. $3 n^{2}+6 n=\text { odd }+ \text { even }=\text { odd }$ | M1 <br> M2 <br> B2 | or any attempt at generalising; M0 for just trying numbers <br> or M1 for $3 n^{2}+6 n=3 n(n+2)=3 \times$ even $\times$ even and M1 for explaining that 4 is a factor of even $\times$ even or M1 for 12 is a factor of $6 n$ when $n$ is even and M1 for 4 is a factor of $n^{2}$ so 12 is a factor of $3 n^{2}$ <br> or $3 n(n+2)=3 \times$ odd $\times$ odd $=$ odd or counterexample showing not always true; M1 for false with partial explanation or incorrect calculation | 5 |

## Section B




