GCE

## Mathematics

## Mark Scheme for June 2010

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| $1$ | $\begin{aligned} & \mathrm{t}=5 / 1.2 \\ & \mathrm{t}=4.17 \mathrm{~s} \end{aligned}$ | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | $\begin{array}{\|l\|} \hline 5=1.2 \mathrm{t} \text { or } 0=5-1.2 \mathrm{t} \\ 41 / 6 \mathrm{~s}, 4.166 \text { or better, } 4.16 \text { recurring. } \end{array}$ |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & \mathrm{s}=(-5)^{2} / 2 \times 1.2 \\ & \mathrm{~s}=10.4 \mathrm{~m} \end{aligned}$ <br> OR (using(i)) $\begin{aligned} & \mathrm{s}=5 \times 4.17-1.2 \times 4.17^{2} / 2 \\ & \mathrm{~s}=10.4 \mathrm{~m} \end{aligned}$ <br> OR (using(i)) $\begin{aligned} & \mathrm{s}=(5(+0)) / 2 \times 4.17 \\ & \mathrm{~s}=10.4 \mathrm{~m} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ {[2]} \\ \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ \hline \end{gathered}$ | $\mathrm{s}=5^{2} / 2 \times 1.2 \text { or } 5^{2}=2 \times 1.2 \mathrm{~s} \text { or } 0=5^{2}-2 \times 1.2 \mathrm{~s}$ <br> Accept 10 5/12, but not 10 <br> Time must be $>0$. Accept $\|t\|$ from (i) Award if \|-4.17| used. |
| iii | $\begin{aligned} & \mathrm{Fr}=3 \times 1.2 \\ & \mathrm{R}=3 \times 9.8 \\ & \mu=(3 \mathrm{x}) 1.2 /(3 \mathrm{x}) 9.8 \\ & \mu=0.122 \\ & O R \\ & \mathrm{R}=3 \times 9.8 \\ & \text { Mass } \times \text { acceleration }=+/-3 \times 1.2 \\ & +/-\mu \times 29.4=+/-3 \times 1.2 \\ & \mu=0.122 \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 <br> [4] <br> B1 <br> B1 <br> M1 <br> A1 | Accept 3.6, +/- <br> Accept 3g, +/- <br> Ratio of 2 positive numerical force terms <br> Not 0.12 <br> Accept 3g, +/- <br> Either both positive or both negative. |


| 2 | $\begin{aligned} & \hline+-(0.4 \times 3-0.6 \times 1.5) \\ & +/-(0.4 \times 0.1+0.6 \mathrm{v}) \\ & (0.4 \times 3-0.6 \times 1.5)=+/-(0.4 \times 0.1+0.6 \mathrm{v}) \\ & \text { speed }\|\mathrm{v}\|=0.433 \mathrm{~ms}^{-1} \\ & O R \\ & +/-(0.4 \times 3-0.4 \times 0.1)=+/-1.16 \\ & (0.6 \mathrm{v}+0.6 \mathrm{x} 1.5)=0.6 \mathrm{v}+0.9 \\ & 1.16=+/-(0.6 \mathrm{v}+0.9) \\ & \text { speed }\|\mathrm{v}\|=0.433 \mathrm{~ms}^{-1} \\ & \hline \end{aligned}$ | B1 B1 M1 A1 $[4]$ B1 B1 M1 A1 | $+/-0.3$ <br> Nb the terms have same signs Equating their total mom before \& after Accept $13 / 30$ or 0.43 recurring, but not 0.43 <br> Momentum change of P <br> Momentum change of Q <br> Equating momentum changes $0.26 / 0.6=v$ |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & +/-(0.4 \times 0.1-0.6 \mathrm{v}) \\ & (0.4 \times 3-0.6 \times 1.5)=+/-(0.6 \mathrm{v}-0.4 \mathrm{x} 0.1) \\ & \mathrm{v}=0.567 \\ & \mathrm{PQ}=0.1 \mathrm{x} 3+0.567 \times 3 \\ & \mathrm{PQ}=2 \mathrm{~m} \\ & O R \\ & +/-0.4 \times 3+0.4 \times 0.1 \text { and }+/-0.6 \mathrm{v}+0.6 \times 1.5 \\ & 1.24=+/-0.6 \mathrm{v}+0.9 \\ & \mathrm{v}=0.567 \end{aligned}$ etc | B1 <br> M1 <br> A1 <br> M1 <br> A1 <br> [5] <br> B1 <br> M1 <br> A1 | Nb the terms have different signs <br> Must use +/- same before momentum as in (i) <br> May be implied, or in any format <br> $(0.1+0.567) \times 3$ <br> Accept 2.00(1), 2.0, 2.00 <br> Both must be correct <br> Equating change in momentum <br> May be implied, or in any format |


| $3$ | $\begin{aligned} & \mathrm{H}=+/-(9-5 \cos 60) \\ & \mathrm{H}=6.5 \mathrm{~N} \end{aligned}$ | AG | $\begin{gathered} \hline \text { M1 } \\ \text { A1 } \\ {[2]} \end{gathered}$ | $+/-(9+5 \cos 120)$ |
| :---: | :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & \mathrm{V}=+/-(12-5 \sin 60) \\ & \mathrm{V}=7.67 \mathrm{~N} \end{aligned}$ |  | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ {[2]} \end{gathered}$ | $+/-(12+5 \cos 150)$ <br> Accept 7.666 or better, or 7.6 recurring |
| iii | $\begin{aligned} & \mathrm{R}^{2}=6.5^{2}+7.67^{2} \\ & \mathrm{R}=10.1 \mathrm{~N} \\ & \tan \mathrm{~A}=6.5 / 7.67 \text { or } 7.67 / 6.5 \\ & \mathrm{~A}=40(.3) \text { or } 49.7 \\ & \text { Bearing }=320^{\circ} \end{aligned}$ |  | M1 <br> A1 <br> M1 <br> A1 <br> A1 <br> [5] | Uses Pythagoras on forces V(ii) and 6.5 10.053.. <br> Uses trigonometry in relevant triangle <br> May be implied by final answer <br> As this is not a final answer, exact accuracy is not an issue <br> Or better |


| $\begin{aligned} & \hline 4 \\ & \text { i } \end{aligned}$ | $\begin{aligned} & 3.2-0.2 \mathrm{t}^{2}=0 \\ & \mathrm{t}=4 \mathrm{~s} \end{aligned}$ | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | Puts 0 for v and attempts to solve QE Accept dual solution +/-4 |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} \mathrm{a} & =-2 \mathrm{x} 0.2 \mathrm{t} \\ \mathrm{a} & =-0.4 \mathrm{x} 4 \\ \mathrm{a} & =-1.6 \mathrm{~ms}^{-2} \end{aligned}$ | $\begin{aligned} & \text { M1* } \\ & \text { D*M1 } \\ & \text { A1 } \\ & {[3]} \end{aligned}$ | Differentiates $v$ <br> Substitutes $+\mathrm{ve} \mathrm{t}(\mathrm{i})$ in derivative of v Negative only |
| iii | $\begin{aligned} & \mathrm{s}=3.2 \mathrm{t}-0.2 \mathrm{t}^{3} / 3(+\mathrm{c}) \\ & \mathrm{t}=0, \mathrm{~s}=0 \mathrm{soc}=0 \\ & \mathrm{~s}(4)=3.2 \mathrm{x} 4-0.2 \mathrm{x} 4^{3} / 3 \\ & \mathrm{~s}=8.53 \mathrm{~m} \end{aligned}$ | M1* <br> A1 <br> B1 <br> D*M1 <br> A1 <br> [5] | Integrates v , not multiplication by t <br> Or correct use of limits 0 and 4 Accept without/loss of c 8 8/15 Accept with/without c |


| $5$ | $\begin{aligned} & +/-3 \times 20 / 2 \\ & 30 \mathrm{~m} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & {[2]} \end{aligned}$ | Use area of scalene triangle(s). Not suvat. Accept -30 |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & (\mathrm{t}+4) \times 3 / 2=30 \text { or } 3 \mathrm{t} / 2=30-4 \times 3 \\ & \mathrm{t}=16 \text { or } \mathrm{t}=12 \\ & \mathrm{~T}=76 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ [4] | Equates scalene trapezium area to distance (i) $[(T-60)+4] \times 3 / 2=30$, award A2 |
| iii | $\begin{aligned} & \mathrm{T}(\mathrm{accn})=3 / 0.4 \quad(=7.5 \mathrm{~s}) \\ & \operatorname{decn}=3 /([76-60]-4-7.5) \\ & \operatorname{decn}=(+/-) 2 / 3 \mathrm{~ms}^{-2} \\ & O R \\ & \mathrm{~S}(\mathrm{accn})=3^{2} /(2 \times 0.4) \quad(=11.25 \mathrm{~m}) \\ & \operatorname{decn}=3^{2} /[2 \times(30-3 \times 4-11.25)] \\ & \operatorname{decn}=(+/-) 2 / 3 \mathrm{~ms}^{-2} \end{aligned}$ | B1 <br> M1 <br> A1 <br> [3] <br> B1 <br> M1 <br> A1 | Or $3=$ decn $x([76-60]-4-7.5)$ (+/-) 0.667 or better - accept 0.6 recurring <br> (+/-) 0.667 or better - accept 0.6 recurring |


| 6 | $\mathrm{T}-0.85 \mathrm{~g} \sin 30=0.85 \mathrm{a}$ | B1 | Either equation correct |
| :---: | :---: | :---: | :---: |
| i | $0.55 \mathrm{~g}-\mathrm{T}=0.55 \mathrm{a}$ | B1 | Both eqns correct and consistent 'a' direction |
| a | $\mathrm{a}=1.225 / 1.4$ | M1 | Solves 2 sim eqn |
|  | $\mathrm{a}=0.875$ | A1 |  |
|  | $\mathrm{T}=4.91$ | $\begin{aligned} & \mathrm{A} 1 \\ & {[5]} \end{aligned}$ | 4.908 or better - has to be positive |
| b | $\mathrm{F}=2 \mathrm{~T} \cos 30$ | M1 | Or Pythagoras or cosine rule |
|  | $\mathrm{F}=8.5(02 .$. | A1ft <br> [2] | $\operatorname{cv}(4.91) \mathrm{x} \sqrt{ } 3$ |
| ii |  | M1 | Uses $\mathrm{v}^{2}=\mathrm{u}^{2}+2 \mathrm{a}(1.5)$, u non-zero, a from (i) |
|  | $\mathrm{v}^{2}=1.3^{2}+2 \times 0.875 \times 1.5(=4.315)$ | A1ft | $\mathrm{v}=2.077 \ldots . .\left(\mathrm{v}^{2}=1.69+3 \mathrm{xcv}(0.875)\right)$ |
|  | $\mathrm{a}=+/-\mathrm{g} \sin 30$ | B1 | $\mathrm{a}=+/-4.9$ |
|  | $0=4.315-2 \mathrm{x} 4.9 \mathrm{~s}$ | M1 | Uses $0^{2}=u^{2}+/-2$ as, with a not $g$ or (i), $u$ not 1.3 |
|  | ( $\mathrm{s}=0.44 \ldots$ ) | A1 | May be implied - need not be 3sf |
|  | $\mathrm{S}=1.94$ | A1 [6] |  |


| 7 | $\begin{aligned} & \mathrm{Fr}=4+5 \sin 60 \\ & \mathrm{Fr}=8.33 \\ & \mathrm{R}=12-5 \cos 60 \\ & \mathrm{R}=9.5 \\ & \mu=(4+5 \sin 60) /(12-5 \cos 60) \\ & \mu=0.877 \end{aligned}$ | $\begin{gathered} \hline \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \\ {[6]} \end{gathered}$ | All 4 + component 5 (4 + 4.333(01)) <br> May be implied <br> +/-(All 12 - component 5 (12-2.5)) <br> May be implied, + ve from correct work <br> Friction/Reaction, $\mathrm{Fr}>4, \mathrm{R}<12$, both positive |
| :---: | :---: | :---: | :---: |
| ii | $\begin{aligned} & \text { Upper block } \\ & \mu=5 \sin 60 /(9-5 \cos 60) \quad(=4.3 / 6.5) \\ & \mu=0.666 \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \quad[2] \\ \hline \end{gathered}$ | (Component 5)/(9-component 5) |
| iii | Upper mass $=9 / \mathrm{g}$ <br> $(9 / \mathrm{g}) \mathrm{a}=5 \sin 60-0.1(9-5 \cos 60)$ $\mathrm{a}=4.01$ <br> Lower mass <br> Tractive force $=4+0.1(9-5 \cos 60)(=4.65)$ <br> Max Friction $=0.877(3+(9-5 \cos 60)(=8.33)$ <br> Tractive force $<$ Max Friction $\mathrm{a}=0$ <br> OR for Lower Mass $\mathrm{ma}=4+0.1(9-5 \cos 60)-0.877(3+9-5 \cos 60)$ <br> -ve a caused by friction impossible, hence $a=0$ | B1 M1 A1 M1 A1 A1 $[6]$ M1 A1 A1 | $0.918(36 .$. <br> N2L 0.918 (36..) $\mathrm{a}=4.33(01 .)-.0.1 \times 6.5$ <br> where friction $=0.1 x(9-$ component 5$)$ <br> Compares TF (tractive force) and max friction <br> N2L with 3 force terms: |

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