

# OCR

Oxford Cambridge and RSA

## Wednesday 23 May 2018 – Morning

### A2 GCE MATHEMATICS (MEI)

4763/01 Mechanics 3

#### QUESTION PAPER

Candidates answer on the Printed Answer Book.

##### OCR supplied materials:

- Printed Answer Book 4763/01
- MEI Examination Formulae and Tables (MF2)

##### Other materials required:

- Scientific or graphical calculator

**Duration:** 1 hour 30 minutes



#### INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the Printed Answer Book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the barcodes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.
- The acceleration due to gravity is denoted by  $g \text{ ms}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use  $g = 9.8$ .

#### INFORMATION FOR CANDIDATES

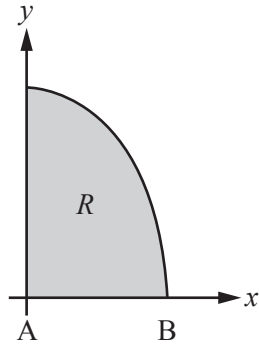
This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- The Printed Answer Book consists of **16** pages. The Question Paper consists of **4** pages. Any blank pages are indicated.

#### INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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- 1 The shaded region  $R$  in the  $xy$  plane is bounded by the axes and the part of the curve  $y = 8 - x^3$  that lies in the first quadrant as shown in Fig. 1. The points  $A$  and  $B$  on the boundary of  $R$  are at the origin and the point where the curve meets the positive  $x$ -axis, respectively.



**Fig. 1**

A uniform solid is formed by rotating  $R$  through one complete revolution about the  $x$ -axis.

- (i) Find the coordinates of the centre of mass of the solid. [7]

A uniform lamina is made in the shape of  $R$ .

- (ii) Show that the coordinates of the centre of mass of the lamina are  $\left(\frac{4}{5}, \frac{24}{7}\right)$ . [6]

The lamina is suspended freely from the point  $B$ .

- (iii) Calculate the angle that  $AB$  makes with the vertical. [3]

- 2 A smooth cylindrical pipe of internal radius 0.7 m is fixed in a position with its axis horizontal. A small ball of mass 0.1 kg is inside the pipe and is projected horizontally from the lowest point, A, of the pipe. The ball moves in a vertical plane perpendicular to the axis of the cylinder. The initial speed of the ball is  $5 \text{ m s}^{-1}$ . The point B is where the ball first reaches the same vertical level as the axis of the pipe. The ball is still in contact with the pipe at B. The cross-section of the pipe in which the ball moves and the positions of A and B are shown in Fig. 2.

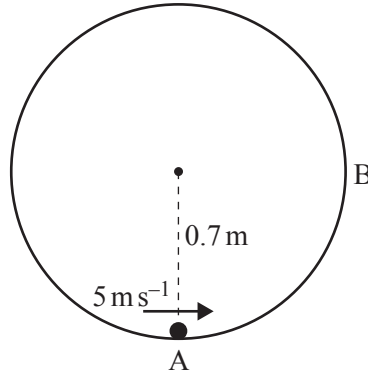


Fig. 2

- (i) Calculate the speed of the ball when it is at B. Calculate also the normal reaction of the pipe on the ball at B. [5]

The ball leaves the inner surface of the pipe at the point C. It subsequently passes through a point D which is vertically above A.

- (ii) Calculate the horizontal and vertical components of the velocity of the ball at C. [10]  
 (iii) Hence determine the distance AD. [5]

- 3 A light elastic string AB has natural length 0.8 m and modulus of elasticity 70 N. The end A is attached to a fixed point and the end B is attached to a particle of mass 1.2 kg.

The string and particle hang in equilibrium with B vertically below A.

- (i) Show that the stretched length of the string is 0.9344 m. [4]

The particle is now held at a point 1.3 m vertically below A and released from rest. In the subsequent motion the speed of the particle is  $v \text{ m s}^{-1}$  when it is at a height of  $h$  m above the release point.

- (ii) Show that, during the motion before the string becomes slack,  $v^2 = \frac{1}{3} (159.95h - 218.75h^2)$ . [6]  
 (iii) Find an expression for  $v^2$  in terms of  $h$  during the motion while the string is slack. [3]  
 (iv) Calculate the maximum speed of the particle during its motion. [4]

- 4 (a) A simple pendulum consists of a light rigid rod AB of length 1.25 m with a mass 0.8 kg attached to the end B and the rod hinged at the end A so that the rod can rotate freely in a vertical plane. The rod is held at rest with AB making an angle 0.1 radians with the downward vertical, and released from rest.
- (i) Show that the motion of the pendulum approximates to simple harmonic motion with period  $\frac{5}{7}\pi$  seconds. [6]
- (ii) Calculate the angular speed of the pendulum when it has turned through 0.05 radians from its initial position. [2]
- (iii) Calculate the time the pendulum takes to turn through 0.05 radians from its initial position. [2]
- (b) (i) Show that the dimensions of moment of force and the dimensions of kinetic energy are the same. [2]
- (ii) Given that angles are dimensionless, state the dimensions of angular speed and angular acceleration. [2]

A compound pendulum is formed when a rigid body is free to rotate about a fixed horizontal axis. The equation of motion of the compound pendulum is

$$\text{moment of weight} = -I\ddot{\theta},$$

where  $I$  is the moment of inertia of the compound pendulum and  $\ddot{\theta}$  is its angular acceleration.

- (iii) Use the equation of motion to deduce that  $I$  has dimensions  $ML^2$ . [2]

The kinetic energy,  $T$ , of the compound pendulum is believed to be given by the formula

$$T = km^\alpha I^\beta \dot{\theta}^\gamma,$$

where  $k$  is a dimensionless constant,  $m$  is the mass of the compound pendulum and  $\dot{\theta}$  is its angular speed.

- (iv) Use dimensional analysis to determine  $\alpha$ ,  $\beta$  and  $\gamma$ . [3]

**END OF QUESTION PAPER**

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