

GCE

Mathematics

Advanced Subsidiary GCE

Unit 4725: Further Pure Mathematics 1

Mark Scheme for January 2013

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations and abbreviations

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT Follow through	
ISW	Ignore subsequent working
M0, M1 Method mark awarded 0, 1	
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC Special case	
٨	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning	
E1	Mark for explaining	
U1	Mark for correct units	
G1	Mark for a correct feature on a graph	
DM1 or M1 dep*	Method mark dependent on a previous mark, indicated by *	
cao Correct answer only		
oe Or equivalent		
rot	Rounded or truncated	
soi Seen or implied		
www	Without wrong working	

Subject-specific Marking Instructions for GCE Mathematics Pure strand

a. Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c. The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f. Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

g. Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h. For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

C	Question	Answer	Marks	Guidance
1	(i)	(2a-3 2)	B1	I or 3I seen or used
			B1	2 elements correct
			B1	Other 2 elements correct
			[3]	
1	(ii)	$\frac{1}{4a-1}\begin{pmatrix}4&-1\\-1&a\end{pmatrix}$ or equivalent	B1	Divide by correct determinant
			B1	Both diagonals correct
			[2]	
			M1*	Attached to some $1 (-1) (-1)$
2		$\frac{1}{6}n(n+1)(2n+1) - n$		Attempt to expand $(r-1)(r+1)$
		6	DM1	Use standard result for $\sum r^2$
			A1	Obtain correct unsimplified answer
			DM1	Attempt to factorise
		$\frac{1}{6}n(2n+5)(n-1)$	A2	Obtain completely correct answer
				Allow A1 if one bracket still contains a common factor
			[6]	
3	(i)	$ z = \sqrt{5}$	B1	Allow 2.2
		$argz = -26.6^{\circ} \text{ or } -0.464$	B1	Allow -27° or -0.46(3)
			[2]	
3	(ii)		B1	$z^* = 2 + i$ stated or used
			M1	Obtain two equations from real and imaginary parts
		a+b=2, b-a=-8 a=5, b=-3	A1	Obtain correct equations
			M1	Attempt to solve 2 linear equations
		a = 5, b = -3	A1	Obtain correct answers
			[5]	

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(Question	Answer	Marks	Guidance
4	(i)		M1	Substitute and attempt to simplify
		$4u^2 + 6u + k + 2 = 0$	A1	Obtain correct answer, must be an equation
4	(ii)	Either	[2]	
-	(11)	Luner	M1	Use products of roots of new quadratic i.e. use $(\pm) c/a$
		<i>k</i> + 2	A1ft	Obtain correct answer, from their quadratic
		4		
			[2]	
		Or	M1	Use sum and product of roots of original equation
		<i>k</i> + 2	Al	Obtain correct answer
		4		
5			M1	Show correct expansion process for correct 3 x 3
		$3\lambda^2 - 7\lambda + 2$	M1 A1	Correct evaluation of any 2 x 2 Obtain correct 3 term quadratic
		$3\lambda - 1\lambda + 2$	B1*	Equate their det to 0
		$\frac{1}{2}$ or 2	DM1	Attempt to solve a quadratic equation
		$\frac{-012}{3}$	A1	Obtain correct answers
			[6]	
6	(i)	$\begin{pmatrix} 1 & 2 \end{pmatrix}$	B1 B1	Each column correct
		$\begin{pmatrix} 0 & 2 \end{pmatrix}$	[2]	
6	(ii)	Either Or		Either Or
		$P: \begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \qquad \begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$	B1 DB1	Stretch, s.f. 2 in y direction Shear, x-axis invariant e.g. $(0,1) \rightarrow (2,1)$
		$\begin{pmatrix} 1 & 0 & 2 \end{pmatrix} \qquad \begin{pmatrix} 0 & 1 \end{pmatrix}$	B1	Correct matrix
		(1 1) $(1 0)$	B1 DB1	Shear, x axis invariant e.g. $(0, 1) \rightarrow (1, 1)$ Stretch, s.f.2 in y direction,
		$Q: \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \qquad \begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$	B1	Correct matrix
			[6]	N.B. "in the x/y axis" is incorrect
6	(iii)	$PO: \begin{pmatrix} 1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 4 \end{pmatrix}$	M1	Attempt at matrix multiplication of two 2 x 2 matrices from (ii)
		$PQ: \begin{pmatrix} 1 & 1 \\ 0 & 2 \end{pmatrix} \qquad \begin{pmatrix} 1 & 4 \\ 0 & 2 \end{pmatrix}$	A1	Obtain correct result cao
			[2]	

(Questio	n	Answer	Marks	Guidance
7	(i)	(a)		B1	Circle
				B1	Centre <i>O</i> and radius 2
				[2]	
7	(i)	(b)		B1	Horizontal line
				B1	(3, 1) on their line
				B1	$\frac{1}{2}$ line to left i.e. horizontal
				[3]	
7	(ii)			B1	Shade only inside their circle or above their horizontal line
				B1	Completely correct diagram
				[2]	
8	(i)			M1	Obtain correct numerator from addition or partial fractions
				A1	Obtain given answer correctly
	(1)			[2]	
8	(ii)			M1	Express at least three relevent terms using (i)
				A1	1 st three terms correct
			n	A1	Last two terms correct
			$\overline{(n+1)(n+2)}$		
				M1	Show correct cancelling
				A1	Obtain given answer correctly
				[5]	
8	(iii)		1	M1	Sum 1 to ∞ - 1 st term or start process at $r = 2$
			$-\frac{1}{6}$	A1	Obtain correct answer
			-	[2]	

(Question	Answer	Marks	Guidance
9	(i)		M1	Attempt at complete expansion
			A1	Obtain correct unsimplified answer
			A1	Obtain given answer correctly
			[3]	
9	(ii)	Either $\sum \alpha = -p, \sum \alpha \beta = -4, \alpha \beta \gamma = -3$	B1	State (anywhere) correct values for $\sum \alpha, \sum \alpha \beta, \sum \alpha \beta \gamma$
			M1	Express given expression as a single fraction
			A1	Obtain correct expression using (i)
			M1	Use their values for sum of roots etc. in their expression
		16 - 6p	A1	Obtain correct answer
		9		
			[5]	
		Or	D.I.	
			B1	Use substitution $1/\sqrt{u}$
		$9u^{3} + (6p - 16)u^{2} + (8 + p^{2})u - 1 = 0$	M1 A1	Rearrange appropriately and square out
		16 - 6p	M1	Obtain correct co-efficients of u^3 and u^2
		9	Al	Use (+/-)b/a from their cubic
10	(i)		B1	Obtain correct answer B1 x 3, Obtain 3 correct values
10	(1)	$\frac{2}{3}, \frac{2}{5}, \frac{2}{7}$	B1 B1	B1 x 5, Obtain 5 confect values
		3 5 /	B1	Justify given answer
			[3]	
10	(ii)	2	M1	Fraction, in terms of <i>n</i> , with correct numerator or denominator
		$\frac{2}{2n-1}$	A1	Obtain correct answer a.e.f.
			[2]	
10	(iii)	2	B1ft	Verify result true when $n = 1$, for their (ii), or $n = 2, 3$ or 4
		$\overline{2(n+1)-1}$	M1	Expression for u_{n+1} using recurrence relation in terms of <i>n</i> using their (ii)
			A1	Correct unsimplified answer
			A1	Correct answer in correct form
			B1	Specific statement of induction conclusion, previous 4 marks must be earned, $n=1$
			[5]	must be verified

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