# GCE 

Edexcel GCE
Mathematics
Statistics 4 (6686)

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Mark Scheme (Final)


J une 2008
6686 Statistics S4

## Mark Scheme

\begin{tabular}{|c|c|c|}
\hline Question Number \& Scheme \& Marks \\
\hline \multirow[t]{3}{*}{1 a} \& \begin{tabular}{l}
\[
\begin{array}{rlr}
\mathrm{E}\left(\theta_{1}\right) \& =\frac{\mathrm{E}\left(X_{3}\right)+\mathrm{E}\left(X_{4}\right)+\mathrm{E}\left(X_{5}\right)}{3} \\
\& =\frac{3 \mu}{3} \\
\& =\mu \quad \text { Bias }=0
\end{array}
\] \\
allow unbiased
\end{tabular} \& B1 \\
\hline \& \[
\begin{array}{rlr}
E\left(\theta_{2}\right) \& =\frac{E\left(X_{10}\right)-E\left(X_{1}\right)}{3} \\
\& =1 / 3(\mu-\mu) \quad \text { Bias }=-\mu \quad \text { allow } \pm \mu \\
\& =0 \quad
\end{array}
\] \& B1,B1 \\
\hline \& \begin{tabular}{l}
\[
\begin{aligned}
\mathrm{E}\left(\theta_{3}\right) \& =\frac{3 \mathrm{E}\left(X_{1}\right)+2 \mathrm{E}\left(X_{2}\right)+\mathrm{E}\left(X_{10}\right)}{6} \\
\& =\frac{3 \mu+2 \mu+\mu}{6} \\
\& =\mu \quad \text { Bias }=0
\end{aligned}
\] \\
allow unbiased
\end{tabular} \& \begin{tabular}{l}
B1 \\
(4)
\end{tabular} \\
\hline \multirow[t]{3}{*}{b} \& \[
\begin{aligned}
\operatorname{Var}\left(\theta_{1}\right) \& =\frac{1}{9}\left\{\left(\operatorname{Var} X_{2}\right)+\operatorname{Var}\left(X_{3}\right)+\operatorname{Var}\left(X_{4}\right)\right\} \\
\& =\frac{1}{9}\left\{\sigma^{2}+\sigma^{2}+\sigma^{2}\right\} \\
\& =\frac{1}{3} \sigma^{2}
\end{aligned}
\] \& M1

A1 <br>

\hline \& $$
\operatorname{Var}\left(\theta_{2}\right)=\frac{2}{9} \sigma^{2}
$$ \& B1 <br>

\hline \& \[
$$
\begin{aligned}
\operatorname{Var}\left(\theta_{3}\right) & =\frac{1}{36}\left\{9 \sigma^{2}+4 \sigma^{2}+\sigma^{2}\right\} \\
& =\frac{7}{18} \sigma^{2}
\end{aligned}
$$

\] \& | M1 |
| :--- |
| A1 | <br>

\hline ci) \& $\theta_{1}$ is the better estimator. It has a lower var. and no bias \& B1 depB1 <br>

\hline ii) \& $\theta_{2}$ is the worst estimator. It is biased \& $$
\begin{gathered}
\mathrm{B} 1 \\
\operatorname{dep} B 1 \\
(4)
\end{gathered}
$$ <br>

\hline
\end{tabular}

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 2 a | $\mathrm{H}_{1}: \sigma_{\mathrm{A}}^{2}=\sigma_{\mathrm{B}}{ }^{2} \quad \mathrm{H}_{0}: \sigma_{\mathrm{A}}{ }^{2} \neq \sigma_{\mathrm{B}}{ }^{2}$ | B1 |
|  | $\mathrm{SA}^{2}=22.5 \quad \mathrm{SB}^{2}=21.6 \quad$ awrt | M1 A1A1 |
|  | $\frac{s_{1}^{2}}{s_{2}^{2}}=1.04$ | M1 A1 |
|  | $\mathrm{F}_{(8,6)}=4.15$ | B1 |
|  | $1.04<4.15$ do not reject $\mathrm{H}_{0}$. The variances are the same. | B1 |
|  |  | (8) |
| b | Assume the samples are selected at random, (independent) | B1 <br> (1) |
| c | $s^{2} p=\frac{8(22.5)+6(21.62)}{14}=22.12 \quad \text { awrt } 22.1$ | M1 A1 |
|  | $\mathrm{H}_{0}: \mu_{\mathrm{A}}=\mu_{\mathrm{B}} \quad \mathrm{H}_{1}: \mu_{\mathrm{A}} \neq \mu_{\mathrm{B}}$ | B1 |
|  | $t=\frac{40.667-39.57}{\sqrt{22.12} \sqrt{\frac{1}{9}+\frac{1}{7}}}$ | M1 |
|  | $=0.462 \quad 0.42-0.47$ | A1 |
|  | Critical value $=t_{14}(2.5 \%)=2.145$ | B1 |
|  | $0.462<2.145$ No evidence to reject $H_{0}$. The means are the same | B1 <br> (7) |
| d | Music has no effect on performance | B1 |



2 sample test can score
MO MO
B 1 for $\mathrm{H}_{0}: \mu_{\mathrm{A}}=\mu_{\mathrm{B}} \quad \mathrm{H}_{1}: \mu_{\mathrm{A}}<\mu_{\mathrm{B}}$
M1 $\frac{9 \times 24.5+9 \times 17.16}{18}$
MO AO
B1 2.552
B1 ft
ie $4 / 8$

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 4a | $\bar{x}=668.125 \mathrm{~s}=84.428$ | M1 M1 |
|  | $T_{7}(5 \%)=1.895$ | B1 |
|  | Confidence limits $=668.125 \pm \frac{1.895 \times 84.428}{\sqrt{8}}$ | M1 |
|  | $\begin{aligned} & =611.6 \text { and } 724.7 \\ \text { Confidence interval } & =(612,725) \end{aligned}$ | A1A1 |
| b | Normal distribution | B1 |
| C | $£ 650$ is within the confidence interval. No need to worry. | B1 $\sqrt{\text { B1 }} \stackrel{(1)}{ }$ |
|  |  |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 5 a |  |  |
| b | $\begin{aligned} \text { Confidence interval } & =\left(\frac{15 \times 0.003}{27.488}, \frac{15 \times 0.003}{6.262}\right) \\ & =(0.00164,0.00719) \end{aligned}$ | $\begin{gathered} \mathrm{M} 1 \\ \mathrm{~B} 1 \mathrm{~B} 1 \\ \mathrm{~A} 1 \mathrm{~A} 1 \end{gathered}$ <br> (5) |
|  | $0.07^{2}=0.0049$ | M1 |
|  | 0.0049 is within the 95\% confidence interval. | A1 |
|  | There is no evidence to reject the idea that the standard deviation of the volumes is not 0.07 or The machine is working well. | A1 |
|  |  | (3) |




