GCE

## Mathematics (MEI)

Advanced Subsidiary GCE

## Mark Scheme for January 2013

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

## Annotations

| Annotation | Meaning |
| :---: | :--- |
| Vand $\boldsymbol{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| Highlighting |  |
| Other abbreviations in mark scheme | Meaning |
| E1 | Mark for explaining |
| U1 | Mark for correct units |
| G1 | Mark for a correct feature on a graph |
| M1 dep* | Method mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |

## Subject-specific Marking Instructions

Annotations should be used whenever appropriate during your marking.
The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

## A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

## B

Mark for a correct result or statement independent of Method marks.

## E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, $A$ and $B$ marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

## Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.
$\mathrm{h} \quad$ For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (i) | $\frac{9}{25} \text { or } 0.36 \text { isw }$ | [2] | M1 for numerator or denominator correct or for squaring correctly or for inverting correctly | M1 for eg $\frac{1}{\left(\frac{25}{9}\right)}$ or $\left(\frac{25}{9}\right)^{-1}$ or $\frac{25}{9}$ or <br> for $\left(\frac{3}{5}\right)^{2}$ or $\frac{3}{5}$ <br> M0 for just $\frac{1}{\left(\frac{5}{3}\right)^{2}}$ |
| 1 | (ii) | 27 | $2$ <br> [2] | M1 for $81^{\frac{1}{4}}=3$ soi | eg M1 for $3^{3}$ <br> M0 for $81^{3}=531441$ (true but not helpful) |
| 2 |  | $4 x^{4} y^{-3}$ or $\frac{4 x^{4}}{y^{3}}$ as final answer | $3$ <br> [3] | B1 each 'term'; or M1 for numerator $=64 x^{15} y^{3}$ and M1 for denominator $=16 x^{11} y^{6}$ | B0 if obtained fortuitously <br> mark B scheme or M scheme to advantage of candidate, but not a mixture of both schemes |





| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8 |  | $\begin{aligned} & 5 c+9 t=2 a c+a t \\ & 5 c-2 a c=a t-9 t \mathrm{oe} \\ & c(5-2 a)=a t-9 t \mathrm{oe} \\ & {[c=] \frac{a t-9 t}{5-2 a} \text { or } \frac{t(a-9)}{5-2 a} \text { oe as final answer }} \end{aligned}$ | M1 M1 M1 M1 [4] | for correct expansion of brackets <br> for correct collection of terms, ft eg after M0 for $5 c+9 t=2 a c+t$ allow this M1 for $5 c-2 a c=-8 t$ oe <br> for correctly factorising, ft ; must be $c \times$ a two-term factor <br> for correct division, ft their two-term factor | for each M, ft previous errors if their eqn is of similar difficulty; <br> may be earned before $t$ terms collected <br> treat as MR if $t$ is the subject, with a penalty of 1 mark from those gained, marking similarly |
| 9 | (i) | sketch of cubic the right way up, with two tps <br> their graph touching the $x$-axis at -2 and crossing it at 3 and no other places <br> intersection of $y$-axis at -12 | B1 <br> B1 <br> B1 <br> [3] | if intns are not labelled, they must be shown nearby | No section to be ruled; no curving back; condone some curving out at ends but not approaching another turning point; condone some doubling (eg erased curves may continue to show); ignore position of turning points for this mark <br> mark intent if 'daylight' between curve and axis at $x=-2$ <br> if no graph but -12 marked on $y$-axis, or in table, allow this $3^{\text {rd }}$ mark |
| 9 | (ii) | -5 and 0 | B2 [2] | B1 each; allow B2 for $-5,-5,0$; or B1 for both correct with one extra value or for $(-5,0)$ and $(0,0)$ <br> or SC1 for both of 1 and 6 | if their graph wrong, allow -5 and 0 from starting again with eqn, or ft their graph with two intns with $x$-axis |



| Question |  |  | Answer <br> completion to given answer $3 y+5 x=10$, showing at least one interim step | Marks <br> M1 | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | condone a slight slip if they recover quickly and general steps are correct (eg sometimes a slip in working with the $c$ in $y=\frac{-5}{3} x+c$ - condone $3 y=-5 x+c$ followed by substitution and consistent working) <br> M0 if clearly 'fudging' | NB answer given; mark process not answer; annotate if full marks not earned eg with a tick for each mark earned <br> scores such as B2M0M0M1M1 are possible <br> after B2, allow full marks for complete method of showing given line has gradient perp to $\mathrm{AB}(\operatorname{grad} \mathrm{AB}$ must be found independently at some stage) and passes through midpt of AB |
| 10 | (ii) |  | $3 y+5(4 y-21)=10$ <br> $(-1,5)$ or $y=5, x=-1$ isw | M1 <br> A2 <br> [3] | or other valid strategy for eliminating one variable attempted eg $\frac{-5}{3} x+\frac{10}{3}=\frac{x}{4}+\frac{21}{4}$; condone one error <br> A1 for each value; if AO allow SC 1 for both values correct but unsimplified fractions, eg $\left(\frac{-23}{23}, \frac{115}{23}\right)$ | or eg $20 y=5 x+105$ and subtraction of two eqns attempted <br> no ft from wrong perp bisector eqn, since given <br> allow M1 for candidates who reach $y=115 / 23$ and then make a worse attempt, thinking they have gone wrong <br> NB M0A0 in this part for finding E using info from (iii) that implies E is midpt of CD |




| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | (ii) | $(2,0) \text { and }(3,0)$ $(0,6)$ <br> graph of quadratic the correct way up and crossing both axes | B2 <br> B1 <br> B1 <br> [4] | B1 each <br> or B1 for both correct plus an extra <br> or M1 for $(x-2)(x-3)$ or correct use of formula or for their $a \pm \sqrt{\text { their } b} \mathrm{ft}$ from (i) <br> ignore label of their tp; <br> condone stopping at $y$-axis | condone not expressed as coordinates, for both $x$ and $y$ values; <br> accept eg in table or marked on graph <br> condone ' $U$ ' shape or slight curving back in/out; condone some doubling / feathering - deleted work sometimes still shows up in scoris; must not be ruled; condone fairly straight with clear attempt at curve at minimum; be reasonably generous on attempt at symmetry |
| 11 | (iii) | $x^{2}-5 x+6=2-x$ $x^{2}-4 x+4[=0]$ | M1 <br> M1 | for attempt to equate or subtract eqns or attempt at rearrangement and elimination of $x$ <br> for rearrangement to zero ft and collection of terms; condone one error; if using completing the square, need to get as far as $(x-k)^{2}=c$, with at most one error $\left[(x-2)^{2}=0\right.$ if correct $]$ | accept calculus approach: $y^{\prime}=2 x-5$ <br> use of $y^{\prime}=-1$ M1 |


| Question |  |  | Answer $x=2,[y=0]$ <br> 'double root at $x=2$ so tangent' oe; www; | Marks <br> A1 <br> A1 <br> [4] | Guidan |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | condone omission of $y=0$ since already found in (ii) <br> if they have eliminated $x, y=0$ is not sufft for A 1 - need to get $x=2$ <br> A0 for $x=2$ and another root <br> eg 'only one point of contact, so tangent'; <br> or showing $b^{2}-4 a c=0$, and concluding 'so tangent'; www | $x=2 \mathrm{~A} 1$ <br> tgt is $y[-0]=-(x-2)$ and obtaining given line A1 |
| 12 | (i) |  | $f(1)=1-1+1+9-10[=0]$ <br> attempt at division by $(x-1)$ as far as $x^{4}-x^{3}$ in working <br> correctly obtaining $x^{3}+x+10$ | B1 <br> M1 <br> A1 <br> [3] | allow for correct division of $\mathrm{f}(x)$ by $(x-1)$ showing there is no remainder, <br> or for $(x-1)\left(x^{3}+x+10\right)$ found, showing it 'works' by multiplying it out <br> allow equiv for $(x+2)$ as far as $x^{4}+2 x^{3}$ in working <br> or for inspection with at least two terms of cubic factor correct <br> or $x^{3}-3 x^{2}+7 x-5$ | condone $1^{4}-1^{3}+1^{2}+9-10$ <br> eg for inspection, M1 for two terms right and two wrong <br> if M0 and this division / factorising is done in part (ii) or (iii), allow SC1 if correct cubic obtained there; attach the relevant part to (i) with a formal chain link if not already seen in the image zone for (i) |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (ii) | $[\mathrm{g}(-2)=]-8-2+10$ or $\mathrm{f}(-2)=16+8+4-18-10$ | M1 | [in this scheme $\mathrm{g}(x)=x^{3}+x+10$ ] allow M1 for correct trials with at least two values of $x$ (other than 1) using $\mathrm{g}(x)$ or $\mathrm{f}(x)$ or $x^{3}-3 x^{2}+7 x-5$ (may allow similar correct trials using division or inspection) | $\begin{aligned} & \text { eg } \mathrm{f}(2)=16-8+4+18-10 \text { or } 20 \\ & \mathrm{f}(3)=81-27+9+27-10 \text { or } 80 \\ & \mathrm{f}(0)=-10 \\ & \mathrm{f}(-1)=1+1+1-9-10 \text { or }-16 \end{aligned}$ <br> No ft from wrong cubic 'factors' from (i) |
|  |  | $x=-2$ isw | A1 | allow these marks if already earned in (i) | NB factorising of $x^{3}+x+10$ or $x^{3}-3 x^{2}+7 x-5$ in (ii) earns credit for (iii) [annotate with a yellow line in both parts to alert you - the image zone for (iii) includes part (ii)] |
|  |  |  | [2] |  |  |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (iii) | attempted division of $x^{3}+x+10$ by $(x+2)$ as far as $x^{3}+2 x^{2}$ in working | M1 | or $x^{3}-3 x^{2}+7 x-5$ by $(x-1)$ as far as $x^{3}-x^{2}$ in working <br> or inspection with at least two terms of quadratic factor correct | alt method: allow M1 for attempted division of quartic by $x^{2}+x-2$ as far as $x^{4}+x^{3}-2 x^{2}$ in working, or inspection etc |
|  |  | correctly obtaining $x^{2}-2 x+5$ | A1 | allow these first 2 marks if this has been done in (ii), even if not used here |  |
|  |  | use of $b^{2}-4 a c$ with $x^{2}-2 x+5$ | M1 | may be in attempt at formula (ignore rest of formula) | or completing square form attempted or attempt at calculus or symmetry to find min pt |
|  |  |  |  |  | NB M0 for use of $b^{2}-4 a c$ with cubic factor etc |
|  |  | $b^{2}-4 a c=4-20[=-16]$ | A1 | may be in formula; | or $(x-1)^{2}+4$ $\text { or } \min =(1,4)$ |
|  |  | so only two real roots[ of $\mathrm{f}(x)]$ [and hence no more linear factors] | A1 | or no real roots of $x^{2}-2 x+5=0$; allow this last mark if clear use of $x^{2}-2 x+5$ $=0$, even if error in $b^{2}-4 a c$, provided result negative, but no ft from wrong factor | or $(x-1)^{2}+4$ is always positive so no real roots [of $(x-1)^{2}+4=0$ ] [ and hence no linear factors] <br> or similar conclusion from min pt |
|  |  |  | [5] | if last M1 not earned, allow SC1 for stating that the only factors of 5 are 1 and 5 and reasoning eg that $(x-1)(x-5)$ and $(x+1)(x+5)$ do not give $x^{2}-2 x+5$ [hence $x^{2}-2 x+5$ does not factorise] |  |

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

## OCR Customer Contact Centre

## Education and Learning

Telephone: 01223553998
Facsimile: 01223552627
Email: general.qualifications@ocr.org.uk
www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations
is a Company Limited by Guarantee
Registered in England
Registered Office; 1 Hills Road, Cambridge, CB1 2EU
GROUP
Registered Company Number: 3484466
OCR is an exempt Charity
OCR (Oxford Cambridge and RSA Examinations)
Head office
Telephone: 01223552552
Facsimile: 01223552553

