

ADVANCED SUBSIDIARY GCE MATHEMATICS (MEI)

4751

Introduction to Advanced Mathematics (C1)

QUESTION PAPER

Candidates answer on the Printed Answer Book

OCR Supplied Materials:

- Printed Answer Book 4751
- MEI Examination Formulae and Tables (MF2)

Other Materials Required:

None

Monday 24 May 2010 Afternoon

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Printed Answer Book.
- The questions are on the inserted Question Paper.
- Write your answer to each question in the space provided in the Printed Answer Book. Additional paper
 may be used if necessary but you must clearly show your Candidate Number, Centre Number and question
 number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- You are **not** permitted to use a calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

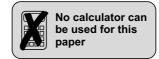
INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to
 indicate that a correct method is being used.
- The total number of marks for this paper is 72.
- The Printed Answer Book consists of 12 pages. The Question Paper consists of 4 pages. Any blank pages
 are indicated.

INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

Do not send this Question Paper for marking; it should be retained in the centre or destroyed.



Section A (36 marks)

- Find the equation of the line which is parallel to y = 3x + 1 and which passes through the point with coordinates (4, 5).
- 2 (i) Simplify $(5a^2b)^3 \times 2b^4$. [2]
 - (ii) Evaluate $(\frac{1}{16})^{-1}$. [1]
 - (iii) Evaluate $(16)^{\frac{3}{2}}$. [2]
- 3 Make y the subject of the formula $a = \frac{\sqrt{y} 5}{c}$. [3]
- 4 Solve the following inequalities.

(i)
$$2(1-x) > 6x + 5$$

(ii)
$$(2x-1)(x+4) < 0$$
 [2]

- 5 (i) Express $\sqrt{48} + \sqrt{27}$ in the form $a\sqrt{3}$. [2]
 - (ii) Simplify $\frac{5\sqrt{2}}{3-\sqrt{2}}$. Give your answer in the form $\frac{b+c\sqrt{2}}{d}$. [3]
- 6 You are given that
 - the coefficient of x^3 in the expansion of $(5 + 2x^2)(x^3 + kx + m)$ is 29,
 - when $x^3 + kx + m$ is divided by (x 3), the remainder is 59.

Find the values of k and m. [5]

- 7 Expand $\left(1 + \frac{1}{2}x\right)^4$, simplifying the coefficients. [4]
- 8 Express $5x^2 + 20x + 6$ in the form $a(x+b)^2 + c$. [4]
- 9 Show that the following statement is false.

$$x - 5 = 0 \iff x^2 = 25$$

© OCR 2010 4751 Jun10

Section B (36 marks)

10 (i) Solve, by factorising, the equation $2x^2 - x - 3 = 0$. [3]

(ii) Sketch the graph of
$$y = 2x^2 - x - 3$$
. [3]

(iii) Show that the equation
$$x^2 - 5x + 10 = 0$$
 has no real roots. [2]

(iv) Find the x-coordinates of the points of intersection of the graphs of $y = 2x^2 - x - 3$ and $y = x^2 - 5x + 10$. Give your answer in the form $a \pm \sqrt{b}$.

11

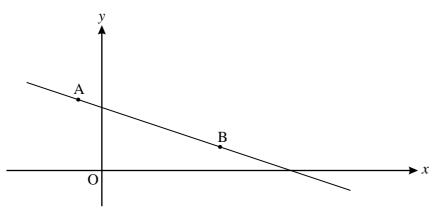


Fig. 11

Fig. 11 shows the line through the points A(-1, 3) and B(5, 1).

- (i) Find the equation of the line through A and B. [3]
- (ii) Show that the area of the triangle bounded by the axes and the line through A and B is $\frac{32}{3}$ square units. [2]
- (iii) Show that the equation of the perpendicular bisector of AB is y = 3x 4. [3]
- (iv) A circle passing through A and B has its centre on the line x = 3. Find the centre of the circle and hence find the radius and equation of the circle. [4]
- 12 You are given that $f(x) = x^3 + 6x^2 x 30$.
 - (i) Use the factor theorem to find a root of f(x) = 0 and hence factorise f(x) completely. [6]
 - (ii) Sketch the graph of y = f(x). [3]
 - (iii) The graph of y = f(x) is translated by $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$.

Show that the equation of the translated graph may be written as

$$y = x^3 + 3x^2 - 10x - 24.$$
 [3]

© OCR 2010 4751 Jun10