## edexcel

## Mark Scheme (Results)

## Summer 2013

GCE Further Pure Mathematics 3 (6669/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme

## General Principles for Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

1. Factorisation
$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $\mathrm{x}=$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $\mathrm{x}=$
2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ).

## 3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c, \quad q \neq 0, \quad$ leading to $\mathrm{x}=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by 1. ( $x^{n} \rightarrow x^{n+1}$ )

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. (a) | $k \operatorname{arsinh}\left(\frac{2 x}{3}\right)(+c) \quad$ or $\quad k \ln \left[p x+\sqrt{\left(p^{2} x^{2}+\frac{9}{4} p^{2}\right)}\right](+c)$ | M1 |
|  | $\frac{1}{2} \operatorname{arsinh}\left(\frac{2 x}{3}\right)(+c) \quad$ or $\frac{1}{2} \ln \left[p x+\sqrt{\left(p^{2} x^{2}+\frac{9}{4} p^{2}\right)}\right](+c)$ | A1 |
|  |  | (2) |
| (b) | So: $\frac{1}{2} \ln [6+\sqrt{45}]-\frac{1}{2} \ln [-6+\sqrt{45}]=\frac{1}{2} \ln \left[\frac{6+\sqrt{45}}{-6+\sqrt{45}}\right]$ | M1 |
|  | Uses correct limits and combines logs |  |
|  | $=\frac{1}{2} \ln \left[\frac{6+\sqrt{45}}{-6+\sqrt{45}}\right]\left[\frac{6+\sqrt{45}}{6+\sqrt{45}}\right]=\frac{1}{2} \ln \left[\frac{(6+\sqrt{45})^{2}}{9}\right]$ | M1 |
|  | Correct method to rationalise denominator (may be implied) Method must be clear if answer does not follow their fraction |  |
|  | $=\ln [2+\sqrt{5}] \quad$ or $\left.\frac{1}{2} \ln [9+4 \sqrt{5}]\right)$ | A1cso |
|  | Note that the last 3 marks can be scored without the need to rationalise e.g. $2 \times \frac{1}{2}\left[\ln \left[2 x+\sqrt{\left(4 x^{2}+9\right)}\right]\right]_{0}^{3}=\ln (6+\sqrt{45})-\ln 3=\ln \left(\frac{6+\sqrt{45}}{3}\right)$ <br> M1: Uses the limits 0 and 3 and doubles <br> M1: Combines Logs <br> A1: $\ln [2+\sqrt{5}]$ oe |  |
|  |  | (3) |
|  |  | Total 5 |
| Alternative for (a) | $x=\frac{3}{2} \sinh u \Rightarrow \int \frac{1}{\sqrt{9 \sinh ^{2} u+9}} \cdot \frac{3}{2} \cosh u \mathrm{~d} u=k \operatorname{arsinh}\left(\frac{2 x}{3}\right)(+c)$ | M1 |
|  | $\frac{1}{2} \operatorname{arsinh}\left(\frac{2 x}{3}\right)(+c)$ | A1 |
| Alternative for (b) | $\left[\frac{1}{2} \operatorname{arsinh}\left(\frac{2 x}{3}\right)\right]_{-3}^{3}=\frac{1}{2} \operatorname{arsinh} 2-\frac{1}{2} \operatorname{arsinh}-2$ |  |
|  | $\frac{1}{2} \ln (2+\sqrt{5})-\frac{1}{2} \ln (\sqrt{5}-2)=\frac{1}{2} \ln \left(\frac{2+\sqrt{5}}{\sqrt{5}-2}\right)$ | M1 |
|  | Uses correct limits and combines logs |  |
|  | $=\frac{1}{2} \ln \left(\frac{2+\sqrt{5}}{\sqrt{5}-2} \cdot \frac{\sqrt{5}+2}{\sqrt{5}+2}\right)=\frac{1}{2} \ln \left(\frac{2 \sqrt{5}+4+5+2 \sqrt{5}}{5-4}\right)$ | M1 |
|  | Correct method to rationalise denominator (may be implied) Method must be clear if answer does not follow their fraction |  |
|  | $=\frac{1}{2} \ln [9+4 \sqrt{5}]$ | A1cso |
|  |  |  |



| Question <br> Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. | Alternative Cartesian Approach |  |
|  | $x=1+\frac{y^{2}}{8} \quad$ Any correct Cartesian equation | B1 |
|  | $\frac{d x}{d y}=\frac{y}{4} \quad$ or $\frac{d y}{d x}=\frac{\sqrt{2}}{(x-1)^{\frac{1}{2}}} \quad$ Correct Derivative | B1 |
|  | $\left.A=\int 2 \pi \cdot y \sqrt{\left(1+\left(\frac{y}{4}\right)^{2}\right.}\right) \mathrm{d} y$ or $A=\int 2 \pi \cdot \sqrt{8}(x-1)^{\frac{1}{2}} \sqrt{\left(1+\left(\frac{2}{x-1}\right)\right.} \mathrm{d} x$ | M1 |
|  | Use of a correct formula |  |
|  | $A=2 \pi \times \frac{2}{3} \times 8\left(1+\frac{y^{2}}{16}\right)^{\frac{3}{2}}$ or $A=\frac{4 \pi \sqrt{8}}{3} x+1^{\frac{3}{2}}$ | dM1 A1 |
|  | M1: Convincing attempt to integrate a relevant expression dependent on the first M1 but allow the omission of $2 \pi$ |  |
|  | A1: Completely correct expression for A |  |
|  | $A=2 \pi \times \frac{2}{3} \times 8 \quad 1+\sinh ^{2} 1^{\frac{3}{2}}-2 \pi \times \frac{2}{3} \times 8$ or $2 \pi \times \frac{2}{3} \times \sqrt{8} 1+\cosh 2^{\frac{3}{2}}-\frac{32 \pi}{3}$ | ddM1 |
|  | Correct use of limits ( $0 \rightarrow 4 \sinh 1$ for y or $\mathbf{1} \boldsymbol{\rightarrow} \cosh 2$ for $\boldsymbol{x}$ ) |  |
|  | Use $1+\sinh ^{2} 1=\cosh ^{2} 1$ to give $\frac{32 \pi}{3}\left[\cosh ^{3} 1-1\right]$ <br> Use $\cosh 2=2 \cosh ^{2} 1-1$ to give $\frac{32 \pi}{3}\left[\cosh ^{3} 1-1\right]$ | A1 |


| Question <br> Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 4. | $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{40}{\sqrt{\left(x^{2}-1\right)}}-9$ | M1: $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{p}{\sqrt{\left(x^{2}-1\right)}}-q$ | M1 A1 |
|  |  | A1: Cao |  |
|  | Put $\frac{\mathrm{d} y}{\mathrm{~d} x}=\mathbf{0}$ and obtain $x^{2}=\ldots$. <br> (Allow sign errors only) | e.g. $\left(\frac{1681}{81}\right)$ | dM1 |
|  |  | M1: Square root |  |
|  | $x=\frac{41}{9}$ | A1: $x=\frac{41}{9}$ or exact equivalent $\left(\operatorname{not} \pm \frac{41}{9}\right)$ | M1 A1 |
|  | $y=40 \ln \left\{\left(\frac{41}{9}\right)+\sqrt{\left(\frac{41}{9}\right)^{2}-1}\right\}-" 41 "$ | Substitutes $x=" \frac{41}{9} "$ into the curve and uses the logarithmic form of arcosh | M1 |
|  | So $y=80 \ln 3-41$ | Cao | A1 |
|  |  |  | Total 7 |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5. (a) (i)\&(ii) | $\left(\begin{array}{rrr}1 & 1 & a \\ 2 & b & c \\ -1 & 0 & 1\end{array}\right)\left(\begin{array}{l}0 \\ 1 \\ 1\end{array}\right)=\left(\begin{array}{c}1+a \\ b+c \\ 1\end{array}\right)=\lambda_{1}\left(\begin{array}{l}0 \\ 1 \\ 1\end{array}\right)$, and so $a=-1, \lambda_{1}=1$ | M1, A1, A1 |
|  | M1: Multiplies out matrix with first eigenvector and puts equal to $\lambda_{1}$ times eigenvector. A1 : Deduces $\boldsymbol{a}=\mathbf{- 1}$. A1: Deduces $\lambda_{1}=1$ |  |
|  | $\left(\begin{array}{rrr}1 & 1 & a \\ 2 & b & c \\ -1 & 0 & 1\end{array}\right)\left(\begin{array}{r}1 \\ 0 \\ -1\end{array}\right)=\left(\begin{array}{l}1-a \\ 2-c \\ -2\end{array}\right)=\lambda_{2}\left(\begin{array}{r}1 \\ 0 \\ -1\end{array}\right)$, and so $c=2, \lambda_{2}=2$ | M1, A1, A1 |
|  | M1: Multiplies out matrix with second eigenvector and puts equal to $\lambda_{2}$ times eigenvector. A1: Deduces $\boldsymbol{c}=2$. A1: Deduces $\lambda_{2}=2$ |  |
|  | $b+c=\lambda_{1} \quad$ so $b=-1 \quad \|$M1: Uses $b+c=\lambda_{1}$ with their $\lambda_{1}$ to <br> find a value for $b$ (They must <br> have an equation in $b$ and $c$ from <br> the first eigenvector to score this <br> mark) | M1A1 |
|  | $\left(a=-1, b=-1, c=2, \lambda_{1}=1, \lambda_{2}=2\right)$ | (8) |
| (b)(i) | $\operatorname{detP}=-d-1$ Allow $1-d-2$ or $1-(2+d)$ <br> A correct (possibly un-simplified) <br> determinant | B1 |
| (ii) | $\begin{aligned} & \mathbf{P}^{T}=\left(\begin{array}{ccc} 1 & 2 & -1 \\ 1 & 1 & 0 \\ 0 & d & 1 \end{array}\right) \text { or minors }\left(\begin{array}{ccc} 1 & d+2 & 1 \\ 1 & 1 & 1 \\ d & d & -1 \end{array}\right) \text { or } \\ & \text { cofactors }\left(\begin{array}{ccc} 1 & -2-\mathrm{d} & 1 \\ -1 & 1 & -1 \\ \mathrm{~d} & -\mathrm{d} & -1 \end{array}\right) \text { a correct first step } \end{aligned}$ | B1 |
|  | $\frac{1}{-d-1}\left(\begin{array}{ccc}1 & -1 & d \\ -2-d & 1 & -d \\ 1 & -1 & -1\end{array}\right) \quad$M1: Identifiable full attempt at <br> inverse including reciprocal of <br> determinant. Could be indicated <br> by at least 6 correct elements. | M1 A1 A1 |
|  |  |  |
|  |  |  |
|  |  | (5) |
|  |  | Total 13 |



| Question <br> Number | Scheme |  |  | Marks |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $I_{1}=\int_{0}^{4} x \sqrt{\left(16-x^{2}\right)} \mathrm{d} x=\left[-\frac{1}{3}\left(16-x^{2}\right)^{\frac{3}{2}}\right]_{0}^{4}=\frac{64}{3}$ |  | M1: Correct integration to find $I_{1}$ <br> A1: $\frac{64}{3}$ or equivalent <br> (May be implied by a later work - they are not asked explicitly for $I_{1}$ ) | M1 A1 |
|  | $\frac{64}{3}$ must come from correct work |  |  |  |
|  | $\begin{gathered} \text { Using } x=4 \sin \theta: \\ I_{1}=\int_{0}^{\frac{\pi}{2}} 4 \sin \theta \sqrt{\left(16-16 \sin ^{2} \theta\right)} 4 \cos \theta \mathrm{~d} \theta=\int_{0}^{\frac{\pi}{2}} 64 \sin \theta \cos ^{2} \theta \mathrm{~d} \theta \\ =\left[-\frac{64}{3} \cos ^{3} \theta\right]_{0}^{\frac{\pi}{2}} \end{gathered}$ <br> M1: A complete substitution and attempt to substitute changed limits <br> A1: $\frac{64}{3}$ or equivalent |  |  |  |
|  | $I_{5}=\frac{64}{7} I_{3}, I_{3}=\frac{32}{5} I_{1}$ | Applies to apply reduction formula twice. First M1 for $I_{5}$ in terms of $I_{3}$, second M1 for $I_{3}$ in terms of $I_{1}$ (Can be implied) |  | M1, M1 |
|  | $I_{5}=\frac{131072}{105}$ | Any exact equivalent (Depends on all previous marks having been scored) |  | A1 |
|  |  |  |  | (5) |
|  |  |  |  | Total 11 |



| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 8(a) | $(\mathbf{6 i}+\mathbf{2 j}+\mathbf{1 2 k}) .(3 \mathbf{i}-4 \mathbf{j}+2 \mathbf{k})=34$ | Attempt scalar product | M1 |
|  | $\left\|\frac{(\mathbf{6 i}+\mathbf{2} \mathbf{j}+\mathbf{1 2 k}) \cdot(3 \mathbf{i}-4 \mathbf{j}+2 \mathbf{k})-5}{\sqrt{3^{2}+4^{2}+2^{2}}}\right\|$ | Use of correct formula | M1 |
|  | $\sqrt{29}($ not $-\sqrt{29})$ | Correct distance (Allow 29/ $\sqrt{29}$ ) | A1 |
|  |  |  | (3) |
| (a) Way 2 | $\therefore 6+3 \lambda 3+2-4 \lambda-4+12+2 \lambda 2=5$ |  | M1 |
|  | Substitutes the parametric coordinates of the line through $(6,2,12)$ perpendicular to the plane into the cartesian equation. |  |  |
|  | $\lambda=-1 \Rightarrow 3,6,10$ or $-3 \mathbf{i}+4 \mathbf{j}-2 \mathbf{k}$ | Solves for $\lambda$ to obtain the required point or vector. | M1 |
|  | $\sqrt{29}$ | Correct distance | A1 |
| (a) Way 3 | $\begin{aligned} & \text { Parallel plane containing }(6,2,12) \text { is } \\ & \quad \mathbf{r} \cdot(3 \mathbf{i}-4 \mathbf{j}+2 \mathbf{k})=34 \\ & \quad \Rightarrow \frac{\mathbf{r} \cdot(3 \mathbf{i}-4 \mathbf{j}+2 \mathbf{k})}{\sqrt{29}}=\frac{34}{\sqrt{29}} \end{aligned}$ | Origin to this plane is $\frac{34}{\sqrt{29}}$ | M1 |
|  | $\Rightarrow \frac{\mathbf{r} .(3 \mathbf{i}-4 \mathbf{j}+2 \mathbf{k})}{\sqrt{29}}=\frac{5}{\sqrt{29}}$ | Origin to plane is $\frac{5}{\sqrt{29}}$ | M1 |
|  | $\frac{34}{\sqrt{29}}-\frac{5}{\sqrt{29}}=\sqrt{29}$ | Correct distance | A1 |
| (b) <br> For a cross product, if the method is unclear, 2 out of 3 components should be correct for M1 | $\left\|\begin{array}{ccc}\mathbf{i} & \mathbf{j} & \mathbf{k} \\ 2 & 1 & 5\end{array}\right\|=\binom{3}{9}$ | M1: Attempts $(2 \mathbf{i}+1 \mathbf{j}+5 \mathbf{k}) \times(\mathbf{i}-\mathbf{j}-2 \mathbf{k})$ | M1A1 |
|  | $\|1-1-2\|(-3)$ | A1: Any multiple of $\mathbf{i}+\mathbf{3 j}-\mathbf{k}$ |  |
|  | $(\cos \theta)=\frac{(\mathbf{3 i}-4 \mathbf{j}+\mathbf{2 k}) \cdot(\mathbf{i}+\mathbf{3} \mathbf{j} \mathbf{- k})}{\sqrt{3^{2}+4^{2}+2^{2}} \sqrt{1^{2}+3^{2}+1^{2}}} \quad\left(=\frac{-11}{\sqrt{29} \sqrt{11}}\right)$ |  | M1 |
|  | Attempts scalar product of normal vectors including magnitudes |  | dM1 A1 |
|  | 52 | Obtains angle using arccos (dependent on previous M1) |  |
|  | Do not isw and mark the final answer e.g. 90-52 = 38 loses the A1 |  | (5) |
| (c) | $\left\|\begin{array}{rrr}\mathbf{i} & \mathbf{j} & \mathbf{k} \\ 1 & 3 & -1\end{array}\right\|=\binom{2}{-5}$ | M1: Attempt cross product of normal vectors | M1A1 |
|  | $\left\|\begin{array}{lll}1-4 & 2\end{array}\right\|\binom{-5}{-13}$ | A1: Correct vector |  |
|  | $x=0:\left(0, \frac{5}{2}, \frac{15}{2}\right), \quad y=0:(1,0,1), \quad z=0:\left(\frac{15}{13}, \frac{-5}{13}, 0\right)$ |  | M1A1 |
|  | M1: Valid attempt at a point on both planes. A1: Correct coordinates May use way 3 to find a point on the line |  |  |
|  | $r \times(-2 i+5 j+13 k)=-5 i-15 j+5 k$ | M1: $\mathbf{r} \times \operatorname{dir}=$ pos.vector $\times \operatorname{dir}$ (This way round) <br> A1: Correct equation | M1A1 |
|  |  |  | (6) |


| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| (c) Way 2 | " $x+3 y-z=0$ " and $3 x-4 y+2 z=5$ uses their cartesian form of and eliminate $x$, or $y$ or $z$ and substitutes back to obtain two of the variables in terms of the third |  | M1 |
|  | $\begin{aligned} & \left(x=1-\frac{2}{5} y \text { and } z=1+\frac{13}{5} y\right) \text { or }\left(y=\frac{5 z-5}{13} \text { and } x=\frac{15-2 z}{13}\right) \text { or } \\ & \left(y=\frac{5-5 x}{2} \text { and } z=\frac{15-13 x}{2}\right) \end{aligned}$ |  | A1 |
|  | Cartesian Equations:$x=\frac{y-\frac{5}{2}}{-\frac{5}{2}}=\frac{z-\frac{15}{2}}{-\frac{13}{2}} \text { or } \frac{x-1}{-\frac{2}{5}}=y=\frac{z-1}{\frac{13}{5}} \text { or } \frac{x-\frac{15}{13}}{-\frac{2}{13}}=\frac{y+\frac{5}{13}}{\frac{5}{13}}=z$ |  |  |
|  | Points and Directions: Direction can be any multiple$\left(0, \frac{5}{2}, \frac{15}{2}\right), \mathbf{i}-\frac{5}{2} \mathbf{j}-\frac{13}{2} \mathbf{k} \text { or }(1,0,1),-\frac{2}{5} \mathbf{i}+\mathbf{j}+\frac{13}{5} \mathbf{k} \text { or }\left(\frac{15}{13},-\frac{5}{13}, 0\right),-\frac{2}{13} \mathbf{i}+\frac{5}{13} \mathbf{j}+\mathbf{k}$ |  | M1 A1 |
|  | M1:Uses their Cartesian equations correctly to obtain a point and direction <br> A1: Correct point and direction - it may not be clear which is which i.e. look for the correct numbers either as points or vectors |  |  |
|  | Equation of line in required form: e.g. $r \times(-2 i+5 j+13 k)=-5 i-15 j+5 k$ <br> Or Equivalent |  | M1 A1 |
|  |  |  | (6) |
|  |  |  | Total 14 |
| (c) <br> Way 3 | $\left(\begin{array}{c} 2 \lambda+\mu \\ \lambda-\mu \\ 5 \lambda-2 \mu \end{array}\right) \cdot\left(\begin{array}{r} 3 \\ -4 \\ 2 \end{array}\right)=5 \Rightarrow 12 \lambda+3 \mu=5$ | M1: Substitutes parametric form of $\Pi_{2}$ into the vector equation of $\Pi_{1}$ <br> A1: Correct equation | M1A1 |
|  | $\begin{aligned} & \mu=\frac{5}{3}, \lambda=0 \operatorname{gives}\left(\frac{5}{3},-\frac{5}{3}, \frac{10}{3}\right) \\ & \mu=0, \lambda=\frac{5}{12} \operatorname{gives}\left(\frac{5}{6}, \frac{5}{12}, \frac{25}{12}\right) \\ & \text { Direction }\left(\begin{array}{c} -2 \\ 5 \\ 13 \end{array}\right) \end{aligned}$ | M1: Finds 2 points and direction <br> A1: Correct coordinates and direction | M1A1 |
|  | Equation of line in required form: e.g. $r \times(-2 i+5 j+13 k)=-5 i-15 j+5 k$ <br> Or Equivalent |  | M1A1 |
|  | Do not allow 'mixed' methods - mark the best single attempt |  |  |
|  | NB for checking, a general point on the line will be of the form:$(1-2 \lambda, 5 \lambda, 1+13 \lambda)$ |  |  |
|  |  |  |  |

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