# Mark Scheme (Results) 

## Summer 2013

GCE Statistics 3 (6691/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATI CS

## General I nstructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.
8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.



| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3(a)i e.g e.g 3(a)ii e.g. | Quota Sampling: <br> Advantages: Fieldwork can be done quickly, or administering the test is easy, or costs are kept to a minimum (cheap), or gives estimates for each course. or OK for large populations or sampling frame not required (o.e.) <br> Disadvantages: Non-random process or not possible to estimate the sampling errors, or non response not recorded, or interviewer can introduce bias in sample choice. (o.e.) <br> Stratified Sampling: <br> Advantages: Can give accurate estimates as it is a random process, or gives estimates for each course or representative of [BUT not "proportional" to] the whole population. (o.e.) | B1 |
| e.g. | Disadvantages: Sampling frame required, or strata may not be clear as some students overlap courses or not suitable for large populations. (o.e.) | B1 |
| 3(b) | Total enrolments $=1000$ <br> (may be implied by calculations) <br> Leisure and Sport $=\frac{420}{1000} \times 100=42$ | B1 <br> M1 |
|  | $\begin{aligned} & \text { Information Technology }=\frac{337}{1000} \times 100=33.7=34 \\ & \text { Health and Social Care }=\frac{200}{1000} \times 100=20 \\ & \text { Media Studies }=\frac{43}{1000} \times 100=4.3=4 \end{aligned}$ | A1 |
| 3(c) | The college's information system would be used to identify each student and which course they are enrolled on. <br> i.e. idea of sampling frame or list for each course. <br> Use of random numbers to select required number of students from each course | B1 <br> B1 <br> (2) <br> Total 7 |
|  | Notes |  |
| (a) | Do not penalise for lack of context in part (a) <br> $1^{\text {st }} \mathrm{B} 1$ for an advantage and a disadvantage for quota sampling (must be $1^{\text {st }}$ or labelled (i)) $2^{\text {nd }} \mathrm{B} 1$ for an advantage and a disadvantage for stratified sampling ( $2^{\text {nd }}$ or labelled (ii)) <br> Do not allow opposite pairs e.g. "quicker/easier" for quota sampling and "takes a long time/more difficult" for stratified or quota "easy to use" but strat. "hard for large populations" <br> Do not allow same reason for both e.g. "gives estimates for each course" |  |
| (b) | M1 for one correct calculation, ft their " 1000 " <br> A1 for 42, 34, 20 and 4 only |  |
| (c) | $1^{\text {st }} \mathrm{B} 1$ for some mention of a suitable sampling frame. Need not give the specific term but a suitable source of list is required for all students in each course. <br> $2^{\text {nd }} \mathrm{B} 1$ for mentioning use of random numbers or some random selection process for each course. If they are describing systematic sampling score B0 here |  |



| Question <br> Number | Scheme Marks |
| :---: | :---: |
| 5 (a) | Let $L \sim \mathrm{~N}(50,25)$ and $S \sim \mathrm{~N}(15,9)$ <br> Let $X=L-\left(S_{1}+S_{2}+S_{3}\right)$ <br> $\mathrm{E}(X)=50-3 \times 15=5$ $\operatorname{Var}(X)=25+3 \times 9=52$ $\mathrm{P}(X<0) \quad=\mathrm{P}\left(Z<\frac{-5}{\sqrt{52}}\right)$ $=\mathrm{P}(Z<-0.693 . .)$ $=0.244 \text { or } 0.2451 \text { (tables) }$ <br> (awrt $0.244 \sim 0.245$ ) <br> Let $Y=L-3 S$ <br> $\mathrm{E}(Y)=50-3 \times 15=5$ $\operatorname{Var}(Y)=25+3^{2} \times 9=106$ $\begin{aligned} \mathrm{P}(Y>0) \quad & =\mathrm{P}\left(Z>\frac{-5}{\sqrt{106}}\right) \\ & =\mathrm{P}(Z>-0.4856 . .) \\ & =0.686 \text { or } 0.6879 \text { (tables) } \end{aligned}$ <br> (awrt $0.686 \sim 0.688$ ) |
|  | Notes |
| (a) | $1^{\text {st }} \mathrm{B} 1$ for forming a suitable variable $X$ explicitly seen. Do not give for $L-3 S$ but allow $L-(S+S+S)$ <br> $2^{\text {nd }} \mathrm{B} 1$ for $\mathrm{E}(X)=5$ (or -5 if their $X$ is defined the other way around) <br> $1^{\text {st }}$ M1 for an attempt at $\operatorname{Var}(X)=\operatorname{Var}(L)+3 \operatorname{Var}(S)$. Do not condone 5 for " 25 " or 3 for " 9 " <br> $1^{\text {st }}$ A1 for 52 <br> $2^{\text {nd }} \mathrm{dM} 1$ for attempting the correct probability and standardising with their mean and sd. <br> This mark is dependent on $1^{\text {st }}$ M1 so if $X$ is not being used or wrong variance score M0 <br> If their method is not crystal clear then they must be attempting $\mathrm{P}(\mathrm{Z}<-$-ve value $)$ <br> or <br> $\mathrm{P}(\mathrm{Z}>+$ ve value $)$ i.e. their probability after standardisation should lead to a prob. $<0.5$ <br> $2^{\text {nd }}$ A1 for awrt $0.244 \sim 0.245$ <br> Correct ans. only scores 5/6 (or 6/6 if $1^{\text {st }}$ B1) but must be clearly labelled as (a) or the first answer. <br> $1^{\text {st }} \mathrm{B} 1$ for defining a new variable $[Y=] \pm(L-3 S)$. May be implied by a correct variance. <br> $2^{\text {nd }} \mathrm{B} 1$ for $\mathrm{E}(Y)=5$ (or -5 if their $Y$ is defined as $Y=3 S-L$ ) <br> $1^{\text {st }}$ M1 for an attempt at $\operatorname{Var}(Y)=\operatorname{Var}(L)+3^{2} \operatorname{Var}(S)$. Do not condone 5 for " 25 " or 3 for " 9 " <br> $1^{\text {st }}$ A1 for 106 only <br> $2^{\text {nd }}$ dM1 for attempting the correct probability and standardising with their mean and sd. <br> This mark is dependent on $1^{\text {st }} \mathrm{M} 1$ so if $Y$ is not being used or wrong variance score M0 <br> If their method is not crystal clear then they must be attempting $\mathrm{P}(Z>$-ve value $)$ <br> or <br> $\mathrm{P}(\mathrm{Z}<+$ ve value $)$ i.e. their probability after standardisation should lead to a prob. $>0.5$ <br> $2^{\text {nd }}$ A1 for an awrt $0.686 \sim 0.688$ <br> Correct answer only scores 6/6 but must be clearly labelled as (b) or the second answer. |


| Question Number | Scheme ${ }^{\text {a }}$ ( Marks |
| :---: | :---: |
| 6 (a) |  |
|  | Notes |
| (a) ALT ALS | $1^{\text {st }} \& 2^{\text {nd }} \mathrm{B} 1$ for hypotheses. Accept $\mu_{1}, \mu_{2}$ or $\mu_{A}, \mu_{B}$ etc if there is some indication of which is which e.g. $A \sim N\left(\mu_{A}, 0.5\right)$ <br> $1^{\text {st }} \mathrm{M} 1$ for an attempt at se. Condone switching 0.5 and $0.75 \sqrt{\frac{0.5 \text { or } 0.75}{60}+\frac{0.75 \text { or } 0.5}{70}}$ <br> $1^{\text {st }} \mathrm{A} 1$ for a correct expression for denominator of test statistic or $0.138 \ldots$ or $\sqrt{0.0190 \ldots}$ <br> $2^{\text {nd }}$ A1 for a correct numerator of test statistic (must have the -1 ) <br> $3^{\text {rd }}$ A1 for awrt 3.62 <br> [Allow - 3.62 from numerator of $5.5-7--1$ and compatible $\mathrm{H}_{1}$ ] <br> $3^{\text {rd }} \mathrm{B} 1$ for $\pm 1.6449$ seen or <br> probability of 0.0002 (tables) or $0.000145 \ldots$ (calc) [allow 0.0001] <br> $2^{\text {nd }}$ dM1 dep. on $1^{\text {st }}$ M1 for a correct statement based on their normal cv and their test statistic <br> $2^{\text {nd }}$ A1 for correct comment in context. Must mention "yield" and "varieties" or "old" and "new" and " 1 " <br> If second B mark is B0 award A0 here <br> Pooled estimate: If they calculate $s_{p}=\sqrt{0.41845 \ldots}=0.64688 \ldots$...allow $1^{\text {st }} \mathrm{M} 1,1^{\text {st }} \mathrm{A} 1$ for expression (or awrt 0.114 ) and $2^{\text {nd }} \mathrm{A} 1$ if numerator correct but A0 for test statistic (4.39) <br> $1^{\text {st }} \mathrm{B} 1$ for mention of mean (yield) and normal (distribution) <br> $2^{\text {nd }} \mathrm{B} 1$ for mention of sample (size) being large in this case |

\begin{tabular}{|c|c|}
\hline Question Number \& Scheme \({ }^{\text {a }}\) \\
\hline \(7 \quad\) (a) \& \begin{tabular}{ll|l}
\(\hat{\mu}=\bar{x}=\frac{33.29}{8}=4.16125\) \& \((\) awrt 4.16) \& B1 \\
\(\hat{\sigma}^{2}=s^{2}=\frac{4.12^{2}+5.12^{2}+\ldots-8 \times \bar{x}^{2}}{7}\) \& M1 \\
\(\hat{\sigma}^{2}=s^{2}=\frac{141.4035-138.528013}{7}=0.41078 \ldots\) \& \((\) awrt 0.411) \& A1
\end{tabular} \\
\hline (b) \& \begin{tabular}{lr|l|l|l}
\(\sum x=33.29+32 \times 4.55=178.89\), \& \((3)\) \\
\(\sum x^{2}=" 141.4035 "+31 \times 0.25+32 \times 4.55^{2}(=811.6335)\) \& \((\) awrt 812) \& M1A1 \\
\& \& \\
Combined sample: \(s^{2}=\frac{811.6335-\frac{178.89^{2}}{40}}{39}=0.29724865 \ldots\). \& \((\) awrt 0.297) \& M1A1
\end{tabular} \\
\hline (c) \& \[
\begin{array}{rl|l}
\frac{s}{\sqrt{n}}=\frac{\sqrt{0.297 \ldots}}{\sqrt{40}}=0.0862 \& \text { (awrt 0.0862) } \& \text { M1A1 } \\
\begin{aligned}
\bar{x} \pm 1.96 \frac{\sigma}{\sqrt{n}} \& =\frac{178.89}{40} \pm 1.96 \frac{0.67}{\sqrt{40}} \\
\& =(4.2646 \ldots, 4.67988 \ldots)
\end{aligned} \& \text { M1B1 } \\
\& \& \text { awrt (4.26[or 4.265], 4.68) }
\end{array} \text { A1 }
\] \\
\hline \& Notes \\
\hline (a)
(b)

(c) \& | M1 for an attempt at $s^{2}$ : correct denom, clear attempt at $\sum x^{2}$ and ft their $\bar{x}$ Ans only $2 / 2$ |
| :--- |
| B1 for correct sum or mean or fully correct expression (accept mean = awrt 4.47) May be in (c) |
| $1^{\text {st }}$ M1 for their $141.4035+31 \times 0.25+32 \times 4.55^{2}$ or " 141.4035 " $+7.75+662.48$ (accept $3 s f$ ) |
| Beware: $\underline{32\left(0.25+4.55^{2}\right)+" 141.4035 " ~=~ a w r t ~} 812$ but scores M0A0. |
| $1^{\text {st }}$ A1 for a fully correct expression (all to 3sf or better) or answer only $=$ awrt 812 |
| $2^{\text {nd }} \mathrm{M} 1$ for a correct expression using their values |
| $3^{\text {rd }}$ M1 dependent on using a changed $s^{2}$ (not their 0.411 or 0.25 ) for $\frac{\sqrt{" 0.297 "}}{\sqrt{40}}$ |
| This $s^{2}$ must be based on a combination of their 0.411 and 0.25 e.g. 0.661 |
| M1 for $\bar{x} \pm z \times \frac{\sigma}{\sqrt{n}}$ for any $z(>1.5)$ and ft their $\bar{x}$ based on combining their 4.16 and 4.55, do not award for simply using 4.55 or their 4.16. Condone $\sigma=\sqrt{\text { their } 0.297}$ or their (b) |
| B1 for $z=1.96$ used in an attempt at a CI, may for example miss $\sqrt{n}$ |
| A1 for both limits awrt 3sf. Allow lower limit of 4.265 | <br>

\hline
\end{tabular}

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