EXPERT TUITION

Maths Questions By Topic:

Geometry & Measures Mark Scheme

Edexcel GCSE (Higher)

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Old Spec A (Linear)

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| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 1 | 12 | P1 | for a process to find the area of cross section, | May use any letter for <i>h</i> or may use ? |
| | | P1 | eg 750 ÷ 25 (= 30) oe or $\frac{1}{2} \times 5 \times h$ oe for a correct equation in h | |
| | | | eg 750 ÷ 25 = $\frac{1}{2}$ × 5 × <i>h</i> oe or $\frac{1}{2}$ × 5 × <i>h</i> × 25 = 750 oe or for a complete process to find <i>h</i> | |
| | | | eg $\frac{750}{25} \times \frac{2}{5}$ oe or "30" × 2 ÷ 5 | |
| | | A1 | cao | |
| | | | SC B1 for answer of 6 if P0 scored | |
| 2 | Shown | M1 | for a correct expression for the area of one face of the cube, eg x^2 or a correct expression for the surface area of the cube, eg $6 \times x^2$ | No marks for $x = \sqrt{6\pi}$ without any working. |
| | | M1 | for a correct expression for the surface area of the sphere, eg $4 \times \pi \times 3^2 (= 36\pi)$ | |
| | | M1 | for forming a suitable equation, eg $6 \times x^2 = 4 \times \pi \times 3^2$ or $6x^2 = "36\pi"$ | $6 \times x^2 = 4 \times \pi \times 3^2$ $x^2 = 36\pi \div 6$ |
| | | A1 | for completing the method to $x = \sqrt{6\pi}$ or $k = 6$ | $x = \sqrt{6\pi}$ |
| | | | | |
| | | | | |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------|------|---|--|
| 3 (a) | 30 | P1 | for a start to the process, eg $5406 \div 6 (= 901)$ or $5400 \div 6 (= 900)$ or $5000 \div 6 (= 833.33)$ or $5410 \div 6 (= 901.66)$ | |
| | | P1 | for a process to find the length of one side, eg $\sqrt{901}$ or $\sqrt{900}$ or $\sqrt{833.33.}$ or $\sqrt{901.66.}$ | |
| | | A1 | for 30 | |
| (b) | Explanation | C1 | for a correct explanation based on their working in (a), eg underestimate because I rounded the total area down | Must be based on the use of a rounded value in a calculation |
| 4 | A & D | B1 | cao | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------------------------------|------|---|---|
| 5 | 85 with working and reasons | M1 | for correct use of corresponding angles eg $AEB = 63$ or co-interior angles eg $BCD = 180 - 148 (= 32)$ or $DEB = 180 - 63 (= 117)$ | Angles must be clearly labelled on the diagram or otherwise identified. Full solution must be seen. |
| | | M1 | (dep) for a complete method to find angle <i>EAB</i> eg. 180 – "63" – (180 – 148) or 148 – "63" or "117" – (180 – 148) | Correct method can be implied from angles on the diagram if no ambiguity or contradiction. |
| | | A1 | for $EAB = 85$ (identified) | |
| | | C2 | (dep on M2) all working correct with all appropriate reasons stated. <u>Corresponding</u> angles are equal <u>Allied</u> angles / <u>Co-interior</u> angles add up to 180 <u>Angles</u> on a straight <u>line</u> add up to 180 <u>Angles</u> in a <u>triangle</u> add up to 180 The <u>exterior angle</u> of a triangle is <u>equal</u> to the sum of the <u>interior opposite angles</u> . | When reasons are given the key words underlined must be present. Reasons need to be linked to their method; any reasons not linked, do not credit. There should be no incorrect reasons given. |
| | | (C1 | for one reason relating to parallel lines clearly used and stated or for any two reasons clearly stated for their fully correct method) | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|--|
| 6 | Proof | M1 | for $\overrightarrow{DQ} = \frac{1}{2} (\mathbf{b} - \mathbf{a})$ or $\overrightarrow{EQ} = \frac{1}{2} (\mathbf{a} - \mathbf{b})$ or | Vectors could be written on the |
| | | M1 | | diagram |
| | | 111 | for $PQ = \frac{1}{2} \mathbf{a} + DQ$ or $\frac{1}{2} \mathbf{a} + \frac{1}{2} (\mathbf{b} - \mathbf{a})$ oe | |
| | | | or $PQ = -\frac{1}{2} \mathbf{a} + \mathbf{b} + EQ$ or $-\frac{1}{2} \mathbf{a} + \mathbf{b} + \frac{1}{2} (\mathbf{a} - \mathbf{b})$ oe | |
| | | B1 | for $\overrightarrow{PQ} = \frac{1}{2} \mathbf{b}$ | |
| | | C1 | for complete proof with statement, eg $FE = 2PQ$ or FE is a multiple of PQ or $\mathbf{b} = 2(\frac{1}{2}\mathbf{b})$ | |
| | 0.5 | D1 | | |
| / | 0.5 | PI | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | |
| | | | eg $\frac{1}{8}\pi [(5x-1)^2 - (3x-1)^2]$ | |
| | | P1 | expand and simplify for either area A or area B | |
| | | | eg $\frac{1}{8}\pi (16x^2 - 4x)$ or $\pi (x^2 - 2x + 1)$ | |
| | | P1 | (dep P2) equate and rearrange into a quadratic eqn of the form $ax^2 + bx + c = 0$ eq $2x^2 + 3x - 2 = 0$ | |
| | | | | |
| | | P1 | (dep P3) factorise eg $(2x - 1)(x + 2) = 0$ or use of formula eg | |
| | | | $\frac{-3\pm\sqrt{3^2-4\times2\times-2}}{2\times2}$ | |
| | | A1 | oe | Accept only the single value of 0.5 oe |
| | | | | but award 0 marks for a correct answer with no supportive working |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------------|------|--|---|
| 8 | sketch | M1 | for sketch of a cylinder | Hidden edges may or may not be shown |
| | | A1 | sketch of cylinder, with dimensions shown | 2 (cm) for radius or 4 (cm) for diameter and 5 (cm) for height |
| 9 | c = -6 $d = -1$ | M1 | for reflection in x-axis shown on diagram | Vertices (3, -2), (5, -2), (3, -5) |
| | | A1 | for $c = -6$ or $d = -1$ | One correct value is M1A1 regardless of second value or diagram |
| | | A1 | for both $c = -6$ and $d = -1$ | |
| | | | SCB2 for $c = -1$ and $d = -6$ | |
| 10 | 8.5 | P1 | for process to use the area of <i>PQRS</i> to find the length of <i>PQ</i> , eg $10y = 45$ or $45 \div 10 (= 4.5)$ | Sets up equation for area |
| | | P1 | for process to use the perimeter of <i>ABCD</i> , eg $2x + 2 \times ``4.5'' = 26$ or $26 - 2 \times ``4.5'' (= 17)$ or $26 \div 2 (= 13)$ | Uses perimeter of <i>ABCD</i> |
| | | P1 | for process to use length of <i>BC</i> to find length of <i>AB</i> , eg solves $2x + 2 \times ``4.5'' = 26$ or $(26 - 2 \times ``4.5'') \div 2$ or $``13'' - ``4.5''$ | |
| | | A1 | for 8.5 or $8\frac{1}{2}$ | Accept $\frac{17}{2}$ |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|---------------|------|--|--|
| 11 | $\frac{1}{2}$ | M1 | for $\frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{2}$ or $\frac{\sqrt{3}}{3} \times \frac{\sqrt{3}}{2}$ or $(\frac{1}{2} \div \frac{\sqrt{3}}{2}) \times \frac{\sqrt{3}}{2}$ | |
| | | | OR $\tan 30 = \frac{1}{\sqrt{3}}$ oe or $\sin 60 = \frac{\sqrt{3}}{2}$ | |
| | | A1 | for $\frac{1}{2}$ or 0.5 | |
| 12 | 48 | M1 | for method to use a volume formula with correct substitution for the cone, sphere or hemisphere eg $\frac{1}{3} \times \pi \times 3^2 \times 10$ or $\frac{4}{3} \times \pi \times 3^3$ or $\frac{2}{3} \times \pi \times 3^3$ oe | May work without π or with an approximation of π ; must use the correct radius of 3 (and 10) in substitution |
| | | M1 | for complete method to find total volume eg $\frac{1}{3} \times \pi \times 3^2 \times 10 + \frac{2}{3} \times \pi \times 3^3$ | |
| | | M1 | (dep first M1) for correct partial simplification, eg 30π or 18π | Must be cone or hemisphere |
| | | A1 | cao | Accept 48π |
| | | | SC B2 for answer of 264 or 264π | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|---|
| 13 | shown | C1 | for method to find area of semicircle, eg $\pi \times 10^2 \div 2 \ (= 50\pi)$ | Can award first 3 marks if a value for π is used |
| | | C1 | for method to find area of quarter circle, for $\pi \times 20^2 \div 4 \ (= 100\pi)$ | |
| | | C1 | for a complete method to find area shaded and area of square, eg $\pi \times 20^2 \div 4 - \pi \times 10^2 \div 2$ and 20×20 | Working out to find the area of the shaded region must be shown |
| | | C1 | fully correct working leading to $\frac{\pi}{8}$ | |
| 14 (a) | 1 | B1 | cao | |
| (b) | 8 | M1 | starts process, eg cos(60) = $\frac{4}{x}$ or $0.5 = \frac{4}{x}$ oe or sin $30 = \frac{4}{x}$ or $\frac{\sin 30}{4} = \frac{\sin 90}{x}$ oe cao | All three elements of cos, 4, x must be present in an equation. eg cos = $4/x$ is acceptable but cos($4/x$) is insufficient |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--|----------|---|--|
| 15 | 21 | C1 C1 | for angle $OAB = 90 - 56 (= 34)$ for process to find angle $CAD (= 69)$ or angle $BCA (= 56)$ or angle $COA (= 138)$, eg use of alternate segment theorem or angle at centre is twice | Throughout, angles may be written on the diagram; accept as evidence if correct. Ignore absence of degree sign Reasons need not be given. |
| | | C1 | cao | |
| 16 | enlargement scale factor $-\frac{1}{3}$ | C2 | for all of: enlargement, (scale factor =) $-\frac{1}{3}$ oe, (centre =) (2, 2) | |
| | centre (2, 2) | (C1 | for two of: enlargement, (scale factor =) $-\frac{1}{3}$ oe, (centre =) (2, 2)) Note: award no marks if more than one transformation is given | |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|--|
| 17 | 3:4 | P1 | starts process eg $\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$ oe | |
| | | P1 | for process to find $\overrightarrow{OM} = \mathbf{a} + \frac{1}{2}$ "($\mathbf{b} - \mathbf{a}$)" or $(=\frac{1}{2}(\mathbf{a} + \mathbf{b}))$ | |
| | | P1 | for process to find $\overrightarrow{AP} = -\mathbf{a} + \frac{3}{5}$ " $(\frac{1}{2}\mathbf{a} + \frac{1}{2}\mathbf{b})$ " oe | |
| | | | or (indep) for $\overrightarrow{AN} = -\mathbf{a} + "k"\mathbf{b}$ | |
| | | P1 | process to find "k" using $\overrightarrow{AN} = -\mathbf{a} + "k"\mathbf{b}$ as a multiple of \overrightarrow{AP} | |
| | | A1 | cao | |
| | | | ALTERNATIVE | |
| | | P1 | for producing OM to C such that AC is parallel to OB | Formal geometric reasoning relating to |
| | | P1 | for process to show that $MC = OM$, using congruent triangles ACM and BOM | congruent and similar triangles is not |
| | | | for process to find <i>PC</i> as a multiple of $OM/5$ (= $7OM/5$) | required |
| | | P1 | for process to find ON as a multiple of $AC(OB)$ (= $3OB/7$) using similar | |
| | | P1 | triangles ACP and NOP | |
| | | Al | cao | |



| Question | | Answer | Mark | Mark scheme | Additional guidance |
|----------|---|--|------|--|--|
| 18 (a) | | isosceles triangle, base 6 cm, height 4 cm | M1 | for drawing an isosceles triangle or for drawing a triangle of base 6cm and height 4cm | Accept a freehand drawing Only a single triangle is acceptable; do not accept any attempted nets or 3-D diagrams |
| | | | A1 | for a fully correct diagram | Condone a perpendicular drawn from base to vertex |
| (b) |) | 96 cm ² | M1 | for a method to find the area of a triangular face eg $\frac{1}{2} \times 6 \times 5$ (= 15) | |
| | | | M1 | (dep) for finding the total surface area eg $4 \times "15" + 6 \times 6$ | |
| | | | A1 | for a numerical answer of 96 | Ignore incorrect or absent units for this mark |
| | | | | SC B1 for an answer of 84 if M0 scored | [The SC is from: $4 \times \frac{1}{2} \times 6 \times 4 + 6 \times 6$] |
| | | | B1 | cm ² | Ignore incorrect or absent numerical answer for this mark |

| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|---|----------|--|---|
| 19 | (22, 20) | P1 P1 | for process to find width or height of diagram eg $38 - 6 (= 32)$ or $36 - 7 (= 29)$ for process to find length of side of square eg " 32 " $\div 4 (= 8)$ or process to find half width of diagram eg " 32 " $\div 2 (= 16)$ | Figures may be shown on the diagram |
| | | P1 | for process to find <i>x</i> coordinate eg 6 + 2 × "8" (= 22) or 6 + "16" (= 22) or (6 + 38) ÷ 2 (= 22) | If $(6 + 38) \div 2$ leads to an answer other than 22, award P2 only |
| | | P1 | for process to find <i>y</i> coordinate eg 36 – 2 × "8" (= 20) or 36 – "16" (= 20) or 7 + "8" + "29" – 3 × "8" (= 20) | |
| | | A1 | cao SC: award 4 marks for (20, 22) | Award for P3 for (22, y) or (x, 20) or $x = 22$ or $y = 20$ |
| 20 | rotation 180° about $(-1, -2)$ | B2 | rotation 180° about $(-1, -2)$ or enlargement sf -1 centre $(-1, -2)$ | Condone missing brackets but do not accept centre written as a vector |
| | enlargement sf -1 centre $(-1, -2)$ | (B1 | rotation 180° or rotation about $(-1, -2)$ OB enlargement sf -1 or enlargement centre $(-1, -2)$ | Do not accept 'half turn' for 'rotation 180°' |
| | contro (1, 2) | | Award no marks for the description if more than one transformation is given | Ignore references to clockwise and anticlockwise |
| | | | SC B1 for fully correct diagram if B0 scored | Triangles at (-3, 1), (-5, 1), (-4, 3) and (-3, -5), (-5, -5), (-4, -7) |

| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|---------|------|--|--|
| 21 | 216 | P1 | for process to work with ratio eg $72 \div (3 + 4 + 5) (= 6)$ or $72 \div 12 (= 6)$ | |
| | | P1 | for process to find length of base or height of triangle eg $3 \times "6"$ (= 18) or $4 \times "6"$ (= 24) | |
| | | | OR process to find area scale factor eg "6" × "6" (= 36) | |
| | | P1 | complete process to find the area of the triangle eg $\frac{1}{2} \times "18" \times "24"$ or $\frac{1}{2} \times 3 \times 4 \times "6"^2$ | |
| | | A1 | cao | |
| 22 | 90 - 2x | M1 | for identifying an unknown angle eg $BAO = x$, $AOB = 180 - 2x$, $OBC = 90$, $ABC = 90 + x$ | Could be shown on the diagram alone |
| | | M1 | full method to find the required angle eg a method leading to $180 - x - x - 90$ | Needs to be an algebraic method Accept $x + x + 90 + y = 180$ for M2 |
| | | A1 | for $90 - 2x$ | |
| | | C2 | (dep M2) full reasons for their method, from base angles in an <u>isosceles triangle</u> are equal <u>angles</u> in a <u>triangle</u> add up to 180° a <u>tangent</u> to a circle is perpendicular to the <u>radius (diameter)</u> <u>angles</u> on a straight <u>line equal 180°</u> the <u>exterior angle</u> of a triangle is <u>equal</u> to the sum of the <u>interior</u> <u>opposite angles</u> | Underlined words need to be shown; reasons need to be linked to their method; any reasons not linked do not credit. |
| | | (C1 | (dep M1) for a <u>tangent</u> to a circle is perpendicular to the <u>radius</u> (diameter)) | Apply the above criteria |

| Question | Working | Answer | Mark | Notes |
|----------|--------------------------------------|-------------------------------|-----------------------|--|
| 23 | <i>CB</i> extended to form <i>CG</i> | Reasoning | B1 M1 C2 (C1 | for 35 or 75 or 145 or 105 or $DEF = 70$, marked on the diagram or 3 letter description for 180-70-35 or 180-75-35 or a correct pair of angles that would lead to 75 or 70, eg $AFB = 35$ and $FAB = 75$ or $AFB = 35$ and $ABG = 75$ or $FBC = 35$ and ABG = 75 or $EDF = 75$ and $DEF = 70$ or $FDC = 105$ and $FBC = 35$ or $ABC = 105and FBC = 35(dep on B1M1) All figures correct with all appropriate reasons stated. Angles must beclearly labelled or on the diagram. Full solution must be seen(dep on B1 or M1) for one reason clearly used and stated.)Corresponding angles are equal, alternate angles are equal, opposite angles in aparallelogram are equal, angles in a triangle sum to 180, angles on a straight line sumto 180, vertically opposite angles are equal, vertically opposite angles are equal,angles in a quadrilateral sum to 360, co-interior angles sum to 180, allied angles sumto 180, angles around a point sum to 360$ |
| 24 | | Daisy is wrong (supported) | P1 P1 A1 C1 | for process to find area of any relevant circle ie $\pi \times 4^2$ (=16 π), $\pi \times 7^2$ (=49 π), $\pi \times 10^2$ (=100 π) or 7^2 and 4^2 for completed method to find shaded area eg " $\pi \times 7^{2"}$ – " $\pi \times 4^{2"}$ (=33 π) or use of radii eg $7^2 - 4^2$ (=33) for 2 comparable figures, eg 33 π and 100 π or 33 and 100 or 103 to 103.7 and 314 to 314.2 or 103 to 103.7 and 104.6 to 104.8 statement eg No because it should be $\frac{33}{100}$ and their accurate figures Allow use of $\pi = 3$ or better |



| Question | Working | Answer | Mark | Notes |
|----------|---------|------------------|------|--|
| 25 | | Correct | B2 | Correct enlargement (-1,-1.5), (-1,-3.5) (-2,-1.5) |
| | | enlargement | | |
| | | | (B1 | correct size, correct orientation in incorrect position or 2 out of 3 vertices correctly |
| | | | | placed) |
| 26 | | $1 \pm \sqrt{2}$ | B1 | for a value for a known trigonometric ratio stated |
| 20 | | 1 + V Z | DI | |
| | | | P1 | for process to form 2 equations in a and b or one correct value stated |
| | | | | |
| | | | P1 | for complete process to solve to reach $a = 2$ and $b = 1$ |
| | | | A 1 | |
| | | | Al | for $1+\sqrt{2}$ oe |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---------------|------|---|
| 27 | | 70.5 | P1 | starts process of Pythagoras e.g. $5^2 + 12^2$ |
| | | | P1 | complete process for Pythagoras e.g. $\sqrt{5^2 + 12^2}$ or $\sqrt{25 + 144}$ or $\sqrt{169}$ (=13) |
| | | | P1 | (dep P1 for Pythagoras) process of adding all the lengths e.g. $5 + 5 + 12 + 12 + "13"$ (=47) |
| | | | P1 | (indep) process of multiplying at least 2 lengths by 1.5 |
| | | | A1 | cao SC: any evidence of working with Pythagoras award the P1 or P2 |
| 28 | | $\frac{2}{5}$ | P1 | for first step to solve the problem e.g. $\overrightarrow{AC} = -\mathbf{a} + \mathbf{c}$ or $\overrightarrow{OX} = \frac{1}{2}\mathbf{a} + \frac{1}{2}\mathbf{c}$ or demonstrates the location of <i>D</i> and <i>X</i> on the diagram |
| | | | P1 | for a correct vector statement using \overrightarrow{CD} eg $\overrightarrow{CD} = \overrightarrow{CX} + \overrightarrow{XD}$ or $\overrightarrow{CD} = \overrightarrow{OD} - \overrightarrow{OC}$ or $\overrightarrow{OD} = \frac{7}{2}\mathbf{c}$ |
| | | | P1 | or $\overrightarrow{CD} = 2.5\mathbf{c}$ oe for a correct equation or ratio using k eg equating $\overrightarrow{XD} = 3\mathbf{c} - \frac{1}{2}\mathbf{a} = \frac{1}{2}(-\mathbf{a} + \mathbf{c}) + \frac{1}{k}\mathbf{c}$ |
| | | | | or $\frac{\overrightarrow{OD}}{\overrightarrow{OC}} = \frac{k+1}{k}$ or $k = \frac{1}{2.5}$ or using a ratio approach eg $(\overrightarrow{OC} : \overrightarrow{CD}) = k : 1 = 1 : 2.5$ |
| | | | A1 | cao |



| Question | Working | Answer | Mark | Notes |
|----------|--|--------|------|---|
| 29 | | | C1 | states (angle) $ABC =$ (angle) BCD |
| | | | C1 | states $2^{nd} link AB = CD$ |
| | | | C1 | states 3^{rd} link with reason: $BC = BC$ (common) |
| | | | C1 | concludes proof by stating (triangle) $ABC \equiv$ (triangle) DCB with reason SAS and $AC = BD$ |
| 30 | | Proof | B1 | (indep) for stating $\cos 30 = \frac{\sqrt{3}}{2}$ |
| | | | M1 | for $PQ^2 = 10^2 + 10^2 - 2 \times 10 \times 10 \times \cos PBQ$ or $AC^2 = x^2 + x^2 - 2 \times x \times x \times \cos 30 (=x^2(2-\sqrt{3}))$ oe |
| | | | M1 | for $\cos PBQ = \frac{10^2 + 10^2 - PQ^2}{2 \times 10 \times 10}$ (implies previous M1) |
| | $\cos PBQ = \frac{10^2 + 10^2 - x^2(2 - \sqrt{3})}{2}$ | | M1 | for $\cos PBQ = \frac{10^2 + 10^2 - (x^2 + x^2 - 2 \times x \times x \times \cos 30)}{2 \times 10 \times 10}$ |
| | 200 | | | |
| | $=\frac{200-x^2(2-\sqrt{3})}{200}$ | | | |
| | | | A1 | conclusion of proof with all working seen |



| Question | Working | Answer | Notes |
|----------|---------|--------------------------------------|---|
| 31 | | 152 | M1 Start to method $ABD = 38^{\circ}$ and BAD or DBC or $DCB = 38^{\circ}$ |
| | | | M1 <i>ADB</i> or $BDC = 180 - 2 \times 38$ (=104) |
| | | | A1 for 152 with working |
| 32 | | Correct sketch | C1 interprets diagram eg. draw a solid shape with at least two correct dimensions |
| | | | C1 draws correct prism with all necessary dimensions. |
| 33 | | x = 21, y = 50 | P1 process to start solving problem eg. form an appropriate equation |
| | | | P1 complete process to isolate terms in <i>x</i> |
| | | | A1 for $x = 21$ |
| | | | P1 complete process to find second variable |
| | | | A1 $y = 50$ |
| 34 | | 6.4 | P1 Start to process eg. find scale factor (0.4) or $\frac{AE}{4} = \frac{4}{10}$ |
| | | | P1 Complete process to find area |
| | | | A1 |
| 35 (a) | | (-2, -2)(-6, -2) (-2,-4) (-4, -4) | M1 Shape drawn in correct orientation |
| | | | A1 |
| (b) | | Enlargement sf -0.5 centre (0,0) | C1 |



| Question | Working | Answer | | Notes | | |
|----------|---------|----------------------|----------------------------|---|---|--|
| 36 | | 42 | P1 P1 A1 | process to start problem solving eg forms an appropriate equation complete process to solve their equation cao | | |
| 37 | | 48 | P1 C1 P1 A1 | begins to work with rectangle dimensions eg $l+w=7$ or $2 \times l+w$ (=11) shows a result for a dimension eg using $l=4$ or $w=3$ begins process of finding total area eg $4 \times "3" \times "4"$ cao | | |
| 38 | | explanation | M1 M1 M1 M1 C1 | works with volume eg 240000 uses conversion 1 litre = 1000 cm^3 uses 8000 eg vol ÷ 8000 (=30) uses "30" eg "30" × 2.50 for explanation and 75 stated | begins working back eg $70 \div 2.50$ (=28) uses conversion 1 litre = 1000 cm ³ uses 8000 eg "28"× 8000 (=224000) works with vol. eg 240000 for explanation with 240000 and 224000 | |
| 39 (a) | | $\frac{\sqrt{3}}{2}$ | B1 | | | |
| (b) | | 6 | M1 A1 | starts process eg sin $30 = \frac{x}{12}$ answer given | | |



| Working | Answer | Notes |
|---------|---------|---|
| | SAS | M1 links angles PQR and PRQ (eg isosceles triangle) with full reasons |
| | | M1 links TR and SQ with full reasons |
| | | C1 gives full conclusion for congruency eg SAS |
| | 75π | P1 starts process by using $\frac{250}{3}\pi$ and $\frac{1}{2} \times \frac{4}{3}\pi r^3$ to find radius |
| | | P1 starts process using $\frac{1}{2}$ curved surface area eg $(4 \times \pi \times 5^{2}) \div 2$ |
| | | P1 complete process shown eg $(4 \times \pi \times "5"^2) \div 2 + (\pi \times "5"^2)$ |
| | | A1 for 75π |
| | | M1 states AB as $6\mathbf{b} - 3\mathbf{a}$ |
| | | M1 for $AX = \frac{1}{3}AB$ or $\frac{1}{3}$ "(6b - 3a)" or ft to 2b - a |
| | | M1 for $\overrightarrow{CY} = \overrightarrow{CB} + \overrightarrow{BY}$ or $6\mathbf{b} + 5\mathbf{a} - \mathbf{b}$ (=5 $\mathbf{b} + 5\mathbf{a}$) |
| | | M1 for $\overrightarrow{CX} = 3\mathbf{a} + \mathbf{a} - \mathbf{a}$ or $\overrightarrow{CX} = 6\mathbf{b} - \frac{2}{3}\mathbf{a} + \mathbf{b} - \mathbf{a}$ ($(= 2\mathbf{a} + 2\mathbf{b})$) |
| | | C1 for $\frac{2}{5}\overrightarrow{CY} = \frac{2}{5}(5\mathbf{a} + 5\mathbf{b}) = 2(\mathbf{a} + \mathbf{b}) = \overrightarrow{CX}$ |
| | Working | Working Answer SAS 75π |



| Question | Working | Answer | Notes | |
|----------|--|-------------------|-------|--|
| 43 | | No with | M1 | Derive <i>AC</i> =9 cm and identify as hypotenuse |
| | | reasoning | M1 | $4^2 + 7^2$ |
| | | | A1 | for using eg $AC = \sqrt{4^2 + 7^2}$ or 65 and 81 |
| | | | C1 | for concluding explanation that ABC is not a |
| | | | | right-angled triangle with evidence. |
| | | | | |
| 44 | | 500g | P1 | $\frac{1}{8} \times 160 \ (=20)$ |
| | | | P1 | 20' × 25 |
| | | | A1 | 500 (or 0.5) |
| | | | B1 | Correct units g (or kg) |
| | | | | |
| 45 | $x \times 2x \times 3x =$ | Reasoning to | M1 | Starts reasoning to find volume in terms of x |
| | | reach $x \le 5$ | | |
| | | | M1 | Gives inequality $6x^3 \le 900$ |
| | | | | or substitutes 5 and 6 into $6x^3$ |
| | | | MI | Completes reasoning to show $x \le 5$ |
| 16 | 4 2 4 2 2 2 | , x | D1 | Draces to find volume of early or homiorhers |
| 46 | $\frac{1}{3\times 2}\pi x^{3} + \frac{1}{3}\pi x^{3} = 2\pi x^{3}$ | $h = \frac{1}{2}$ | PI | Process to find volume of cone or nemisphere |
| | | | P1 | Process to total volume of solid |
| | $(2x)^2 \pi h = 4x^2 \pi h$ | | P1 | Process to find volume of cylinder |
| | $4x^2 \pi h = 2 \pi x^3$ | | P1 | Equates 2 volumes |
| | | | A1 | Reaches $h = \frac{x}{2}$ |
| | | | | |
| 47 | | Complete proof | M1 | Begins proof <i>BAE=ACD</i> and <i>ABE=EDC</i> |
| | | | MI | AB = DC because opposite sides of a |
| | | | C1 | parallelogram are equal |
| | | | CI | completes proof with all reasons eg alternate |
| | | | | angles are equal and reference to ASA |
| 18 | | 48 | P1 | Identifies that $16 \div 8 = 2$ so $PI = 2NP$ |
| 40 | | טד | P1 | Process to find area of LMN $8 \times (2+1)^2 (=72)$ |
| | | | P1 | Completes process to find area of LOM |
| | | | | ·72'-16 - 8 |
| | | | A1 | 48 cao |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|----------|--|---|
| 49 | 41.6 | P1 P1 | for start of process to find the length of the hypotenuse, eg (hyp ² =) 8 ² + 10 ² (= 164) for complete process to find hypotenuse, eg $\sqrt{8^2 + 10^2}$ or $\sqrt{64 + 100}$ or $\sqrt{164}$ (= 12.8) | Note lengths may be seen on the diagram |
| | | P1 | (dep P2) for complete process to find the required perimeter, eg $8+8+10+$ "12.8" + "12.8 - 10" or $16+4\sqrt{41}$ | 8 + 8+ "12.8" + "12.8" oe is acceptable for this mark |
| | | A1 | for answer in the range 41 to 42 | If an answer in the range 41 to 42 is given in the working space then incorrectly rounded, award full marks. |
| 50 (a) | 17.8 | M1 | for $\tan 56 = \frac{x}{12}$ or $(BC) = 12 \times \tan 56$ oe or alternative method to find BC | For any alternative method candidates must arrive at an equation with BC as the only unknown |
| | | A1 | for an answer in the range 17.7 to 17.8 | If an answer in the range 17.7 to 17.8 is given in the working space then incorrectly rounded, award full marks. |
| (b) | 33.6 | M1 | for $\cos x = \frac{15}{18}$ or $\cos x = 0.83$ or $x = \cos^{-1} \frac{15}{18}$ or alternative method to find x | For any alternative method candidates must arrive at an equation with x as the only unknown |
| | | A1 | for an answer in the range 33.5 to 33.91 | If an answer in the range 33.5 to 33.91 is given in the working space then incorrectly rounded, award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------------|------|---|--|
| 51 | 25 with reasons | M1 | for method to find angle <i>BCD</i> eg $180 \div (3 + 1)$ (= 45) or <i>BAD</i> = $180 \div (3 + 1) \times 3$ (=135) | Could be shown on the diagram or in working |
| | | M1 | for method to find angle BDA eg $180 - 20 - (180 - "45")$ (=25) or method to find angle SBD eg $SBD = BCD$ (=45) | Do not award if it ambiguous as to which angle is being found |
| | | C2 | for finding <i>SBA</i> (=25) and both reasons given, eg <u>Opposite angles</u> of a <u>cyclic</u> <u>quadrilateral</u> add up to 180 for angle <i>SBD</i> = 45 because <u>alternate segment</u> theorem | |
| | | (C1 | (dep M1) for one reason given <u>Opposite angles</u> of a <u>cyclic quadrilateral</u> add up to 180 for angle $SBD = 45$ because <u>alternate segment</u> theorem) | Underlined words need to be shown; reasons need to be linked to their method |
| | | | | |
| 52 (a) | 11.4 | M1 | for start to method to find the length of <i>BC</i> eg. $8^2 + 11^2 - 2 \times 8 \times 11 \times \cos 72$ | |
| | | M1 | (dep on M1) for method to use correct order of operations, eg. $64 + 121 - 54.38$ (= 130.61) | |
| | | A1 | for answer in the range 11.4 to 11.5 | If an answer within the given range is seen in working and rounded incorrectly award full marks. |
| (b) | 41.8 | M1 | for $0.5 \times 8 \times 11 \times \sin 72 (= 41.8)$ | Any alternative method must be complete |
| | | A1 | for answer in the range 41.5 to 41.9 | If an answer within the given range is seen in working and rounded incorrectly award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--|------|---|--|
| 53 | 99.5 | M1 | for sin (34) = $\frac{x}{178}$ oe or alternative method to find x | |
| | | A1 | for answer in range 99.5 to 99.7 | If an answer in the range 99.5 to 99.7 is given in the working space then incorrectly rounded, award full marks |
| 54 | $\begin{pmatrix} -9\\14 \end{pmatrix}$ | M1 | for $2\begin{pmatrix}3\\4\end{pmatrix} - 3\begin{pmatrix}5\\-2\end{pmatrix}$ or $\begin{pmatrix}6\\8\end{pmatrix}$ and $\begin{pmatrix}15\\-6\end{pmatrix}$ or $\begin{pmatrix}-9\\y\end{pmatrix}$ or $\begin{pmatrix}x\\14\end{pmatrix}$ | May be seen in two separate calculations eg $2 \times 3 + -3 \times 5$ and $2 \times 4 + -3 \times -2$ Condone incorrect notation if method is clear for this mark only |
| | | A1 | cao | |
| 55 | 35.3 | P1 | for starting the process to find length of third side of triangle, eg $9^2 - 6^2$ (= 45) or $6^2 + x^2 = 9^2$ | |
| | | P1 | for $\sqrt{9^2 - 6^2}$ or $\sqrt{81 - 36}$ or $\sqrt{45}$ or $3\sqrt{5}$ (= 6.7) or $r^2 = 45$ | |
| | | P1 | for stating or using $\pi \times [radius]^2 \div 4$ | [radius] is any value |
| | | A1 | for answer in range 35.2 to 35.4 | If an answer in the range 35.2 to 35.4 is given in the working space then incorrectly rounded, award full marks No working, answer only, no marks |
| | | | | |



| Question | Answer | Mark | Marks | scheme | Additional guidance |
|----------|--|------|---|---|---|
| 56 | 15.4 | M1 | for $\frac{AB}{\sin 34} = \frac{23.8}{\sin''120''}$ or $\frac{\sin 34}{AB}$ | $=\frac{\sin''120''}{23.8}$ | "120" comes from 180 – 26 – 34 |
| | | M1 | for $(AB =) \frac{23.8}{\sin"120"} \times \sin 34$ | | |
| | | A1 | for answer in range 15.36 to 15.4 | | If an answer in the range 15.36 to 15.4 is given in the working space then incorrectly rounded, award full marks |
| 57 | 116 | P1 | for setting up an equation, eg $(x + 4)^2 = x^2 + 70$ | for setting up an equation, eg $x^2 - (x - 4)^2 = 70$ | Equation must be in a single variable. If a candidate uses a trial and improvement method, it is either full marks or no marks. |
| | | P1 | for process to reduce equation down to a linear equation ready to solve eg $8x = 54$ oe | for process to reduce equation down to a linear equation ready to solve eg $8x = 86$ oe | Candidates must get as far as $ax = b$ |
| | | A1 | for 6.75 oe | for 10.75 oe | |
| | | B1 | ft (dep P2) for finding the area of B | or for answer in range 115 to 116 | |
| 58 | Enlargement sf - 1.5 centre $(1, 1)$ | B2 | for enlargement scale factor -1.5 an | id centre (1, 1) | Award no marks if more than one transformation is given |
| | (1, 1 <i>)</i> | (B1 | for enlargement scale factor –1.5 or | enlargement centre (1, 1)) | |
| | | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 59 | 160π | P1 | for process to find curved surface area of cone, eg $\pi \times 10 \times 25$ (= 250 π) (= 785) | |
| | | Р1 | for process to find the radius or diameter of the smaller cone eg $10 \times \frac{15}{25}$ (= 6) or $20 \times \frac{15}{25}$ (= 12) oe OR uses area scale factor, eg "250 π " × $\left(\frac{15}{25}\right)^2$ (= 90 π) | 15 comes from $25 - 10$ $\frac{15}{25}$ may be seen as 0.6 |
| | | P1 | for a complete process, eg " 250π " – $\pi \times$ "6" × 15 (= 785 – 282) or answer in range 502 to 503 | |
| | | A1 | for 160π | Award 0 marks for an answer of 160π or an answer in range 502 to 503 with no supportive working. If 160π seen but answer in range 502 to 503 given on answer line isw and award full marks |



| Question | Answer | Mark | Mark | scheme | Additional guidance |
|----------|-------------------|------|---|--|---|
| 60 | No (supported) | P1 | for finding the area of 3 or more faces of eg $(6 \times 8) + (8 \times 18) + (6 \times 18) \dots$ or "4 | f the cuboid and adding 8" + "144" + "108" (= 300) | Could be an addition of <i>any</i> three faces eg $48 + 48 + 144$ etc. |
| | | P1 | complete process to find surface area of eg $6 \times 8 \times 2 + 6 \times 18 \times 2 + 8 \times 18 \times 2$ (= | cuboid, = 600) | |
| | | P1 | for process to find side length of cube, eg [surface area] ÷ 6 and square rooting (= 10) | for a process to find the volume of the cuboid $6 \times 8 \times 18$ (= 864) and cube rooting (= 9.52) to find a side length | [surface area] must come from the addition of at least three attempts at area, but not from volume. |
| | | P1 | (dep on previous P1) for processes to find volume of cube and volume of cuboid, eg [side length] ³ (= 1000) and $6 \times 8 \times 18$ (= 864) | (dep on previous P1) for process to find surface area of cube, eg. ("9.52") ² × 6 (= 544.28) | |
| | | A1 | No with 1000 and 864 OR No with 600 | and 544(.28) | |
| 61 | 32.1 | P1 | starts process, eg $\sin 40 = \frac{DB}{8.6}$ oe or for | 8.6 × sin 40 (=5.52797) | Accept values rounded or truncated to 2 dp. |
| | | P1 | complete process to find <i>ED</i> , eg ($8.6 \times s$ | in40) ÷ 2 (=2.76) | |
| | | P1 | process to find angle <i>EAD</i> , eg $\tan^{-1}\left(\frac{"2}{}\right)$ | $\left(\frac{76''}{4.4}\right)$ or $\tan^{-1}(``0.628'')$ | |
| | | A1 | answer in range 32.09 to 32.2 | | If an answer in the range is seen in working and then incorrectly rounded award full marks |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------|------|---|---|
| 62 | 61 | B1 | angle $OAD = 90$, may be marked on diagram | Angle could be shown by a right-angle symbol |
| | | M1 | method to work out angle OAB (=29) | Correct method can be implied from angles on the diagram if no ambiguity or contradiction |
| | | A1 | cao | Reasons need not be given. |
| | | | | other working. |
| 63 | 155 | M1 | for a complete method to find the volume of the hemisphere, | |
| | | | eg $\frac{1}{2} \times \frac{4}{3} \times \pi \times 4.2^3$ oe | |
| | | A1 | answer in range 155 to 155.2 | If an answer in the range is seen in working and then incorrectly rounded award full marks |
| 64 | Description | C2 | for (rotation) 90° clockwise about (-1, 0) | Award 0 marks if there is reference to other |
| | | | or (rotation) 90° anticlockwise about $(-1, 6)$ or (rotation) 180° about $(-1, 2)$ | vectors (which is a translation) |
| | | | or (rotation) 180° about (-1, 4) | |
| | | (C1 | for (-1, 0) or (-1, 6) or (-1, 2) or (-1, 4)) | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|---|
| 65 | 8 | P1 | for working with volume of the cuboid, eg $30 \times 6 \times 19$ (= 3420) | For P marks, ignore attempts at unit conversion |
| | | | OR for using $\frac{4}{3}$ with one dimension, eg. $30 \times 2 \div 3 (= 20)$ | |
| | | P1 | for " 3420 " × 2 ÷ 3 (= 2280) or " 3420 " ÷ 3 (= 1140) | |
| | | | OR "20" \times 6 \times 19 (= 2280) OR "2420" \times 275 (= 12.4) | |
| | | | OR $^{-3}420^{+} \div 2/5 \ (= 12.4 = 12 \ \text{cups})$ | |
| | | P1 | (dep on P2) for "2280" \div 275 (= 8(.29)) or "1140" \div 275 (= 4(.14)) OR "12" \times 2 \div 3 | |
| | | | OR for $275 \times 8 \ (= 2200)$ or $275 \times 9 \ (= 2475)$ | |
| | | A1 | cao | |
| 88 | 9.85 | M1 | for $\sin(38) = \frac{CD}{16}$ oe | |
| | | | or alternative method to find AB | |
| | | A1 | for an answer in the range 9.76 to 9.92 | |
| | | | | |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|---|
| 89 | 25.4 | P2 | for finding the size of the angle eg $\frac{40 \times 360}{\pi \times 7^2}$ (=93.5(4)) or for working with proportion, eg $\frac{40}{49\pi}$ (=0.259(8) or 0.26) or $\frac{49\pi}{40}$ (=3.84(8) or 3.85) | |
| | | (P1 | for finding the area of the circle eg $\pi \times 7^2$ (=153(.938) or 154)) | May be embedded |
| | | Р1 | (dep on P2) for a process to find the arc length, eg $\frac{"93.5(4)"}{360} \times \pi \times 2 \times 7$ (=11.4(28)) or $\frac{40}{49\pi} \times \pi \times 2 \times 7$ (=11.4(28)) or $\pi \times 2 \times 7 \div \frac{49\pi}{40}$ (=11.4(28)) | |
| | | A1 | for answer in the range 25 to 25.44 | If an answer is shown in the range in working and then incorrectly rounded award full marks. Accept $\frac{178}{7}$ |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|------------------|------|--|--|
| 8: | 75° with reasons | M1 | for finding angle $BAD = \frac{180 - 40}{2}$ (= 70) or angle $BDA = \frac{180 - 40}{2}$ (= 70) | Could be shown on the diagram or in working |
| | | M1 | for finding angle $BCD = 180 - "70"$ (=110) or $40 + x + 70 + x = 180$ | |
| | | A1 | for finding angle $ADE = 75$ | |
| | | C2 | (dep M2) for <u>Opposite angles</u> of a <u>cyclic quadrilateral</u> add up to 180 and one other reason; all reasons given must be appropriate for their working Base angles of an <u>isosceles triangle</u> are equal <u>Angles</u> in a <u>triangle</u> add up to 180, <u>Angles</u> on a straight <u>line</u> add up to 180 [or <u>exterior angle</u> of a <u>cyclic</u> <u>quadrilateral</u> is equal to the <u>interior opposite angle</u>] | Underlined words need to be shown; reasons need to be linked to their method |
| | | (C1 | (dep M2) for <u>Opposite angles</u> of a <u>cyclic quadrilateral</u> add up to 180, or all other reasons given appropriate for their working) | Apply the above criteria |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 8; | 31.0 | P1 | for $\tan 35 = BE \div 15$ or $BE = 10.5(0)$ | $MB = \sqrt{9 \cdot 1 \cdot 5^2} = \sqrt{306} (=17.4(9) \text{ or } 17.5)$ |
| | | | OR finding the length DM = $\frac{2}{5} \times 15(=6)$ or MA = $\frac{3}{5} \times 15(=9)$ or 6:9 | $BE = 15 \times \tan 35 \ (=10.5(0))$ $AE = 15 \div \cos 35 \ (=18.3(1))$ |
| | | | OR showing the required angle on a diagram eg with an arc | $ME = \sqrt{9^2 \ 1 \ 8.31 \dots^2} = \sqrt{416. (3 \dots)}$ (=20.4(0)) |
| | | P1 | for $MB = \sqrt{15^2 + "9"^2}$ or $\sqrt{306}$ or 17.4(9) OR $ME = \sqrt{"9"^2} = 18.3(1)^{"2}$ or $\sqrt{416.(3)}$ or 20.4(0) | Check diagram for working |
| | | P1 | for using appropriate trigonometry ratio to set up an equation in angle <i>EMB</i> eg tan $\theta = "10.5(0)" \div "17.4(9)"$ or $\cos \theta = "17.4(9)" \div "20.4(0)"$ or $\sin \theta = "10.5(0)" \div "20.4(0)"$ | |
| | | A1 | for answer in the range 30.9 to 31 | If an answer is shown in the range in working and then incorrectly rounded award full marks. |



| Questi | on | Answer | Mark | Mark scheme | Additional guidance |
|--------|-----|------------|------|---|---|
| 92 | (a) | 2 a | M1 | for $\mathbf{a} - \mathbf{b} + \mathbf{a} + \mathbf{b}$ (=2a) | |
| | | | AI | cao | |
| | (b) | 4 | P1 | for a process to find $\overrightarrow{MF} = -0.5\mathbf{b} - \mathbf{a} - (\mathbf{a} - \mathbf{b}) (=0.5\mathbf{b} - 2\mathbf{a})$ or $\overrightarrow{CE} = \mathbf{a} + \mathbf{b}$ or $\overrightarrow{FM} = \mathbf{a} - \mathbf{b} + \mathbf{a} + 0.5\mathbf{b}$ (=2a-0.5b) | Accept ft from (a) providing vectors are clearly stated |
| | | | P1 | For finding a suitable vector expression for two of $(\overrightarrow{CE} \text{ or } \overrightarrow{EC})$, $(\overrightarrow{CX} \text{ or } \overrightarrow{XC}) \text{ or } (\overrightarrow{EX} \text{ or } \overrightarrow{XE})$ eg, $\overrightarrow{CX} = \mathbf{a} + 0.5\mathbf{b} + \frac{1}{n+1}(0.5\mathbf{b} - 2\mathbf{a})$ or $\overrightarrow{CX} = -\mathbf{a} + \mathbf{b} + \frac{n}{n+1}(2\mathbf{a} - 0.5\mathbf{b})$ $\overrightarrow{XE} = \frac{1}{n+1}(2\mathbf{a} - 0.5\mathbf{b}) + 0.5\mathbf{b}$ or $\overrightarrow{XE} = \frac{n}{n+1}(0.5\mathbf{b} - 2\mathbf{a}) + 2\mathbf{a}$ or $\overrightarrow{XC} = \frac{n}{n+1}(0.5\mathbf{b} - 2\mathbf{a}) + \mathbf{a} - \mathbf{b}$ or $\overrightarrow{XC} = \frac{1}{n+1}(2\mathbf{a} - 0.5\mathbf{b}) - 0.5\mathbf{b} - \mathbf{a}$ or $\overrightarrow{EX} = -0.5\mathbf{b} + \frac{1}{n+1}(0.5\mathbf{b} - 2\mathbf{a})$ or $\overrightarrow{EX} = -2\mathbf{a} + \frac{n}{n+1}(2\mathbf{a} - 0.5\mathbf{b})$ | $\overrightarrow{CX} = \frac{n-1}{n+1}\mathbf{a} + \frac{n+2}{2(n+1)}\mathbf{b} \qquad \overrightarrow{XE} = \frac{2}{n+1}\mathbf{a} + \frac{n}{2(n+1)}\mathbf{b}$ $\overrightarrow{XC} = \frac{1-n}{n+1}\mathbf{a} + \frac{-n-2}{2(n+1)}\mathbf{b} \qquad \overrightarrow{EX} = \frac{-2}{n+1}\mathbf{a} - \frac{n}{2(n+1)}\mathbf{b}$ |
| | | | P1 | for complete process to equate the coefficients of a and b eg $\frac{n-1}{n+1} = \frac{n+2}{2(n+1)}$ | |
| | | | A1 | cao | |
| | | | | ALTERNATIVE | |
| | | | P1 | for a process to find $\overrightarrow{MF} = -0.5\mathbf{b} - \mathbf{a} - (\mathbf{a} - \mathbf{b}) (=0.5\mathbf{b} - 2\mathbf{a})$ or $\overrightarrow{CE} = \mathbf{a} + \mathbf{b}$ or $\overrightarrow{FM} = \mathbf{a} - \mathbf{b} + \mathbf{a} + 0.5\mathbf{b}$ (=2 $\mathbf{a} - 0.5\mathbf{b}$) | Accept ft from (a) providing vectors are clearly stated |
| | | | P1 | For finding two suitable vector expressions for \overrightarrow{FX} eg $\overrightarrow{FX} = \frac{n}{n+1}(2\mathbf{a} - 0.5\mathbf{b})$ and $\overrightarrow{FX} = \mathbf{a} - \mathbf{b} + k\mathbf{a} + k\mathbf{b}$ | |
| | | | P1 | for complete process to equate the coefficients of a and b eg $\frac{2n}{n+1} - 1 = 1 - \frac{n}{2(n+1)}$ | |
| | | | A1 | cao | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------------|----------|---|---|
| 93 | 60 | M1 | use of parallel lines to find an angle eg <i>ABE</i> =70 or <i>EBG</i> =75 or <i>EBC</i> = 110 or shows parts of <i>x</i> as 35 or 25 | Parts of <i>x</i> should be identified on the diagram by the insertion of a dividing line through angle <i>x</i> (need not be identified or drawn parallel). |
| | | M1 | for a complete method to find angle <i>x</i> ; could be in working or on the diagram | Correct method can be implied from angles on the diagram if no ambiguity or contradiction. |
| | | A1 | for $x = 60$ | |
| | | C1 | (dep on M1) for one reason linked to parallel lines and one other reason, supported by working taken from: <u>alternate</u> angles are equal, <u>allied</u> angles / <u>co-interior</u> angles add up to 180, <u>angles</u> on a straight <u>line</u> add up to 180, <u>angles</u> in a <u>triangle</u> add up to 180° | Underlined words need to be shown; reasons need to be linked to their method; any reasons not linked do not credit. There should be no incorrect reasons given. |
| 94 | Rotation | M1 | stating rotation | Award for a triangle in the correct position |
| | | | or for showing R [(1,1), (1,-3), (3,-3)] | without the label R as long as this is the only triangle in lower right quadrant. |
| | 90° anticlockwise | A1 | for rotation of 90° anticlockwise | Accept rotation of 270° clockwise |
| | centre $(-1,1)$ | A1 | for centre $(-1, 1)$ given as a coordinate. | Can be given as a coordinate alone. Do not award A marks if there is evidence of other transformations in the description, or other ambiguity in the answer given. |
| 95 | 84.9 | P1 P1 | shows a process to find the radius or diameter eg $44 = 2 \times \pi \times r$ or $r = \frac{22}{\pi}$ or $d = \frac{44}{\pi}$ or $r = 7.0028$ or $d = 14.0056$ (dep on P1) complete method to find the area | Allow <i>r</i> in the range 7 to 7.1 and <i>d</i> in the range 14 to 14.1 Could be shown on the diagram. |
| | | | eg $\frac{1}{2} \times d^{2} \times \sin 60$ oe, $\frac{1}{2} \times 14 \times \tan 60$ oe, $\frac{1}{2} \times 14 \times \sqrt{14^{2} - 7^{2}}$ oe | |
| | | A1 | for answer in the range 84.8 to 85 | If the correct answer in the range is given in working and then rounded incorrectly award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|---|
| 96 | 3.75 | P1 | works to find vol of frustum eg $1/3\pi(3.6)^2 \times 6.4 - 1/3\pi(1.8)^2 \times 3.2$ | |
| | | | or 86.858 -10.857 (=24.192 π or 76.00) | |
| | | P1 | works to find vol of hemisphere eg $\frac{1}{2} \times \frac{4}{3}\pi \times 3.6^3$ (=31.104 π or 97.7) | 781.7 by use of diameter does not get the mark |
| | | P1 | mass of frustum as [vol]×density eg "76.00" × 2.4 (=182.4) or mass of hemisphere as [vol]×density eg "97.7"×4.8 (=469.037) | [vol] is their volume which could be ft using the radius, using the diameter, or could be another value as long as it is stated as being the volume, or clearly intended from working. |
| | | P1 | mean density as total mass ÷ total volume | All figures must come from correct method |
| | | | eg ("182.4" + "469.037") \div ("76" + "97.7") | shown. |
| | | | or "651.4" ÷ "173.7" | |
| | | | | |
| | | A1 | answer in the range 3.7 to 3.8 | |
| 07 | proof | C1 | uses evaluating and ag if $CAP = r$ then $CPO = 180$, r (Opposite angles of | Underlined words need to be shown: reasons |
| 97 | ргоог | CI | a <u>cyclic quadrilateral</u> add up to 180° .) | need to be linked to their method; any reasons not linked do not credit. |
| | | C1 | establishes relationship outside a circle eg $ORB = x$ (<u>Angles</u> on a straight <u>line</u> add up to 180) | Correct method can be implied from angles on the diagram if no ambiguity or contradiction. |
| | | C1 | uses properties of a circle eg $RO = OB$ (both radii) so $ABC = x$ (Base angles of an <u>isosceles triangle</u> are equal.) | |
| | | C1 | Complete proof and conclusion | Full reasons given without any redundant reasons and correct reasoning throughout. |


| Questi | on | Answer | Mark | Mark scheme | Additional guidance |
|--------|-----|--|------|--|---|
| 78 | | Enlargement | B2 | for correct enlargement at (1,2) (2,3) (2,4) (1,4) | |
| | | | (B1 | for correct size and orientation in the wrong position OR 3 of 4 vertices correct and joined OR 4 correct vertices not joined) | |
| 99 | (a) | Diagram | B1 | for correct vector drawn including arrow | May be drawn anywhere on the grid. |
| | (b) | $\left(\begin{array}{c}3\\4\end{array}\right)$ | M1 | for $\mathbf{a} + 2\mathbf{b}$ drawn with resultant vector or for writing \mathbf{a} and \mathbf{b} as column vectors and attempt to add $\mathbf{a} + 2\mathbf{b}$, eg $\binom{1}{2} + 2 \times \binom{1}{-3}$ or $\binom{1+2}{c}$ or $\binom{d}{2+-6}$ or $\binom{-4}{3}$ | Accept consistent incorrect notation for M1 |
| | | | A1 | cao | |
| 9: | (a) | Shown | M1 | for finding one missing angle eg $BDE = y$ or $ODE = 90$ or $ODF = 90$ or $DBO = x$ or $BCD = 180 - y$ or (reflex) $BOD = 2y$ | Could be shown on the diagram or in working |
| | | | A1 | for a complete correct method leading to $y - x = 90$ | |
| | | | C1 | (dep on A1) for all correct circle theorems given appropriate for their working eg The <u>tangent</u> to a circle is perpendicular (90°) to the <u>radius</u> (<u>diameter</u>) <u>Alternate segment</u> theorem OR <u>Angle</u> at the <u>centre</u> is <u>twice</u> the <u>angle</u> at the <u>circumference</u> Opposite angles in a <u>cyclic quadrilateral</u> sum to 180° | |
| | (b) | Explanation | C1 | for explanation eg No as y must be less than 180 as it is an angle in a triangle | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 9; | 39.5 | P1 | for a start to a process eg, for a correct trigonometric statement, eg sin48 = $\frac{7.3}{AC}$ or cos42 = $\frac{7.3}{AC}$ or $\frac{AC}{sin90} = \frac{7.3}{sin48}$ OR angle <i>CAH</i> unambiguously identified on a diagram | Must include correct values |
| | | Р1 | for a complete correct process to find <i>AC</i> , eg (<i>AC</i> =) $\frac{7.3}{\sin(48)}$ (=9.8) or (<i>AC</i> =) $\frac{7.3}{\cos(42)}$ (=9.8) or (<i>AC</i> =) $\sin 90 \times \frac{7.3}{\sin 48}$ (=9.8) | |
| | | P1 | for a correct statement using angle <i>CAH</i> , eg tan(<i>CAH</i>) = $\frac{8.1}{"9.8"}$ OR $\sqrt{8.1^2 + "9.8"^2}$ (=12.7) and $\frac{\sin CAH}{8.1} = \frac{\sin 90}{"12.7"}$ | |
| | | A1 | for answer in the range 39.5 – 39.51 | If an answer is given in the range but then incorrectly rounded award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| :2 | 905 | P1 | for correct use of formula for the volume of a sphere eg $\frac{1}{4} \times \frac{4}{3} \times \pi \times r^3$ (= 576 π or 1809) OR 576 $\pi \times 4$ or 2304 π or 7238($\frac{4}{3} \times \pi \times r^3$) | We do not need to see what is in the brackets to award this mark. The contents of the bracket alone would score P0 |
| | | P1 | for a complete correct process to find <i>r</i> , eg $r = \sqrt[3]{\frac{576 \times 4 \times 3}{4}}$ or $r = 12$ | Could be shown in several stages $\sqrt[3]{\frac{576 \times 4 \times 3}{4}} = \sqrt[3]{1728}$ |
| | | P1 | for a process to find the curved surface area eg $\frac{4 \times \pi \times [radius]^2}{4}$ (=144 π or 452) OR the surface area of both flat surfaces eg $(2 \times \frac{\pi \times [radius]^2}{2})$ OR complete expression for the total surface area eg $\frac{4\pi r^2}{4} + \frac{\pi r^2}{2} \times 2$ oe | Radius used must be clearly identified as their radius of the solid |
| | | P1 | for process to find the complete surface area eg $\frac{4 \times \pi \times [radius]^2}{4} + (2 \times \frac{\pi \times [radius]^2}{2})$ | |
| | | A1 | answer in the range $904.7 - 905$ or 288π (SCB2 for an answer in the range $358.1 - 359.2$) | If an answer is given in the range but then incorrectly rounded, award full marks. |



| Question | Working | Answer | Mark | Notes |
|----------|---------|------------------------------------|----------------------|--|
| : 3 | | 31.4 | P1 | for working with circumference formula, eg $\pi \times 80$ (=251) oe |
| | | | A1 | for answer in the range 31.4 to 31.5 accept 10π |
| :4 (a) | | (-2, 1) (-4, 1) (-2, 2) (-5, 2) | B1 | Shape labelled A |
| (b) | | (1, -4) (3, -4) (1, -5) (4, -5) | B1 | Shape labelled B |
| : 5 | | 32.3 | P1 P1 P1 P1 | for using Pythagoras to find length of third side of triangle, eg $7.5^2 - 6^2$ or $6^2 + x^2 = 7.5^2$ or uses trigonometry to find angle in triangle, eg sin $A = \frac{6}{7.5}$ or cos $B = \frac{6}{7.5}$ (dep P1) for complete process to find length of third side of triangle eg $\sqrt{7.5^2 - 6^2}$ or $\sqrt{56.25 - 36}$ or $\sqrt{20.25}$ (= 4.5) or uses trigonometry to find base length of triangle, eg $7.5 \times \cos "A"$ or $7.5 \times \sin "B"$ or $\frac{6}{\tan "A"}$ (dep P2) for 24 - 10 - "4.5" (= 9.5) (indep) for process to find angle <i>CDA</i> , eg tan <i>CDA</i> = $\frac{6}{\text{base}}$ from right- angled triangle |
| | | | A1 | for answer in the range 32.2 to 32.3 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|----------------------|------|--|
| :6 | | 15 | P1 | for a process to find the interior or exterior angle of a regular 12 sided polygon e.g. $\frac{10 \times 180}{12}$ (= 150) or $\frac{360}{12}$ (= 30), must be no contradictions |
| | | | P1 | for process to find angle <i>STR</i> , eg $\frac{180 - "150"}{2}$ or $\frac{"30"}{2}$ |
| | | | A1 | cao |
| :7 | | Proof (supported) | M1 | for a method to find coordinates of $M(-1, -1)$ or $N(3, 1)$ |
| | | | M1 | for method to find gradient of MN or PR |
| | | | | or for method to find column vector for MN or PR |
| | | | | or for differences of x coordinates and differences of y coordinates for MN or PR |
| | | | A1 | for gradients of MN and PR , ie $\frac{1}{2}$ oe |
| | | | | or for column vectors of <i>MN</i> and <i>PR</i> , $\overrightarrow{MN} = \binom{4}{2}$ and $\overrightarrow{PR} = \binom{8}{4}$ |
| | | | | or for differences of x coordinates and of y coordinates for MN and PR |
| | | | C1 | for conclusion from reasoning and correct working |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| : 8 | | 68.5 | B1 | for angle $OAB = 90^{\circ}$ or angle $OCB = 90^{\circ}$, may be seen on diagram |
| | | | P1 | for a process to find the length of <i>AB</i> or the length of <i>CB</i> (= $10\sqrt{3}$ oe) eg $10 \times \tan 60^\circ$ (= 17.3) or the length of <i>OB</i> (= 20), eg $10 \div \cos 60^\circ$ |
| | | | P1 | for a process (dep previous P1) to find the area of the triangle OAB (= 50 $\sqrt{3}$ oe) or area of triangle OCB (= 50 $\sqrt{3}$ oe) or area of kite $OABC$ (= 100 $\sqrt{3}$ oe) |
| | | | P1 | for a process to find the area of the sector <i>OAC</i> e.g. $\frac{1}{3} \times \pi \times 10^2$ (= 104.7),accept rounded or truncated to 3 significant figures or more |
| | | | A1 | for 68.4 – 68.6 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|-----------------|------|---|
| :9 | | Side elevation | C2 | for the side elevation (4 cm by 2 cm rectangle with a solid line drawn 1 cm from the 2 cm edge, and correct orientation) |
| | | | [C1 | for the side elevation as a rectangle] |
| | | Front elevation | C2 | for the front elevation as a trapezium in correct orientation with base 4 cm, parallel sides 1 cm and 4 cm |
| | | | [C1 | for the front elevation as a trapezium with two right angles] |
| | | No | M2 | for the correct position of C or F |
| •• | | (supported) | IM12 | for a correct position of B or Dl |
| | | (supported) | C1 | for No with correct supporting evidence, eg. showing C and E in the correct positions |
| | | | | OR |
| | | | M2 | for C is a rotation of 90° anticlockwise about O or E is a rotation of 90° clockwise about O for No with supporting evidence, eg. C is a rotation of 90° anticlockwise about O and E is a rotation of 90° clockwise about O |
| | | | C1 | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|----------------------|---|
| :; | | Proof | C1 | for identifying one pair of equal angles with a correct reason, e.g. (angle) $BAE =$ (angle) CDE ; <u>angles</u> in the same <u>segment</u> are equal or <u>angles</u> at the circumference <u>subtended</u> on the same <u>arc</u> are equal or for identifying two pairs of equal angles with no correct reasons given (angles must be within the appropriate triangles) |
| | | | C1 | for identifying a second pair of equal angles with a correct reason, e.g. (angle) <i>AEB</i> = (angle) <i>DEC</i> ; <u>opposite angles or vertically opposite angles are equal</u> or for identifying the three pairs of equal angles with no correct reasons given |
| | | | C1 | for stating the three pairs of equal angles of the two triangles e.g. $ABE = DCE$, $BEA = CED$, $EAB = EDC$ with fully correct reasons |
| ;2 | | 66.5 | B1 | for recognising an angle of 60 at <i>AOB</i> |
| | | 0.600 | P1 P1 P1 A1 | for a process to find the area of the sector, e.g. $\frac{"60"}{360} \times \pi \times 11^2$ (= 63.3 or $\frac{121\pi}{6}$) for a process to find the area of the triangle, e.g. $\frac{1}{2} \times 7^2 \times \sin "60"$ (=21.2 or $\frac{49\sqrt{3}}{4}$) for a process to find the required percentage, eg. $\frac{"63.3."-"21.2."}{"63.3."} \times 100$ for answer in the range 66.5 to 66.6 |
| ; 3 | | 8600 | P1 | for process to find the length of the rectangle, e.g. 24×4 (= 96) |
| | | | P1 | for process to find the perpendicular height of an equilateral triangle of side (24×2) cm e.g. $48 \sin 60 (= 41.5(69.))$ or $\sqrt{48^2 - 24^2} (= 24\sqrt{3} \cos 2)$ |
| | | | P1 | for complete process to find the width of rectangle, e_{α} "41 5(69)" + 24 + 24 (= 89 5(69)) |
| | | | A1 | for answer in the range 8592 to 8602 |



| Question | Working | Answer | | Notes |
|----------|---------|--------|----|--|
| ;2 | | 20.9 | M1 | correct recall of appropriate formula eg sin $x = \frac{5}{14}$ |
| | | | A1 | for 20.9(248) |
| ; 5 | | 9.54 | P1 | $10^2 - 5^2 (=75)$ |
| | | | P1 | "75" + 4 ² (=91) |
| | | | P1 | $\sqrt{(10^2 - 5^2 + 4^2)}$ |
| | | | A1 | 9.53 - 9.54 |
| 96 | | 203 | P1 | translate into algebra for rectangle: $4x+4x+3x+4+3x+4$ (=14 <i>x</i> +8) or for trapezium: $5x+5x+x-3+7x-3$ (=18 <i>x</i> -6) |
| | | | P1 | equating: eg 18x-6=14x+8 (4x=14) |
| | | | A1 | solving for <i>x</i> : $x=14/4 = 3.5$ oe |
| | | | P1 | process to find area: " 3.5 " × $3+4$ (ft) or " 3.5 " × 4 ft |
| | | | A1 | cao |



| Question | Working | Answer | Notes |
|----------|---------|--------|---|
| ;7 | | 29° | C1 angle $OTP = 90^\circ$, quoted or shown on the diagram |
| | | | M1 method that leads to $180 - (90 + 32)$ or 58 shown at <i>TOP</i> OR that leads to 122 shown at <i>SOT</i> |
| | | | M1 complete method leading to "58"÷2 or $(180 - "122") \div 2$ or 29 shown at <i>TSP</i> |
| | | | C1 for angle of 29° clearly indicated and appropriate reasons linked to method eg angle between <u>radius</u> and <u>tangent</u> = 90° and sum of <u>angles</u> in a <u>triangle</u> = 180° ; <u>ext angle</u> of a triangle <u>equal</u> to sum of <u>int opp</u> <u>angles</u> and base <u>angles</u> of an <u>isos</u> triangle are <u>equal</u> or <u>angle</u> at <u>centre</u> = $2x$ <u>angle</u> at <u>circumference</u> or <u>ext angle</u> of a triangle <u>equal</u> to sum of <u>int opp</u> <u>angles</u> |
| ; 8 | | 4.89 | $\frac{M1}{360} \times 2 \times \pi \times 7 \text{ oe}$ |
| | | | A1 4.8 – 4.9 |



| Question | Working | Answer | Notes |
|----------|---------|--------|---|
| ;9 (a) | | 130 | P1 start to process eg draw a labelled triangle or use of sine rule $\frac{\sin Q}{8.7} = \frac{\sin 32}{5.2}$ |
| | | | P1 process to find of Q eg Q = $\sin^{-1}\left[\frac{\sin 32}{5.2} \times 8.7\right]$ |
| | | | P1 process to find area of triangle <i>PRQ</i> . |
| | | | A1 22.5 – 22.6 |
| (b) | | | C1 angle PRQ is obtuse so need to find area of two triangles. |
| ;: | | 1361 | P1 process using similar triangles to find base of small cone eg. 4 cm used as diameter or 2 cm used as radius |
| | | | P1 process to find volume of one cone |
| | | | P1complete process to find volume of frustumP1complete process to find mass or 1360 - 1362 |
| | | | A1 1361 or 1360 or 1400 |



| Question | Working | Answer | Notes |
|----------|--|--------------|---|
| 99 | | 66.9 | P1for process to find the area of one shape, eg. 19×16 (= 304) or $\pi \times 8^2$ (= 201.06)P1for process to find the shaded area, eg. "304" - "201.06" $\div 2$ (= 203.46)P1for a complete process to find required percentage, eg. $\frac{"203.46"}{304} \times 100$ A1for answer in range 66 to 68 |
| 100 | | 135 | B1 for identifying the angle of 70° (on the diagram), showing understanding of notation P1 for process to find an angle in triangle <i>ABC</i>, eg. for process to find angle <i>BAC</i>, eg. (180 - 50) ÷ 2 (= 65°) A1 for 135 |
| 101 | angle BAD = angle DCA = 22.62° angle DBA = angle DAC = 67.38° | 33.8 | P1for recognition of similar triangles or equal ratio of sides OR for a method to find angle <i>BAD</i> or angle <i>DBA</i> and state that this is the same as angle <i>DCA</i> or angle <i>DAC</i> P1for process to find <i>CB</i> , eg. $\frac{5}{13} = \frac{13}{CB}$ A1for an answer rounding to 33.8 |
| 102 | | 8.63 to 8.65 | P1 for a start of process, eg. 0.5x(x - 2) = 2.5 P1 for rearranging to give a quadratic equation, eg x² - 2x - 5 (= 0) oe. P1 (dep on P1) for a process to solve their 3-term quadratic equation, condoning one sign error in use of formula (x = 3.449 and x = -1.449) P1 for selecting the positive value of x and applying Pythagoras to find the hypotenuse, eg.√ ("3.449"² + "1.449"²) (= 3.74) P1 (dep on previous P1) for complete process to find perimeter A1 for answer in the range 8.63 to 8.65 |



| Question | Working | Answer | Notes |
|----------|---------|--------|--|
| 103 | | Proof | C1 for joining <i>AO</i> (extended to <i>D</i>) and considering angles in two triangles (algebraic notation may be used here) |
| | | | C1 for using isosceles triangle properties to find angle <i>BOD</i> (eg. $x + x = 2x$) or angle <i>COD</i> (eg. $y + y = 2y$) |
| | | | C1 for angle $BOC = 2x + 2y$ [= 2×angle $BAO + 2$ ×angle CAO] |
| | | | C1 for completion of proof with all relevant reasons given, eg. base <u>angles</u> of <u>isosceles</u> triangle are <u>equal</u> and sum of <u>angles</u> at a <u>point</u> is 360° |



| Question | Working | Answer | | Notes |
|----------|--|---|----|---|
| 326 | | Translation $by \begin{pmatrix} 4\\ -3 \end{pmatrix}$ | B1 | for translation |
| | | | B1 | $\begin{pmatrix} 4\\ -3 \end{pmatrix}$ |
| 327 | | 105 | P1 | for process to find the exterior angle or interior angle of a hexagon or octagon |
| | | | P1 | for process to find the both exterior angles or both interior angles |
| | | | A1 | for 105 from correct working |
| 328 | $\frac{1}{4} \times \pi \times 4.8^2$ | 6.58 | B1 | for use of formula for area of a circle |
| | $\frac{1}{2} \times 4.8 \times 4.8$ | | P1 | for complete process to find area of shaded region |
| | $\frac{1}{4} \times \pi \times 4.8^2 - \frac{1}{2} \times 4.8 \times 4.8$ | | A1 | for 6.56 – 6.58 |
| 329 | $\sim TSU = 360 \div 5 (=72)$ Exterior angles of a polygon | proof | M1 | for method to find interior or exterior angle of regular pentagon |
| | and up to 360 $\geq QRO = \geq OTP = 90$ The tangent to a circle is perpendicular (90°) to the radius (diameter) | | M1 | for using angle between tangent and radius |
| | $\sim ROT = 540 - 2 \times 90 - 2 \times 108 (= 144)$ | | M1 | for method to find angle <i>ROT</i> |
| | $\sim RUT = 144 \div 2 (= 72)$ The angle at the centre of a circle is twice the angle at | | C1 | for method to find angle <i>RUT</i> with reason |
| | the circumference Base angles of an isosceles triangle are equal | | C1 | for deduction that $ST = UT$ with reasons |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|---|
| 32: | 18.3 | P1 | for finding the area of the triangle eg $0.5 \times 8 \times 8$ (= 32) | Accept rounded or truncated figures |
| | | P1 | for finding the area of the circle $\pi \times 8 \times 8$ (= 201.06) | |
| | | P1 | for finding the area of the sector | |
| | | | eg $\frac{1}{4} \times \pi \times 8^2$ or "201.06" ÷ 4 (= 50.26) | |
| | | A1 | for an answer in the range 18.2 to 18.3 | If the answer is given within the range but then rounded incorrectly award full marks. |
| 10; | 14.14 | P1 | works out scale factor eg $(9 + 6) \div 6 (= 2.5)$ | Note method can be carried out in either order |
| | | | OR | |
| | | | for start of process to find angle <i>DBE</i> eg sin $B = \frac{1}{6}$ oe | |
| | | P1 | uses Pythagoras eg $6^2 - 2^2$ (= 32) or $\sqrt{32}$ (= 5.6) OR | |
| | | | calculates $AC \ge 2 \times (2.5) = 5$ | May be seen on diagram |
| | | | for complete process to find angle <i>DBE</i> eg $\sin^{-1}\left(\frac{2}{6}\right)$ (= 19.4) | |
| | | P1 | complete process to find <i>CB</i> eg "2.5" × " $\sqrt{32}$ " (= 10 $\sqrt{2}$) | |
| | | | or $\sqrt{(9+6)^2 - 5''^2}$ (= 10\(\frac{1}{2}) | |
| | | | OR | |
| | | | uses trigonometry, eg $15 \times \cos $ "19.4" | |
| | | A1 | 14.1 to 14.15 | If the answer is given within the range but then |
| | | | | rounded incorrectly award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------------------|----------|---|---------------------|
| 332 | $\frac{2}{5}a + b$ | P1 P1 | for relationship involving D eg $\overrightarrow{OD} = \frac{2}{5} \overrightarrow{OB}$ or $\overrightarrow{DB} = \frac{3}{5} \overrightarrow{OB}$ or for relationship involving E eg $\overrightarrow{BE} = \frac{1}{5} \overrightarrow{BC}$ or $\overrightarrow{EC} = \frac{4}{5} \overrightarrow{BC}$ for relationship involving D in terms of \mathbf{a} and \mathbf{b} eg $\overrightarrow{OD} = \frac{2}{5} (\mathbf{a} + \mathbf{b})$ or $\overrightarrow{DB} = \frac{3}{5} (\mathbf{a} + \mathbf{b})$ or for relationship involving E in terms of \mathbf{a} and \mathbf{b} | Additional guidance |
| | | P1 A1 | eg $\overrightarrow{BE} = \frac{1}{5} (-\mathbf{b} - \mathbf{a} + 3\mathbf{b})$ oe or $\overrightarrow{EC} = \frac{4}{5} (-\mathbf{b} - \mathbf{a} + 3\mathbf{b})$ oe or $\overrightarrow{BC} = 2\mathbf{b} - \mathbf{a}$ oe or $\overrightarrow{CB} = \mathbf{a} - 2\mathbf{b}$ oe (dep P2) for expression for \overrightarrow{DE} in terms of \mathbf{a} and \mathbf{b} eg $\overrightarrow{DE} = \frac{3}{5} (\mathbf{a} + \mathbf{b}) + \frac{1}{5} (-\mathbf{b} - \mathbf{a} + 3\mathbf{b})$ for $\frac{2}{5}\mathbf{a} + (1)\mathbf{b}$ or $\frac{1}{5} (2\mathbf{a} + 5\mathbf{b})$ | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|----------------------|----------|---|---|
| 333 | Proof (supported) | M1 | for using the sine rule on triangle <i>ABD</i> or on triangle <i>ADC</i> , to involve sides <i>AB</i> , <i>BD</i> , <i>AC</i> , or <i>DC</i> $eg \frac{AB}{sinADB} = \frac{BD}{sin x}$ oe or $\frac{AC}{sinADC} = \frac{DC}{sin x}$ oe OR for an expression for the area of triangle <i>ABD</i> or for the area of triangle <i>ADC</i> $eg \frac{1}{2}AB AD sin x$ or $\frac{1}{2}AD AC sin x$ or $\frac{1}{2}h BD$ or $\frac{1}{2}h DC$ | Accept extra letters eg y shown on diagram for any angle used |
| | | M1 | for using the sine rule on both triangle <i>ABD</i> and on triangle <i>ADC</i> , to involve sides <i>AB</i> , <i>BD</i> , <i>AC</i> , or <i>DC</i> eg $\frac{AB}{\sin ADB} = \frac{BD}{\sin x}$ oe and $\frac{AC}{\sin ADC} = \frac{DC}{\sin x}$ oe OR for two expressions for the area of either triangle <i>ABD</i> or for triangle <i>ADC</i> eg $\frac{1}{2}ABAD \sin x$ and $\frac{1}{2}hBD$ or $\frac{1}{2}ADAC \sin x$ and $\frac{1}{2}hDC$ | |
| | | M1 C1 | for stating or showing sin $ADB = \sin ADC$, eg sin $y = \sin (180 - y)$ OR for using two expressions to form an equation eg $\frac{\frac{1}{2}AB AD \sin x}{\frac{1}{2}AD AC \sin x} = \frac{\frac{1}{2}h BD}{\frac{1}{2}h DC}$ oe for a full method to arrive at the given answer | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|---|--|
| 334 | 2820 | P1 | for start to process to find height of triangle, | |
| | | | $eg \tan(40) = \frac{h}{2}$ oe | |
| | | | 5 | |
| | | | or equivalent process to find the height of the triangle 10×10^{-10} | |
| | | | or start to process to find slant height, eg $\frac{1}{\sin 100} = \frac{1}{\sin 40}$ | |
| | | | | |
| | | P1 | for complete process to find height of triangle, eg 5tan 40 (= 4.19) | Accept 4.2 |
| | | | or complete process to find the slant height, eg $\frac{10}{\sin 100} \times \sin 40$ (= 6.5) | |
| | | | SIII100 | |
| | | D1 | Constant a Constant to Constant a Constant | |
| | | PI | $eg 10 \times 20 \times 12 (= 2400) \text{ or } 0.5 \times 10 \times 4.19 \text{ "} \times 20 (= 419)$ | $10 \times 20 \times 12$ may be seen as part of a calculation to find the volume of the prism |
| | | | or $\frac{1}{2} \times 10 \times 6.52 \times 10^{-12} \times 10^$ | |
| | | | or process to find total area of cross section. | |
| | | | eg $0.5 \times 10 \times "4.19" + 10 \times 12 (= 140.9)$ | |
| | | | or $\frac{1}{2}$ × "6.52" × "6.52" × sin 100 + 10 × 12 (= 140.9) | |
| | | | | |
| | | D1 | for complete process to find total volume | |
| | | I I | eg $(0.5 \times 10 \times "4.19" + 10 \times 12) \times 20$ | |
| | | | | |
| | | Δ 1 | for an answer in the range 2810 to 2820 | If an answer is given in the range in working and |
| | | AI | for an answer in the range 2810 to 2820 | then rounded incorrectly award full marks. |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------------------------------|----------------|---|--|
| 115'(a) | rotation of 180° about (2.5, -1) | M1 | for method to find position of \mathbf{Q} , eg shape drawn at $(-1, -2)$, $(-1, -5)$ and $(-2, -5)$ or for method to find position of \mathbf{R} , eg shape drawn at $(4, -4)$, $(4, -7)$ and $(3, -7)$ or for method to translate their \mathbf{Q} correctly | The method mark is awarded if no working is shown but at least 2 of the 3 aspects are correct in the description |
| | | A2 (A1 | for rotation of 180° about $(2.5, -1)$ or enlargement by scale factor -1 , centre $(2.5, -1)$ for any 2 of the 3 aspects) | Cannot award A marks for a combination of transformations With no extra incorrect aspects |
| (b) | (2.5, -1) | B1 | for $(2.5, -1)$ ft from rotation or enlargement in (a) | No follow through from a combined transformation in part (a) |
| 134 | 60 (supported) | M1 M1 A1 | for angle <i>DBF</i> , eg $180 - 100 (= 80)$ for angle <i>BFD</i> , eg $180 - "80" - 40 (= 60)$ or for angle <i>CBF</i> = 40 for angle <i>ABD</i> = 60 | Angles may be shown on the diagram or in working |
| | | C1 | (dep M2) for at least 2 reasons from Opposite angles of a cyclic quadrilateral add up to 180 Angles in a triangle add up to 180 Alternate segment theorem OR Opposite angles of a cyclic quadrilateral add up to 180 <u>Alternate segment</u> theorem Angles on a straight line add up to 180 | Underlined words need to be shown; reasons need to be linked to their method |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 337 | Proof | P1 | for start to process to find area of ABCDEF, | Any correct process to find the area of part of the |
| | | | eg area of equilateral triangle = $\frac{1}{2} \times x \times x \times \sin 60$ (= $\frac{\sqrt{3}}{r^2}$) | hexagon is acceptable for this mark, |
| | | | $\frac{1}{2}$ | eg $\frac{1}{2} \times x \times x \times \sin 120$ |
| | | | OR | 2 |
| | | | for start to process to find area of $FGHJK$, | or $\frac{1}{2} \times (x+2x) \times \frac{\sqrt{3}}{2}x$ |
| | | | eg area of equilateral triangle = $\frac{1}{2} \times px \times px \times \sin 60 \ (= \frac{\sqrt{3}}{4} p^2 x^2)$ | 2 2 |
| | | | | Allow sin 60 left in expressions for the first 3 |
| | | D1 | | marks. |
| | | PI | for complete process of finding area of <i>ABCDEF</i> , | |
| | | | eg $6 \times \frac{1}{2} \times x \times x \times \sin 60$ or $6 \times \frac{1}{2} \times x \times x \times \frac{\sqrt{3}}{2} = \left(= \frac{3\sqrt{3}}{2} x^2 \right)$ oe | |
| | | | OR | |
| | | | for complete process of finding area of <i>FGHIJK</i> , | |
| | | | eg $6 \times \frac{1}{2} \times px \times px \times \frac{\sqrt{3}}{2} \left(=\frac{3\sqrt{3}}{2}p^2x^2\right)$ oe | |
| | | P1 | for process of finding area of <i>ABCDEF</i> | |
| | | | $eg \frac{3\sqrt{3}}{2}x^2$ oe | |
| | | | AND | |
| | | | for process of finding area of FGHIJK, | |
| | | | eg $p^2 \times \frac{3\sqrt{3}}{2} x^2$ oe | |
| | | C1 | correct algebra leading to given result, $\frac{3\sqrt{3}}{2}(p^2-1)x^2$ | Accept $\frac{3\sqrt{3}}{2}x^2(p^2-1)$ as final result. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------|------|---|--|
| 338 | 45 | P1 | for $180 - 117$ (=63) | Angles may be shown on the diagram. |
| | | | or states, or uses, exterior angle + $x = 117$ | Any angle labelled correctly as 63 and not contradicted scores this mark |
| | | P1 | for process to find the exterior or the interior angle of the pentagon, eg $360 \div 5(=72)$ or $180 - (360 \div 5) (=108)$ or $((5-2) \times 180) \div 5$ (=108) | Exterior = 108 or interior =72 does not score the mark |
| | | P1 | for a complete process to find <i>x</i> , eg 180 – "72" – "63" or "108" – "63" or 117 – "72" | |
| | | A1 | cao | An answer of 45 with no supporting working scores 0 |
| 339 | Enlargement | B2 | vertices at (2.5, 1) (2.5, 6) (5, 6) | |
| | | (B1 | for triangle of the correct size and orientation in the wrong position | |
| | | | or a correct enlargement of a different scale factor centre (0, 1) | |
| | | | or correct orientation with 2 of 3 vertices correct) | |
| 318 | 1.95 | P1 | for correct substitution into the cosine rule, eg $3.4^2 = 6.1^2 + 6.2^2 - 2 \times 6.1 \times 6.2 \times \cos BCA$ | Can be any angle within triangle <i>ABC</i> |
| | | P1 | for a full process to find <i>BCA</i> eg (cos <i>BCA</i> =) $\frac{6.1^2 + 6.2^2 - 3.4^2}{2 \times 6.1 \times 6.2}$ or (<i>BCA</i> =) 32(.08046913) | P2 can be awarded for $BCA = 32(.08046913)$ |
| | | P1 | correct substitution into the sine rule, $eg \frac{DC}{\sin("32.08" \times \frac{2}{5})} = \frac{6.2}{\sin(180 - "32.08" - ("32.08" \times \frac{2}{5})}$ | |
| | | P1 | for complete process to find <i>DC</i> eg (<i>DC</i> =) $\frac{6.2 \times \sin^{"} 12.832"}{\sin^{"} 135.088"}$ | |
| | | A1 | Answer in the range 1.94 to 1.951 | Must not come from incorrect processing |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 33; | 264 | P1 | correct substitution into the volume formula, eg $56.8 = \frac{1}{3} \times \pi \times r^2 \times 3.6$ | |
| | | P1 | completes process to find base radius or the value of r^2 , eg $r =$ | |
| | | | $\sqrt{\frac{56.8 \times 3}{\pi \times 3.6}}$ (=3.88158) or r ² = $\frac{56.8}{1.2\pi}$ (=15.066) | |
| | | P1 | Uses Pythagoras to find the sloping length, eg $\sqrt{"3.88 \dots "^2 + 3.6^2}$ (=5.29) | |
| | | P1 | process to find an equation in <i>AOB</i> , eg $\pi \times "3.88" \times "5.29" = \frac{AOB}{360} \times \pi$ $\times "5.29"^2$ | <i>AOB</i> does not need to be the subject of the equation |
| | | | or $\frac{AOB}{360} \times \pi \times 2 \times "5.29" = 2 \times \pi \times "3.88"$ or $\frac{AOB}{360} \times "5.29" = "3.88"$ | |
| | | A1 | answer in the range 263.9 to 264.1 | |
| 342 | 4:3 | P1 | Process to find a missing vector using the given ratios as fractions, eg. $\frac{1}{3}$ of \overrightarrow{OX} ($=\frac{1}{3}$ a) or. $\frac{1}{4}$ of \overrightarrow{OY} ($=\frac{1}{4}$ b) | |
| | | P1 | for a process to use $\overrightarrow{ZO} = \overrightarrow{YX} = \mathbf{a} - \mathbf{b}$ oe | Might be embedded in their answer for ZP |
| | | P1 | for a process to find either \overrightarrow{ZP} or \overrightarrow{ZR} in terms of a and b , eg. either $\overrightarrow{ZP} = \mathbf{a} - \mathbf{b} + \frac{1}{3}\mathbf{a}$ or $\overrightarrow{ZR} = \mathbf{a} - \mathbf{b} + \frac{1}{4}\mathbf{b}$ | The award of this mark implies the first two process marks. |
| | | P1 | for a process to write \overrightarrow{ZP} and \overrightarrow{ZR} as multiples of the same vector, eg. multiplying both by 12 to get the ratio, $\frac{4}{3}(\mathbf{a} - 0.75\mathbf{b})$ and $\mathbf{a} - 0.75\mathbf{b}$ respectively | |
| | | A1 | oe | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------|------|---|--|
| 343 | 162 | M1 | for method to find sum of the interior angles of a hexagon | Must be a complete process that would lead to a |
| | supported | | $eg (6-2) \times 180 (= 720)$ oe | figure of 720 if evaluated correctly. |
| | | | OR | |
| | | | for method to find sum of the interior angles of a pentagon, | For a pentagon there must be an indication that |
| | | | $eg (5-2) \times 180 (= 540)$ OR | they have divided the nexagon into two halves. |
| | | | for method to find angle AFC or BCF, eg $(360 - 2 \times 117) \div 2 (= 63)$ OR | 63 may be shown on the diagram for angle <i>AFC</i> or angle <i>BCF</i> |
| | | | for dropping a perpendicular from A or B to ED with 90° marked on ED and 27° at the top | |
| | | M1 | for method to use ratio 2 : 1 | Ratio must be used correctly if awarded for |
| | | | eg marks as $2x$ and x or as x and $\frac{1}{2}x$ on diagram | diagram |
| | | | OR for ([angle sum of hexagon] -2×117) $\div 6$ (= 81) oe or ([angle sum of hexagon] $\div 2 - 117$) $\div 3$ (= 81) oe or $117 + 117 + 2x + 2x + x + x =$ [angle sum of hexagon] oe OR eg ([angle sum of pentagon] $-117 - 180$) $\div 3$ (= 81) oe | Award provided [angle sum of hexagon] is greater than 700 or [angle sum of pentagon] is greater than 500 Algebraic route needs to show both sides of the equation. LHS of equation may be simplified. |
| | | | or $117 + 180 + 2x + x = $ [angle sum of pentagon] oe | |
| | | M1 | for finding angle $FED = 81$ or for finding angle $CDE = 81$ OR for complete process to find angle AFE eg ([angle sum of hexagon] -2×117) $\div 6 \times 2$ oe OR ([angle sum of pentagon] $-117 - 180$) $\div 3 \times 2$ oe | This may be shown by solving a correct equation to find the value of <i>x</i> . |
| | | C1 | for accurate working leading to angle $AFE = 162$ | Award marks for 162 on the diagram with working and not contradicted by the answer line. Award 0 marks for 162 without working. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------------|------|--|---|
| 344 | No Supported | P1 | for finding the area of a circle eg $\pi \times 0.8^2$ (= 2.01) | Must be area of circle and not part of a volume, eg $\pi r^2 h$ May be seen as $2\pi r^2$ |
| | | P1 | for finding the curved surface area eg $2\pi \times 0.8 \times 1.8$ (= 9.047) | May be seen from $2\pi rh$ or from πdh |
| | | P1 | for use of the coverage information with an area eg "2.01" \div 5 (= 0.402) or "4.02" \div 5 (= 0.804) or "9.047" \div 5 (= 1.8095) or "11.058" \div 5 (= 2.2116) or "13.069" \div 5 (= 2.6138) OR for precess to find total coverage for comparison | Accept numbers without working written to no less than 2dp Do not award if a volume has been used as part of the calculation. |
| | | | eg 5 \times 7 (= 35) | An independent mark for 5 ×7 |
| | | Ρ1 | (dep P1) for finding total surface area for 3 tanks eg [total surface area] × 3 (= 39.2) OR for complete process to find the number of tins needed for total area of 3 tanks eg "13.069"× 3 ÷ 5 (= 7.84) OR for complete process to find coverage needed from each tin eg "13.069"× 3 ÷ 7 (= 5.6) | [total surface area] must come from the addition of two attempts at area, but not from volume. |
| | | C1 | for conclusion "No" supported by accurate figures eg 8 tins or 7.84 (> 7) or 39.2 > 35 or 5.6 (>5) | Clear statement that there is not enough paint supported by correct figures for comparison. NB: $2.6 \times 3 = 9$ tins needed is inaccurate 8 or 7.84 tins is sufficient without restating the 7, 5.6 m ² is sufficient without restating the 5 but 39.2 and 35 are needed for comparison. A statement of "No, 8 tins" alone gets 0 marks without supporting working. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|--|
| 345 | 36 | P1 | for process to find an expression for the area of triangle | Accept any correct expression, |
| | | | $\operatorname{eg} \frac{1}{2} \times 24 \times AE \times \sin 30 \ (= 6AE)$ | $eg \frac{1}{2} \times 24 \times y \times \sin 30$ |
| | | P1 | (dep P1) for process to link the area of rectangle with the area of the | |
| | | | triangle eg $2 \times \frac{1}{2} \times 24 \times AE \times \sin 30 (= 12AE)$ | |
| | | | or for $AB = 12^2$ | |
| | | P1 | (indep) for use of given ratio eg $AE = 3AB$ oe, | May be shown on the diagram by labelling AE |
| | | | eg area of rectangle = $AE \times AB = 3x \times x$ | and AB with, for example, $3x$, x or x, $\frac{1}{3}x$ or $\frac{3}{4}x$, $\frac{1}{4}x$ |
| | | | | Do not accept 3, 1 or 1, $\frac{1}{3}$ or $\frac{3}{4}$, $\frac{1}{4}$ for this mark. |
| | | A1 | cao | |
| | | | | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|-----------------------------|--------|------|--|--|
| 346 | 098.6 | P1 | for using bearings to determine ABC as 67° | Accept 67 written on the diagram. |
| | | P1 | for using the cosine rule to find AC eg $(AC^2 =)$ 9 ² + 8 ² - 2 × 9 × 8 × cos[67] oe or AC = 9.4199 | Accept correct substitution into RHS of equation Accept AC in the range 9.41 to 9.42 |
| | | P1 | (dep P1) for using the sine rule to find angle <i>BAC</i> eg $\frac{9}{\sin BAC} = \frac{"9.42"}{\sin [67]}$ oe | |
| | | | OR | |
| | | P1 | for using the cosine rule to find angle <i>BAC</i> eg $9^2 = "9.42^2" + 8^2 - 2 \times "9.42" \times 8 \times \cos BAC$ oe for rearranging | Accept any equivalent form with values substituted |
| eg sin B. OR eg cos B | | | eg sin $BAC = 9 \times \frac{1}{"9.42"}$ oe OR eg cos $BAC = (``9.42^{2"} + 8^{2} - 9^{2}) \div (2 \times ``9.42" \times 8)$ oe | |
| | | A1 | OR for angle $BAC = 61.57$ for angle in the range 98.5 to 98.6 | If the correct answer is given without supportive evidence award 0 marks. Condone missing "0" at the front. If an answer within the range is seen in working and rounded incorrectly award full marks. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|--|
| 347 | 17.3 | P1 | for full process to find either angle eg $(180 - 90) \div (2+3) \times 2 (=36)$ or for 36 or 54 seen as an angle | May be seen on diagram Condone correct values if incorrectly placed. |
| | | P1 | for a correct equation using trigonometry eg cos $[A] = 14 \div AB$ | This must be shown as an equation with all four elements (eg cos, [<i>A</i>], 14, <i>AB</i>) present. [<i>A</i>] could be 36 or any angle clearly and unambiguously identified as <i>A</i> . This also applies to [<i>B</i>] with Sine. |
| | | P1 | (dep previous P mark) for rearranging their trigonometry equation to make <i>AB</i> the subject eg (<i>AB</i> =) "14 \div cos 36" | |
| | | A1 | for an answer in the range 17.3 to 17.4 | If an answer is shown in the range in working and then incorrectly rounded award full marks. |
| | | | | |
| | | | | |
| 128 | 73.6 | P1 | for correct initial use of Pythagoras eg 5 ² + 5 ² (=50) or a trigonometric ratio in the form $\frac{5 \div 2}{0.5AC} = \sin 45$ oe | |
| | | P1 | for finding the length of half of the diagonal eg $\sqrt{50"} \div 2 (= 3.5)$ or $0.5AC = \frac{5 \div 2}{\sin 45} (= 3.5)$ oe | do not accept $\sqrt{20} \div 2$ |
| | | P1 | for process to use tan eg tan $TAC = (12 \div ``3.5'') (=3.3)$ or complete alternative method arriving at an equation with the subject as sin <i>TAC</i> or cos <i>TAC</i> | |
| | | A1 | for an answer in the range 73.58 to 74.1 | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-----------|------|---|--|
| 349 | 39.9 | P1 | for finding the length of the minor or major arc $eg \frac{220}{360}\pi \times 12 \ (= 23(.03834))$ | Allow appropriate rounding if calculation seen in parts |
| | | P1 | for substituting into the sine or cosine rule to find <i>OD</i> eg $14 \div \sin 140 = OD \div \sin 24$ or $(OD^2=) 6^2 + 14^2 - 2 \times 6 \times 14 \times \cos 24$ (=78.5) | Must involve <i>OD</i> in the relationship but may be implied |
| | | P1 | for a complete process to find the length <i>OD</i> eg $14 \div \sin 140 \times \sin 24$ (=8.8(58778)) | |
| | | P1 | for a complete process to find the perimeter eg "23(.03834)" + 14+ "8.8(58778)" - 6 | May be seen in multiple calculations |
| | | A1 | for an answer in the range 39.8 to 40 | If an answer in the range is seen in working and then incorrectly rounded award full marks. |
| 34. | (-351) | M1 | for a complete method to show the transformations | Image at (-41) (-31) and $(-35-2)$ |
| 57. | (0.0, 1) | A1 | cao | |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------------------|------|--|--|
| 34; | Triangle of area 18 | M1 | for a complete method to find area of trapezium eg $\frac{1}{2}(2+7) \times 4$ (= 18) OR for a triangle drawn of area 36 OR for a triangle that would give an area ft their area of trapezium | The value for the area of the trapezium must be clear for the ft to be checked. |
| | | A1 | for a triangle drawn of area 18 eg base = 6, height = 6 or base = 9, height = 4 | Accept use of dimensions that are not whole numbers as long as the intention is clear |
| 352 (a) | 50.5 | M1 | for $\cos ABC = \frac{7}{11} (0.63)$ oe | Must be a complete statement for cos, sin or tan with all three elements present. |
| | | A1 | for answer in the range 50.4 to 50.51 | If an answer is in the range 50.4 to 50.51 is given in the working space then incorrectly rounded, award full marks. |
| (b) | Increase (supported) | C1 | States increase with supporting reason eg " $\frac{7}{10}$ is greater than $\frac{7}{11}$ " "0.636 is less than 0.7" "cos increases as angle decreases" "decreasing the denominator increases the value of the fraction" "angle is now 45.6" (accept 45.5 – 45.6) | If figures are given they must be correct (truncated or rounded). |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|--------|------|--|---|
| 353 | 140 | P1 | for complete process to find sum of the interior angles of a pentagon eg $(5-2) \times 180$ or exterior $360 \div 5 = 72$, interior $180 - 72 = 108$, 108×5 OR for complete process to find sum of the exterior angles of the pentagon eg $(180 - x) + (180 - 2x) + (180 - 125) + (180 - 115) + (180 - 90)$ | Must be a complete process that could lead to a figure of 540 if that process is evaluated incorrectly |
| | | A1 | for sum of interior angles is 540 OR for sum of exterior angles is 360 | 360 must be identified as the sum of the exterior angles |
| | | P1 | for start to process to find angle <i>ABC</i> eg [angles in a pentagon] $-115 - 125 - 90$ (= 210) or $115 + 125 + 90 + x + 2x$ = [angles in a pentagon] OR (180 - x) + (180 - 2x) + (180 - 125) + (180 - 115) + (180 - 90) = 360 | Award provided [angles in a pentagon] is greater than 400 Algebraic route needs to show both sides of the equation. LHS of equation may be simplified |
| | | P1 | for process to find angle <i>ABC</i> eg "210" \div 3 (= 70), "210" divided in the ratio 2 : 1 or for process to find angle <i>BCD</i> eg $\frac{2}{3} \times$ "210" or for $3x =$ "210" or $-3x = -$ "210" | Award if 70 is given for either <i>ABC</i> or <i>BCD</i> on the diagram |
| | | A1 | сао | Award marks for 140 on the diagram with working and not contradicted by the answer line. Award 0 marks for 140 without working. |



| Question | Answer | Mark | Mark scheme | Additional guidance |
|----------|-------------|------|---|---|
| 354 | 13.1 | P1 | for start of process to find the length of <i>BD</i> , $eg \frac{BD}{\sin 34^{\circ}} = \frac{12.5}{\sin 109^{\circ}}$ | |
| | | P1 | for complete process to find the length of <i>BD</i> , eg $BD = \frac{12.5}{\sin 109^{\circ}} \times \sin 34^{\circ} (= 7.39)$ | Accept 7.4 for the award of the first two P marks |
| | | P1 | for process to find the length of AD , eg $AD^2 = 11.4^2 + \text{``} 7.39^2 \text{''} - 2 \times 11.4 \times \text{``} 7.39^{\text{''}} \times \cos 86^\circ$ | |
| | | P1 | for process to use correct order of operations, eg $129.96 + 54.6(5) - 11.7(5) (= 172.85)$ | |
| | | A1 | for answer in the range 13.1 to 13.2 | If an answer is given within the range and then incorrectly rounded to 3 sig figs award full marks. |
| 355 (a) | Proof | C1 | for starting the proof, identifying a pair of relevant equal sides or angles with reasons from AD = BC (opposite sides of a parallelogram are equal) angle PAD = angle QCB (opposite angles of a parallelogram are equal) angle ADP = angle CBQ (given or both 90°) | |
| | | C1 | (dep C1) for complete identification of all three equal aspects with reasons | |
| | | C1 | (dep C2) for conclusion of congruency proof | Congruency conclusion must include a reference to ASA |
| (b) | Explanation | C1 | for identifying a pair of equal sides or angles in $APCQ$, with reason, eg $AP = QC$ since triangle ADP is congruent to triangle CBQ | |
| | | C1 | (dep C1) for reasoning that $APCQ$ is a parallelogram so opposite sides of a parallelogram are parallel | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---------------|------|---|
| 356 | | 14.4 | P1 | for start of process, eg $0.5 \times 11 \times CD \times \sin 105 = 56$ |
| | | | P1 | for complete process to find CD, eg (CD =) $\frac{56}{0.5 - 11}$ oe (= 10.54) |
| | | | P1 | for process to find AC, eg (AC ² =) $11^2 + [CD]^2 - 2 \times 11 \times [CD] \times \cos 105$ (AC = 17.09) |
| | | | P1 | for process to find AB, eg $\frac{AB}{AB} = \frac{[AC]}{AB}$ |
| | | | A1 | answer in range 14.3 to 14.4 |
| 357 | | Proof | C1 | draws <i>OC</i> and considers angles in an isosceles triangle (algebraic notation may be used, eg two angles labelled x) |
| | | | C1 | finds sum of angles in triangle <i>ABC</i> , eg $x + x + y + y = 180$, or sum of angles at <i>O</i> , eg $180 - 2x + 180 - 2y$ |
| | | | C1 | complete method leading to $ACB = 90$ |
| | | | C1 | complete proof with all reasons given, eg base angles of an <u>isosceles triangle</u> are equal, <u>angles</u> in a <u>triangle</u> add up to 180°, <u>angles</u> on a straight <u>line</u> add up to 180° |
| 358 | | $\frac{2}{5}$ | P1 | for process to find \overrightarrow{AB} (= b - a) or \overrightarrow{BA} (= a - b) |
| | | | P1 | for process to find $\overrightarrow{MN} (= -\frac{1}{2}\mathbf{b} + \mathbf{a} + 2\mathbf{a})$ or $\overrightarrow{PN} (= -\mathbf{k}(\mathbf{b} - \mathbf{a}) + 2\mathbf{a})$ |
| | | | | or \overrightarrow{MP} (= $-\frac{1}{2}\mathbf{b} + \mathbf{a} + k(\mathbf{b} - \mathbf{a})$ or $\frac{1}{2}\mathbf{b} + (1 - k)(\mathbf{a} - \mathbf{b})$) |
| | | | P1 | for process to find two of \overrightarrow{MN} , \overrightarrow{PN} and \overrightarrow{MP} |
| | | | P1 | for process to find k, using \overrightarrow{MN} as a multiple of \overrightarrow{PN} or using \overrightarrow{MN} as a multiple of \overrightarrow{MP} or using \overrightarrow{PN} as a multiple of \overrightarrow{MP} |
| | | | A1 | for $\frac{2}{5}$ oe |



| Question | Working | Answer | Mark | N | otes |
|----------|---------|------------------|------|---|--|
| 359 | | Shows polygon is | M1 | for a complete method to find the interior of | or exterior angle of the dodecagon |
| | | a hexagon | | eg $180 - \frac{360}{12}$, $\frac{180}{12}(12 - 2)$ oe (= 150), 3 | 360 ÷ 12 (=30) |
| | | | M1 | for a complete method to find the interior a eg at <i>B</i> or <i>C</i> : $360 - (150) - 90 (= 120)$ or $(150) - 90 (= 120)$ | ngle of polygon P "30" + 90 (= 120) or for a complete method |
| | | | | to find the interior or exterior angle of the l | nexagon |
| | | | | eg $180 - \frac{360}{6}$, $\frac{180}{6}(6-2)$ oe (= 120), 36 | $50 \div 6 (= 60)$ |
| | | | A1 | for 30 and 120 or 30 and 60 or 120 and 15 | 0 or 60 and 150 |
| | | | C1 | complete solution, fully supported by accur | rate figures |
| 35: | | 5.86 | M1 | for sin 23 = $\frac{CD}{15}$ | |
| | | | | NB Allow any alternative equivalent metho | od to form an equation in AB |
| | | | Al | 5.8 to 5.9 | |
| 35; | | 5.59 | M1 | For use of $\pi r^2 = 49$, where <i>r</i> is the radius or | r = 3.9(49) or diameter = $7.8(9865)$ |
| | | | M1 | For use of Pythagoras to set up an equation in x^2 e.g. $x^2 + x^2 = (d)^2$ or $x^2 = x^2 + x^2$ | For use of trigonometry to set up an equation in <i>x</i> eg sin $45 = x \div d$ |
| | | | M1 | (dep on M2) Rearrange to ($x^2 = 2 \times "3.949"^2$ | Rearrange to $(x=)$ "7.898" × sin 45 oe |
| | | | A1 | 5.5 to 5.6 | |
| 362 | | 2.63 | P1 | for setting up the expression $\frac{1}{2}(x+3)(2x-1)$ | - 1) sin 45 (may be seen in an equation) |
| | | | P1 | (dep) for expanding the brackets in the exp $\frac{1}{2}$ | ression or for the equation |
| | | | | $\frac{1}{2}(x+3)(2x-1)\sin 45 = 6\sqrt{2}$ oe | |
| | | | P1 | (dep) for the process to set up the equation $ax^2+bx+c = d$ e.g. to $2x^2+5x-27 =$ | and rearrange to the form 0 or $24 = 2x^2 + 5x - 3$ |
| | | | P1 | (dep) for substitution into the quadratic for | mula e.g. $\frac{-5 \pm \sqrt{5^2 - 4 \times 2 \times -27}}{4}$ |
| | | | A1 | for 2.63(10436) | |



| Question | Working | Answer | Mark | Notes |
|----------|---------------|--------|------|---|
| 363 | Note DOC=DOA, | 21.6 | P1 | Recognises that OAD or OCD is 90° or right angle |
| | ADO=CDO | | P1 | for using trigonometry to set up an equation in DOA or ADO |
| | | | | $eg \cos DOA = \frac{5}{9}$ |
| | | | P1 | for using inverse trigonometry to find DOA or ADO |
| | | | | $eg DOA = Cos^{-1} \frac{5}{9} (= 56.25)$ |
| | | | P1 | for a complete process to find arc length ABC or AC |
| | | | | eg $\frac{360-2\times 56.25.7}{360} \times 2 \times \pi \times 5$ (=21.598) or $\frac{2\times 56.25.7}{360} \times 2 \times \pi \times 5$ (=9.8174) |
| | | | A1 | for answer in the range 21.5 to 21.65 |
| | | | | |



| Question | Working | Answer | Notes |
|----------|--|--------|--|
| 364 | | 252 | P1 For start to process eg. radius = 12 ÷ 4 (=3) M1 Method to find area of trapezium or semicircle or circle P1 Process to find area of the shaded region A1 251.7 - 252 |
| 365 | DN = MB (given) $\angle NDC = \angle MBC \text{ (base angles of isosceles triangle)}$ DC = BC (sides of a rhombus are equal) $\therefore \Delta DNC \equiv \Delta BMC \text{ (SAS)}$ | Proof | C1 One correct relevant statement C1 All correct relevant statements C1 Correct conclusion with reasons |
| 366 | $AC^{2} = 20^{2} + 20^{2} = 800$ $AX^{2} = 10^{2} + 10^{2} = 200$ $\sqrt{200} \times \tan 55 = VX (= 20.19)$ $VM^{2} = \sqrt{"20.19"^{2} + 10^{2}} (= 22.54)$ $4 \times \frac{1}{2} \times "22.54" \times 20 + 20^{2}$ | 1300 | Let X be centre of base, M be midpoint of AB P1 process to find AC or AX P1 process to find VX or VA P1 process to find height of sloping face or angle of sloping face. P1 process to find surface area of one triangular face. A1 For 1300 – 1302 |



| Question | Working | Answer | Notes |
|----------|--|--------|---|
| 367 | $\vec{OM} = 3a$ $\vec{AB} = 6b - 6a$ $\vec{MC} = 3a + 2(6b - 6a)$ = 12b - 9a = 3(4b - 3a) $\vec{MN} = kb - 3a$ <i>MNC</i> is a straight line so \vec{MC} is a scalar multiple of \vec{MN} | 4 | P1 For process to start e.g. $\vec{OM} = 3\mathbf{a}$ or $\vec{MA} = 3\mathbf{a}$ P1 For process to find $\vec{AB} (=6\mathbf{b} - 6\mathbf{a})$ P1 For process to find $\vec{MC} (=3\mathbf{a} + 2(6\mathbf{b} - 6\mathbf{a}) \mathbf{and})$ $\vec{MN} (= k\mathbf{b} - 3\mathbf{a})$ P1 For correct process to find k e,g. $3k\mathbf{b} - 9\mathbf{a} = 12\mathbf{b} - 9\mathbf{a}$ A1 |


| Question | Working | Answer | Notes |
|----------|--|-----------|--|
| 146 | 160 tiles 18 packs | 18 | M1 a full method to find the area of the trapezium M1 a full method to calculate both areas in consistent units M1 for the area of the trapezium ÷ area of a tile (with consistent units) M1 (dep on previous M) for complete method to find the number of packs required A1 |
| 147 | $1.5 \times 1.7 - 1.7$ Or $0.5 \times 1.7 = (0.85)$ | 0.664(09) | P1 for finding the difference in height by ratio or multiplier P1 for use of tan ratio P1 (dep) for "0.85" ÷ tan 52 oe A1 0.664 to 0.6641 |
| 148 | | 430 | P1 for appropriate use of Pythagoras P1 for setting up an equation equivalent to $x = 15 - 5 - 7$ or better eg $\sqrt{151}$ P1 for finding the volume using their " $\sqrt{15 - 5 - 7}$ " A1 430 to 430.1 |
| 149 | l = 20x $x = 3$ | 20736 | P1 for a first step to solve the problem eg method to find the slant height of the cone or the volume equals $768\pi x^3$ P1 for setting up an equation for the curved surface area in terms of x eg $2160\pi = \pi \times 12x \times 20x$ P1 for complete method to find the value of x P1 for a method to find the volume or value of V A1 cao |



| Question | Working | Answer | Notes |
|----------|---------|--------------------|--|
| 372 | | plan | C1 a partially correct plan |
| | | | C1 correct plan |
| | | 1.1.1 | |
| 373 | | complete chain | C1 starts chain of reasoning eg finds area of large |
| | | or reasoning | Square and area of triangle of use of Typingoras |
| | | | for $(x + y)^2 - 4 \times (x \times y \div 2)$ oe or $\sqrt{x^2 + y^2} \times$ |
| | | | $\sqrt{x^2 + y^2}$ |
| | | | C1 complete chain of reasoning with correct algebra |
| 374 | | Triangle | M1 for correct shape and the correct orientation in |
| | | (-6, 2), (-6, -1), | the wrong position or two vertices correct. |
| | | (-3, -1) | A1 cao |
| 275 | | 10.2 | M1 2(0 100 |
| 3/5 | | 18.2 | for $\frac{260}{360} \times \pi \times 8$ oe or $\frac{100}{360} \times \pi \times 8$ oe |
| | | | A1 for 18.1 to 18.2 |
| | | | |
| 376 | | 1 | P1 starts process eg $\overrightarrow{AB} = 2\mathbf{b} - 2\mathbf{a}$ |
| | | 4 | |
| | | | P1 process to find \overrightarrow{AP} or \overrightarrow{BP} |
| | | | P1 complete process to find \overrightarrow{OP} |
| | | | A1 1 |
| | | | $\operatorname{tor} - \operatorname{oe} 4$ |
| | | | |



| Question | Working | Answer | Notes |
|----------|---------|--------|---|
| 377 | | 10.4 | P1 starts process by using cosine rule to find <i>CD</i> |
| | | | $eg (CD)^2 = 4.9^2 + 3.8^2 - 2 \times 4.9 \times 3.8 \times \cos 80 (=$ |
| | | | 31.98) |
| | | | P1 uses sine rule to find angle <i>ACD</i> or angle <i>ADC</i> |
| | | | $\sin C \sin 80 \sin D \sin 80$ |
| | | | $eg = \frac{1}{3.8} = \frac{1}{5.655'}$ of $\frac{1}{4.9} = \frac{1}{5.655'}$ |
| | | | P1 uses sine rule to find <i>BC</i> or <i>BD</i> |
| | | | BD '5.655' |
| | | | $eg \frac{1}{\sin 25} = \frac{1}{\sin^2 3.6^2}$ |
| | | | P1 process to find area eg $1/2 absinC$ |
| | | | $\Delta 1$ for 10 4 to 10 43 |
| | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------------------|------|---|
| 378 | | 42 | 3 | M1 for a method to find angle <i>ABD</i> eg <i>ABD</i> = $360 - 130 - 130 - 40$ (= 60) or angle <i>DBC</i> eg <i>DBC</i> = $180 - 2 \times 72$ (= 36) (may be on the diagram) M1 for a complete method eg ($180 - "60" - "36"$) ÷ 2 A1 cao |
| | | | | OR |
| | | | | M1 for a method to find angle <i>ABC</i> eg <i>ABC</i> = $540 - 130 - 40 - 130 - 72 - 72$ (= 96) M1 for a complete method eg (180 - "96") ÷ 2 A1 cao |
| 379 | | 15 200 | 3 | M1 for a method to obtain at least 2 different areas from |
| | | | | $50 \times 80 \ (=4000), \frac{1}{2} \times 40 \times 60 \ (=1200), 60 \times 80 \ (=4800)$ |
| | | | | M1 (dep on M1) for adding at least 4 correct face areas A1 cao |
| 378 (a) | | Transfor mation | 2 | B2 for a triangle with vertices at (-1, 1), (-2, 3) and (-2, 1) (B1 for a triangle in correct orientation or rotated 90° clockwise centre the origin) |
| (b) | | Description | 3 | B1 Enlargement B1 Scale factor 3 (accent × 3) |
| | | | | B1 Scale factor 5 (accept × 5) B1 Centre (1,0) |
| | | | | NB: More than one transformation is B0 |
| 37; | | 270 | 3 | M1 for correct use of formula for volume of a cylinder using exact or (some) approximate figures eg $\pi \times 31^2 \times 97.5$ or $\pi \times 31^2 \times 100$ or using an estimate of π eg $\pi = 3$ in the volume formula |
| | | | | M1 for a complete method to find an estimate for the volume in cm ³ with at least 2 values rounded eg $\pi \times 30^2 \times 100$ (= 270 000) eg $3.1 \times 30^2 \times 100$ eg $3 \times 31^2 \times 100$ |
| | | | | A1 accept answer in the range 270 – 300 from a method using estimates |





12 x



| Working | Answer | Mark | Notes |
|---------|---------|-----------------------------|--|
| | 18 | 4 | M1 for correct initial use of Pythagoras eg $(AB^2 =) 10^2 - 6^2 (= 64)$ or $AB = 8$ |
| | | | M1 (dep M1) for " $\sqrt{64}$ " ÷ 2 (= 4) |
| | | | M1 for method to find area of trapezium eg $\frac{1}{2} \times "4" \times (6 \div 2 + 6)$ |
| | | | A1 cao |
| | | | OR |
| | | | M1 for correct initial use of Pythagoras eg $(AB^2 =)$ 10 ² – 6 ² (= 64) or $AB = 8$ |
| | | | M1 (dep M1) for method to find area of $\triangle ABC$ eg $\frac{1}{2} \times \sqrt[n]{64} \times 6$ (= 24) |
| | | | or area of $\triangle AED$ $\frac{1}{2} \times 6 \div 2 \times ``4"$ (=6) or $24 \times (\frac{1}{2})^2$ (=6) |
| | | | M1 for a complete method to find area of <i>EDBC</i> e.g $\frac{3}{4} \times \frac{2}{24}$ eg 24 eg 24 eg 24 |
| | | | A1 cao |
| | Working | Working Answer 18 | WorkingAnswerMark184 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| *383 | | 155° | 5 | M1 for a method to find angle AOD e.g $90 - 40$ (= 50) |
| | | | | M1 for a complete method to find angle <i>BCD</i> |
| | | | | eg $360 - 50'$ (= 310) and $310' \div 2$ (= 155) |
| | | | | A1 for 155 |
| | | | | C2 for complete reasons for their method |
| | | | | Angle between <u>tangent</u> and <u>radius</u> = 90 |
| | | | | Angle at the <u>centre</u> is <u>twice</u> the <u>angle</u> at the <u>circumference</u> oe |
| | | | | <u>Angle</u> sum of a <u>triangle</u> = <u>180</u> |
| | | | | Sum of <u>angles</u> round a <u>point</u> = $\underline{360}$ |
| | | | | (C1 for at least two reasons, one of which must be a circle theorem) |
| | | | | OR |
| | | | | M1 for a method to find angle AOD eg 90 – 40 (= 50) |
| | | | | M1 for a complete method to find angle <i>BCD</i> eg $50 \div 2$ (= 25) and $180 - 25'$ (= 155) |
| | | | | A1 for 155 |
| | | | | C2 for complete reasons for their method |
| | | | | Angle between <u>tangent</u> and <u>radius</u> = 90 |
| | | | | Angle at the centre is twice the angle at the circumference oe |
| | | | | Opposite angles of a cyclic quadrilateral add up to 180 |
| | | | | <u>Angle</u> sum of a triangle = 180 |
| | | | | (C1 for at least two reasons, one of which must be a circle theorem) |
| | | | | |



| Question Workin | g Answer | Mark | Notes |
|---|--|--------|---|
| QuestionWorkin384 (a)*(b)*(b)Method 1Show that \overrightarrow{AG} isto \overrightarrow{AN} | g Answer 3a + 3b Shown parallel | Mark24 | Notes M1 for $\overrightarrow{AB} = 6\mathbf{b} - 6\mathbf{a}$ oe or $\overrightarrow{BA} = 6\mathbf{a} - 6\mathbf{b}$ oe or $(\overrightarrow{OM}) = \frac{1}{2}(6\mathbf{a} + 6\mathbf{b})$ oe A1 cao M1 for a method to find \overrightarrow{OG} or \overrightarrow{GM} in terms of \mathbf{a} and \mathbf{b} eg $\overrightarrow{OG} = \frac{2}{3}$ " $(3\mathbf{a} + 3\mathbf{b})$ " $(= 2\mathbf{a} + 2\mathbf{b})$ eg $\overrightarrow{GM} = \frac{1}{3}$ " $(3\mathbf{a} + 3\mathbf{b})$ " $(= \mathbf{a} + \mathbf{b})$ M1 for a method to find \overrightarrow{AN} in terms of \mathbf{a} and \mathbf{b} eg $-6\mathbf{a} + 6\mathbf{b} \div 2$ $(= 3\mathbf{b} - 6\mathbf{a})$ M1 for a method to find \overrightarrow{AG} in terms of \mathbf{a} and \mathbf{b} eg $-6\mathbf{a} + "2\mathbf{a} + 2\mathbf{b}$ " $(= 2\mathbf{b} - 4\mathbf{a})$ C1 for correct simplified expressions in terms of \mathbf{a} and \mathbf{b} for \overrightarrow{AG} and \overrightarrow{AN} |
| Method 2 Show that \overrightarrow{AG} is to \overrightarrow{GN} | parallel | | C1 for correct simplified expressions in terms of a and b for \overrightarrow{AG} and \overrightarrow{AN} followed by conclusion OR M1 for a method to find \overrightarrow{OG} in terms of a and b $eg \frac{2}{3}$ "(3 a + 3 b)" (= 2 a + 2 b) M1 for a method to find \overrightarrow{GN} in terms of a and b $eg -$ "(2 a + 2 b)" + 6 b ÷ 2 (= b - 2 a) M1 for a method to find \overrightarrow{AG} in terms of a and b $eg \frac{1}{2} (6\mathbf{b} - 6\mathbf{a}) - \frac{1}{3}$ "(3 a + 3 b)" (=2 b - 4 a) C1 for correct simplified expressions in terms of a and b for \overrightarrow{AG} and \overrightarrow{GN} followed by conclusion |



| Question | Working | Answer | Mark | Notes |
|------------------|--|------------------------|------|---|
| 385 | | Diagram drawn | 3 | B3 for fully correct shape(B2 for 3 or 4 vertices correct or enlargement scale factor 3 in wrong position or enlargement, centre <i>A</i>, with different scale factor)(B1 for 2 vertices correct or enlargement, not from <i>A</i>, with different scale factor) |
| 386 | | | 2 | B2 for correct side elevation (B1 for a rectangle with base 2 squares or height 3 squares) |
| 165 | $(7 + 3 + 3) \times (4 + 3 + 3) - 7 \times 4 = 102 OR 2 \times 7 \times 3 + 2 \times 4 \times 3 + 4 \times 3 \times 3 = 102$ | 11 | 4 | M1 for a correct method to find the area of one appropriate rectangle M1 for a complete method to find the area of the path M1 (dep on M1) for "102" ÷ 10 A1 cao from correct working |
| *388 | | 95° with reasons | 4 | M1 for angle $DBC = 180 - 125 (= 55)$ or angle $EAC = 180 - 125 (= 55)$ (May be on diagram) A1 for $x = 95$ C2 (dep on M1) with full reasons for their given method, e.g. angles on a straight line add up to 180° and angles in a triangle add up to 180° and <u>corresponding angles</u> are equal or <u>allied angles</u> / <u>co-interior angles</u> add up to 180° and angles in a triangle add up to 180° (C1 (dep on M1) for one appropriate reason linked to parallel lines) M1 for angle $CDB = 125 - 30 (= 95)$) (May be on diagram) A1 for $x = 95$ C2 (dep on M1) for full reasons, for their given method, e.g. <u>exterior</u> angles are equal to the sum of the <u>interior opposite</u> angles and <u>corresponding angles</u> are equal (C1 (dep on M1) for one of these appropriate reasons linked to parallel lines) |
| 389 " (a) | | 049 | 1 | B1 for answer in range 47 to 51 |
| (b) | | 12 | 2 | M1 for line drawn on a bearing of $320^{\circ} \pm 2^{\circ}$ A1 for answer in range 10 to 14 |



| Question | Working | Answer | Mark | Notes |
|----------|--|---|------|---|
| 38: | B at $(1, 0), (1, -1), (3, -2)$ C at $(-2, -1), (-2, -2), (0, -3)$ Rotation 90° clockwise (or 270° anti-clockwise) about $(-2, 2)$ | Rotation 90° clockwise centre (-2, 2) | 3 | M2 for stating rotation 90° clockwise (or 270° anti-clockwise) or centre (-2, 2) (M1 for showing B and C correctly on the grid) A1 for a fully correct description NB Award a maximum of M1 if more than one transformation is given |
| 169 | | 3.75 oe | 3 | M1 for a correct scale factor or ratio using two corresponding sides from similar triangles or two sides from the same triangle (may be seen in an equation) e.g $\frac{6}{1.5}$ oe or $\frac{1.5}{6}$ oe or $\frac{5}{6}$ or $\frac{6}{5}$ etc. (accept these written as ratios) M1 for a complete method to find ED A1 |
| 392 | | $9x^2 + 7x - 2$ | 4 | M1 for finding an expression for a missing length eg $4x - 1 - x - x$ (=2 $x - 1$) or $x + 2 - 2x$ (=2 - x) M1 for a correct expression for one area from the cross-section, eg. $x \times 2x$ or $(4x - 1)(x + 2 - 2x)$ or for one volume of cuboid(s), eg. $x \times 2x \times (x + 1)$ M1 for a complete method to find the volume A1 for $9x^2 + 7x - 2$ or $(9x - 2)(x + 1)$ oe |
| 171 | | 8 | 4 | M1 for $(2\sqrt{10})^2 - 2^2$ (= 36) A1 for (<i>CD</i> =) 6 M1 (dep on M1) for '6' × 4 - $\frac{1}{2}$ × '6' × 2 - $\frac{1}{2}$ × 2 × 2 - $\frac{1}{2}$ × ('6' - 2) × 4 C1 for area of 8 from fully correct working |



| Question | Working | Answer | Mark | Notes |
|----------------|---------|---------------------------|------|--|
| 394 | | 750 cm^3 | 3 | M1 for 30×25 A1 for 750 B1 (indep) for cm ³ |
| | | | | |
| 395 (a) | | Correct shape | 2 | B2 for correct reflection with vertices (-4, 2) (-6, 3) (-6, 7) (-4, 6) (B1 for reflection in a vertical or horizontal line) |
| (b) | | Correct shape | 2 | B2 for correct rotation with vertices $(-1, 3) (-5, 3) (-6, 5) (-2, 5)$ (B1 for rotation of 90(°) clockwise about (0,1) or correct orientation fully in top left quadrant) |
| *376 | | Conclusion (supported) | 5 | M1 for finding the area of one rectangle which is not 6×10 eg 2×2.5 (=5) or 4×10 (=40) or 2.5×6 or 5×2 |
| | | | | M1 for a complete method to find the total area eg 5+5+40 or 60-10 (=50) |
| | | | | M1 for a complete method to find the number of tins needed eg " 50 " ÷ 5 ÷ 2.5 (=4) |
| | | | | OR for a complete method to find the number of litres needed. eg "50" \div 5 (=10) |
| | | | | OR for a complete method to find the area covered by 3 tins eg $3 \times 2.5 \times 5$ (=37.5) |
| | | | | A1 for 50 (m ²) and 4 (tins needed) or for 10 (litres) and 7.5 (litres) or for $50(m^2)$ and $37.5(m^2)$ |
| | | | | C1 (dep M2) for a conclusion supported by their calculations |
| 397 | | $100 - 25\pi$ | 3 | M1 for $\pi \times 5 \times 5$ or 25π M1 for $(10 \times 10 - \pi \times 5 \times 5^{\circ})$ A1 for $100 - 25\pi$ oe NB: ignore the inclusion of any units. |



| Question | Working | Answer | Mark | Notes |
|----------|---------|-------------------------|------|--|
| 398 (a) | | Correct construction | 2 | M1 for correct construction arcs or bisector within guidelines but no (or incorrect) construction arcs A1 for bisector within guidelines with correct arcs shown |
| (b) | | Correct construction | 2 | M1 for correct construction arcs or perpendicular within guidelines but no (or incorrect) construction arcs A1 for perpendicular within guidelines with correct arcs shown |
| *399 | | 69° (supported) | 5 | M1 for method to find angle PSR eg 90 – 48 (= 42) or method in triangle POS to find angle POS (= 84) M1 for method to find angle PMS (= 42) A1 cao C2 (dep on at least M1) for correct and complete set of appropriate reasons (C1 for one correct reason involving a circle theorem supported by working) eg The tangent to a circle is perpendicular (90) to the radius (diameter) <u>Alternate segment theorem</u> . <u>Angles in a triangle add up to 180</u> Base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> . The <u>angle</u> at the <u>centre</u> of a circle is <u>twice the angle</u> at the <u>circumference</u> . |



| Question | Working | Answer | Mark | Notes |
|------------|---------|---|------|--|
| 39: (a)(i) | | a + b | 2 | B1 for $\mathbf{a} + \mathbf{b}$ oe |
| (ii) | | $-\mathbf{a} + 3\mathbf{b}$ | | B1 for $-\mathbf{a} + 3\mathbf{b}$ oe |
| (b) | | $\frac{3}{4}\mathbf{a} + \frac{3}{4}\mathbf{b}$ | 2 | M1 for $\overrightarrow{OP} + \frac{1}{4}\overrightarrow{PR}$ or $\overrightarrow{OR} + \frac{3}{4}\overrightarrow{RP}$ (may be in terms of a and b) A1 for $\frac{3}{4}\mathbf{a} + \frac{3}{4}\mathbf{b}$ or $\frac{3}{4}(\mathbf{a} + \mathbf{b})$ |
| *(c) | | $OS = \frac{3}{4}OT$ | 2 | C2 (dep A1) for <i>S</i> divides <i>OT</i> in the ratio 3:1 oe or $OS = \frac{3}{4}OT$ oe (C1 (dep A1) for <i>S</i> lies on <i>OT</i> or that <i>OT</i> and <i>PR</i> intersect at <i>S</i> oe) |
| 39; | | $\frac{1}{4} - \frac{\sqrt{6}}{12}$ | 3 | M1 for $\frac{1}{2} \times \frac{\sqrt{2}}{2} \times \frac{\sqrt{2}}{2}$ or $\frac{1}{2} \times \frac{\sqrt{2}}{2} \times \frac{\sqrt{3}}{3}$ M1 for $\frac{1}{2} \times \frac{\sqrt{2}}{2} \times \frac{\sqrt{2}}{2} - \frac{1}{2} \times \frac{\sqrt{2}}{2} \times \frac{\sqrt{3}}{3}$ A1 for $\frac{1}{4} - \frac{\sqrt{6}}{12}$ oe OR M1 for (BC =) $\frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{3}$ M1 for $\frac{1}{2} \times \left\{\frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{3}\right\} \times \frac{\sqrt{2}}{2}$ A1 for $\frac{1}{4} - \frac{\sqrt{6}}{12}$ oe |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---------------------|------|--|
| 3: 2 | | 40° | 4 | M1 for angle FBC=70 or CFG = x or ABF = 110 may be seen in diagram M1 for angle CBF = BFC =70 or $90 - \frac{1}{2}x$ A1 for 40 supported by working C1 (dep on M2) for all reasons and linked to appropriate working, e.g. <u>Alternate angles</u> are equal; <u>Allied angles</u> / <u>Co-interior angles</u> add up to <u>180°</u> ; Base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> ; <u>angles</u> in a <u>triangle</u> add to <u>180°</u> , <u>angles</u> on a straight <u>line</u> equals <u>180°</u> |
| *3:3 | | NO with evidence | 4 | M1 for $50 \times 40 \times 30$ (=60000) M1 for "60000" ÷ 3000 (=20) M1 for "20" × £3.50 C1 eg for 70 and comparison resulting in NO OR M1 for £60 ÷ 3.50 (=17 bottles) M1 for "17" × 3000 (=51000) M1 for 50 × 40 × 30 (=60000) C1 eg for 51000 and 60000 and comparison resulting in NO |
| 3:4 (a) | | 150 | 2 | M1 for $180 - (360 - 330)$ or $180 - 30$ or $330 - 180$ or a complete diagram showing the bearing of 330° A1 cao |
| (b) | | 11 40 | 4 | M1 for 200 ÷ 120 (=1 2/3 h) M1 for conversion between hours and minutes A1 for 1 h 40 min or 100 minutes B1 (ft dep on M1) for 11 40 |
| 3: 5 | | 126 | 4 | M1 for method to find exterior or interior angle of octagon M1 for method to find exterior or interior angle of pentagon M1 for complete method A1 cao |



| Question | Working | Answer | Mark | Notes |
|----------|---------|----------------------|------|--|
| 3: 6 | | 13.75 | 5 | M1 for finding perimeter of rectangle e.g. $5x + 5 + 5x + 5 + 4x + 4x$ (= $18x + 10$) M1 for finding perimeter of trapezium e.g. $9x - 2 + 7x - 2 + 10x$ (= $26x - 4$) M1 for equation e.g. $26x - 4 = 18x + 10$ (or $8x = 14$) A1 for finding the value of x as 1.75 B1 ft for subs of x into $5x + 5$ and evaluated (= 13.75) |
| 3:7 | | 756π | 5 | M1 for $\frac{1}{3}\pi r^2 \times 10$ (=270 π) A1 for $r = 9$ M1 (dep on M1) for $\frac{1}{2} \times \frac{4}{3}\pi \times "9"^3$ (= 486 π) M1 for 270 π + "486 π " oe A1 cao |
| *3: 8 | | Proof | 5 | M1 for finding one other vector expressed as a and/or b M1 for method to find one of \overline{DM} , \overline{MA} or \overline{DA} eg $\overline{DM} = -\mathbf{b} + \frac{1}{2}(3\mathbf{b} + \mathbf{a})$ oe, $\overline{MA} = \frac{1}{2}(3\mathbf{b} + \mathbf{a}) + \mathbf{a}$ oe or $\overline{DA} = 2\mathbf{b}+2\mathbf{a}$ oe M1 for method to find two of \overline{DM} , \overline{MA} or \overline{DA} A1 for two of $\overline{DM} = \frac{1}{2}(\mathbf{a} + \mathbf{b})$, $\overline{MA} = 1.5(\mathbf{a} + \mathbf{b})$, $\overline{DA} = 2(\mathbf{a}+\mathbf{b})$ ie simplified but oe C1 (dep on working shown) for conclusion relating to correct working |
| *3:9 | | Similarity and proof | 5 | B1 for method matching a pair of opposite angles, e.g. if $EAB = x$, $BDE = 180-x$, $EAB + BDE = 180$ B1 for linking angles between quad and triangle, e.g. if $BDE = 180-x$ then $BDC = x$ B1 for stating or implying $ACE = BCD$ (same angle) C1 for <u>Opposite angles</u> of a <u>cyclic quadrilateral</u> add up to <u>180°</u> or statement linking three angles for similarity C1 for complete proof |



| Que | estion | Working | Answer | Mark | Notes |
|-----|--------|---------|--|------|--|
| 3:: | | | 12 | 3 | M1 for a method to find volume of a cuboid, eg. $2 \times 10 \times 15$ (= 300) or $5 \times 5 \times x$ (= $25x$) M1 (dep) for "300" ÷ "25" oe A1 cao |
| | | | | | M1 for $10 \div 5 (= 2)$ and $15 \div 5 (= 3)$ or $10 \div 5 (= 2)$ and $2 \div 5 (= 0.4)$ M1 (dep) for $2 \times "2" \times "3"$ or $15 \times "2" \times "0.4"$ A1 cao |
| 3:; | (a) | | Triangle with vertices at $(-3, 3), (-3, 4)$ and $(-1, 4)$ | 2 | B2 for a triangle with vertices at $(-3, 3)$, $(-3, 4)$, $(-1, 4)$ (B1 for triangle in correct orientation and size or rotated 90° clockwise about centre <i>O</i> or three correct vertices without joining) |
| | (b) | | Reflection in line $y = x$ | 2 | B1 for reflection B1 for (in the line) $y = x$ Note: award no marks if more than one transformation is given |



| Question | Working | Answer | Mark | Notes |
|----------|---------|-------------------------------|------|--|
| *1; 0 | | Has enough (with evidence) | 5 | M1 for splitting the shape (or showing recognition of the "absent" triangles) and using a method to find the area of one shape M1 for a complete method to find the total area, (= 9 m ²) M1 (dep on M1) for a method to find the number of packs required from their total area, eg. "9" \div 2 = 4.5 rounded up to 5 M1 for a method to find 75% of 24.80 or 75% of the cost of their total number of packs, eg. 24.80 x "5" $\times \frac{75}{100}$ (= 93) or 24.80 $\times \frac{75}{100}$ (= 18.6) C1 for a conclusion supported by fully correct answers, eg. showing 9 (m ²), 5 (packs) and 93 or 7 (from 100 – 93) OR M1 for method to find 75% of £24.80, eg. 24.80 $\times \frac{75}{100}$ (= 18.6) M1 for method to find total number of packs Mary can buy, eg. 100 \div "18.60" = 5.3 truncated to 5 or 10 (m ²) M1 for finding area of one relevant shape or showing how one pack (2 m ²) can fit in the diagram M1 (dep on previous M1) for complete method to show that 5 packs can cover the floor C1 for a conclusion supported by fully correct answers, showing the capacity (10) greater than total area (9) |



| Question | Working | Answer | Mark | Notes |
|----------|---------|------------------|------|--|
| *3; 3 | | 40° with reasons | 4 | M1 for finding one related angle using parallel lines A1 for $x = 40(^{\circ})$ C2 for full reasons linked to appropriate method eg. <u>alternate angles</u> are equal_ and <u>angles</u> in a <u>triangle</u> add up to <u>180°</u> eg. <u>angles</u> on a straight line add up to <u>180°</u> and <u>corresponding angles</u> are equal and <u>alternate angles</u> are equal eg. <u>co-interior (allied) angles</u> add up to <u>180°</u> and <u>exterior angle</u> of a <u>triangle</u> is equal to <u>sum</u> of <u>interior</u> opposite <u>angles</u> Other solutions may include reasons such as: <u>vertically opposite angles</u> are equal the sum of <u>angles</u> at a <u>point</u> is equal to <u>360°</u> (C1 (dep on M1) for one appropriate reason linked to parallel lines) |
| 3;4 | | 48 | 5 | M1 for $8 - 2 (= 6)$ M1 (indep) for $x^2 + 8^2$ (provided $x \le 8$) M1 (dep on previous M1) fo $\sqrt{"x"^2 + 8^2}$ or $\sqrt{"100"}$ M1 (dep on M2) for $4 \times 2 + 4 \times "10"$ A1 cao |
| 3; 5 | | 18 | 4 | M1 for a method to find the exterior angle of a pentagon eg. $360 \div 5$ (=72) or the interior angle of a pentagon, eg. $180 - 360 \div 5$ (= 108) A1 for 72 or 108 M1 (dep M1) for a fully complete method to find the required angle, <i>DCF</i> A1 for 18 or ft their interior or exterior angle |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---------------|------|--|
| 3;6 | | 14 | 5 | M1 for correct substitution into a volume formula for a cylinder or a |
| | | $\frac{1}{3}$ | | cone, eg. $\frac{1}{3} \times \pi \times 3^2 \times 4$ (= 12 π) or $\pi \times 3^2 \times (6 - 4)$ (= 18 π) or $\pi \times 3^2 \times h$ (= 9 πh) or $\pi \times 3^2 \times (h-2)$ M1 for method to find volume after 5 hours, eg. "12 π " + "18 π " (= 30 π) M1 (dep on M1) for use of a correct ratio, eg. "30 π " $\times \frac{1}{5}$ (= 54 π) or "30 π " $\times \frac{4}{5}$ (= 24 π) M1 for deriving an equation in h , eg. "54 π " = "9 πh " + "12 π " A1 for $\frac{14}{3}$ or equivalent fraction |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|------------------------------|------|---|
| 3; 7 | | 9 | 4 | M1 for method to find area of one rectangle, eg 15×8 (=120) or 15×11 (=165) M1 (dep) for subtracting from/by given area, eg $(138 - "120")$ (=18) or "165" - 138 (=27) M1 for final step from complete method shown, eg $15 - "18" \div 3$ or "27" $\div 3$ A1 cao OR M1 for a correct expression for the area of one rectangle, eg $(8 + 3) \times (15 - x)$ or $8 \times x$ M1 (dep) for a correct equation eg $(8 + 3) \times (15 - x) + 8 \times x = 138$ M1 for correct method to isolate <i>x</i> , eg $3x = 27$ A1 cao |
| *3; 8 | | x = 130 + correct reasons | 4 | M1 for angle $BFG = 65$ may be seen on diagram M1 (dep) for correct method to calculate x, eg (x=) $65 + 65$ (=130) or (x=) $180 - (180 - 2 \times 65)$ (=130) C2 for <u>x</u> = 130 and full appropriate reasons related to method shown (C1 (dep on M1) for any one appropriate reason related to method shown) eg alternate angles; base angles in an isosceles triangle are equal; angles in a triangle add up to 180° ; angles on a straight line add up to 180° ; exterior angle of triangle = sum of two interior opposite angles; co-interior angles add up to 180° (allied angles) NB Any reasons stated must be used |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------------|------|--|
| 3;9 | | construction | 2 | M1 for a pair of arcs or a single arc, centre C , that cut line AB and at least one pair of arcs not at C within guidelines A1 for perpendicular within guidelines with appropriate construction arcs |
| | | | | M1 for an arc, centre A radius AC and an arc centre B radius BC. The two arcs must intersect below AB A1 for perpendicular within guidelines with appropriate construction arcs (SC If M0 scored, B1 for correct perpendicular line within guidelines) |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 3;: | | 25 | 4 | M1 for complete method to work out interior angle of a regular octagon or 135° identified as an interior angle of the octagon M1 for complete method to work out angle <i>KFG</i> or angle <i>KFG</i> identified as 110° M1 (dep on M2) for complete method to work out angle <i>KFE</i> , eg "135" - "110" or (8×"135" - 4×"135" - 4×"110") \div 4 or (3×180 - 2×"135" - 2×"110") \div 2 A1 for 25 with supporting working OR M1 for complete method to work out the exterior angle of a regular octagon or 45° identified as an exterior angle of the octagon M1 for complete method to work out angle <i>KFG</i> identified as 110° M1 (dep on M2) for complete method to work out angle <i>KFG</i> identified as 110° M1 (dep on M2) for complete method to work out angle <i>KFE</i> , eg 180 - "45" - "110" A1 for 25 with supporting working |
| | | | | OR M1 for complete method to work out the exterior angle of a regular octagon or 45° identified as an exterior angle of the octagon M1 for complete method to work out angle <i>JKF</i> or angle <i>JKF</i> identified as 70° M1 (dep on M2) for complete method to work out angle <i>KFE</i> , eg "70" – "45" A1 for 25 with supporting working |



| Que | stion | Working | Answer | Mark | Notes |
|-----|-------|---------|--------|------|---|
| 3;; | (a) | | 7.5 | 2 | M1 for $\frac{12}{18}$ oe or $\frac{18}{12}$ oe or $\frac{12}{5}$ oe or $\frac{5}{12}$ oe A1 cao |
| | (b) | | 45 | 3 | M1 for $\left(\frac{3}{2}\right)^2$ oe or $\left(\frac{2}{3}\right)^2$ oe M1 for complete method to find area of shaded region, eg 36 × "1.5" ² – 36 A1 cao (SC B2 for 81) |
| 220 | | | 128π | 5 | M1 for $\frac{4\pi r^2}{2} = 32\pi$ oe A1 for $(r =) 4$ M1 for $2 \times \pi \times "4" \times 10$ (=80 π) or $\pi \times "4"^2$ (=16 π) or ft their r M1 for $32\pi + "80\pi" + "16\pi"$ oe or 402.1 -402.3 or ft their r A1 cao |



| Questio | n Working | Answer | Mark | Notes |
|---------|-----------|----------------|------|--|
| *423 | | 3 | 4 | M1 for a method to calculate at least one area eg 10×7 (=70) or 16×10 (=160) M1 for a method to find the total area (=124) M1 (dep on M1) for "124" ÷ 36 C1 (dep on M3) for 3 (pigs) clearly identified and supported by correct calculations Or M1 for an area of $36m^2$ drawn with dimensions shown M1 for 3 areas of $36m^2$ drawn with dimensions shown M1 (dep on M1) for method to find the area left (=16) C1 (dep on M3) for 3 (pigs) clearly identified and supported by correct calculations |
| 424 (4 | a) | Shape drawn | 2 | B2 for shape with vertices at $(0, -1)$, $(-1, -3)$, $(-2, -3)$, $(-2, -1)$ (B1 for rotation of 180° about the wrong centre) |
| (1 | b) | Triangle drawn | 2 | B2 for triangle with vertices at (6, 9), (9, 9), (9, 3) (B1 for 2 vertices correct or enlargement sf 3 in wrong position or enlargement, centre (0, 0), but sf >1, \neq 3) |
| 425 | | 36 | 3 | M1 for a correct method to find either an interior or an exterior angle; eg. $(180 \times 3) \div 5$ or $540 \div 5$ (=108) or $360 \div 5$ (=72) M1 (dep) for a complete method to find angle <i>CFD</i> . A1 cao |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 206 | | 6 | 3 | M1 for $\frac{15}{10}$ (=1.5) or $\frac{10}{15}$ (=0.66) or $\frac{16}{10}$ (=1.6) or $\frac{10}{16}$ (=0.625) M1 for $\frac{15}{10} \times 16$ (=24) oe A1 cao OR M1 for $\frac{15}{16}$ (=0.9375) or $\frac{16}{15}$ (=1.066) or $\frac{16}{10}$ (=1.6) or $\frac{10}{16}$ (=0.625) M1 for $\frac{15}{16} \times 10$ (=9.375) oe A1 20.625 oe |
| 427 | | 55 | 3 | M1 for angle ABO = 90 or angle ADO = 90, or angle OBC = 15 or angle FDO = 90 or angle EBO = 90 (could be marked on the diagram) M1 for reflex angle BOD = $360 - (360 - 90 - 90 - 40)$ (= 220) or angle BCD = $(360 - 90 - 90 - 40) \div 2$ (= 70) or angle BDO or angle DBO = $90 - (180 - 40)/2$ (= 20) or angle BOC = $180 - (15 + 15)$ (=150) A1 cao |
| *228 | | Proof | 3 | M1 for $\overline{MN} = \overline{MO} + \overline{ON} (= \mathbf{n} - \mathbf{m})$ or $\overline{NM} = \overline{OM} + \overline{NO} (= \mathbf{m} - \mathbf{n})$ or $\overline{AB} = \overline{AO} + \overline{OB} (= 2\mathbf{n} - 2\mathbf{m})$ or $\overline{BA} = \overline{OA} + \overline{BO} (= 2\mathbf{m} - 2\mathbf{n})$ M1 for $\overline{MN} = \mathbf{n} - \mathbf{m}$ and $\overline{AB} = 2\mathbf{n} - 2\mathbf{m}$ oe C1 (dep on M1, M1) for fully correct proof, with $\overline{AB} = 2\overline{MN}$ or \overline{AB} is a multiple of \overline{MN} [SC M1 for $\overline{MN} = 0.5\mathbf{n} - 0.5\mathbf{m}$ and $\overline{AB} = \mathbf{n} - \mathbf{m}$ C1 (dep on M1) for fully correct proof, with $\overline{AB} = 2\overline{MN}$ or \overline{AB} is a multiple of \overline{MN}] |



| Que | stion | Working | Answer | Mark | Notes |
|-----|-------|---------|--|------|---|
| 429 | | | 120 cm ³ | 4 | M1 for $\frac{1}{2} \times 3 \times 4$ M1 (dep) for ' $\frac{1}{2} \times 3 \times 4$ ' × 20 A1 for 120 B1 (indep) for cm ³ |
| 42: | (a) | | Shape with vertices at (-1, 3), (0, 6), (2, 6), (1, 3) | 1 | B1 for correct shape in correct position |
| | (b) | | Rotation centre (0,0) 90° anticlockwise | 3 | B1 rotation B1 (centre) (0,0) B1 90° anticlockwise or 270° clockwise Note: award no marks if more than one transformation is given |
| 42; | | | 38 | 5 | M1 $3x - 5 = 19 - x$ M1 for a correct operation to collect the <i>x</i> terms or the number terms on one side of an equation of the form $ax + b = cx + d$ A1 for $x = 6$ M1 for substituting their value of <i>x</i> in the three expressions and adding or substituting their value of <i>x</i> after adding the three expressions A1 cao |

| Question | Working | Answer | Mark | Notes |
|----------|---------|---------------------------|------|--|
| *410 | | Not enough, needs £133 | 5 | M1 for splitting the shape (or showing recognition of the "absent" rectangle) and using a correct method to find the area of one shape M1 for a complete and correct method to find the total area M1 for a complete method to find 70% of 19 (= 13.3) or 70% of their total cost or 70% of their area A1 114(m²) and (£)133 or 114(m²) and (£)13.3(0) and 108(m²) C1 (dep on M2) for a conclusion supported by their calculations OR M1 for a complete method to find the number of tins required for one section of the area of the floor M1 for a complete method to find 70% of their total number of tins for the whole floor M1 for a complete method to find 70% of their total number of tins and multiply by 19 A1 (£)133 C1 (dep on M2) for a conclusion supported by their calculations |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---|------|---|
| *433 | 360 - y | $180 - \frac{y}{2}$ | 4 | $M1 ADC = \frac{y}{2}$ $A1 180 - \frac{y}{2}$ $C2 (dep on M1) for both reasons$ <u>Angle at centre is twice the angle at the circumference</u> <u>Opposite angles in cyclic quadrilateral</u> add to <u>180°</u> (C1 (dep on M1) for one appropriate circle theorem reason) OR M1 reflex $AOC = 360 - y$ A1 $\frac{360 - y}{2}$ oe C2 (dep on M1) for both reasons <u>Angles around a point</u> add up to <u>360°</u> <u>Angle at centre is twice the angle at the circumference</u> (C1 (dep on M1) for one appropriate circle theorem reason) |
| 434 | | Triangle with vertices at $(-1,-4)$, $(-1,-5)$, $(-3,-4.5)$ | 2 | M1 for correct shape and size and the correct orientation in the wrong position or two vertices correct A1 cao |



| Ques | stion | Working | Answer | Mark | Notes |
|------|-------|---|---|------|---|
| 435 | (a) | $\overrightarrow{AB} = -\mathbf{a} + \mathbf{b}$ $\overrightarrow{ON} = \overrightarrow{OA} + \frac{2}{3}\overrightarrow{AB}$ $\overrightarrow{ON} = \mathbf{a} + \frac{2}{3}(-\mathbf{a} + \mathbf{b})$ $= \frac{1}{3}\mathbf{a} + \frac{2}{3}\mathbf{b}$ OR $\overrightarrow{ON} = \overrightarrow{OB} + \frac{1}{3}\overrightarrow{BA}$ $\overrightarrow{ON} = \mathbf{b} + \frac{1}{3}(-\mathbf{b} + \mathbf{a})$ $= \frac{1}{3}\mathbf{a} + \frac{2}{3}\mathbf{b}$ | $\frac{1}{3}\mathbf{a} + \frac{2}{3}\mathbf{b}$ | 3 | M1 for correct vector equation involving \overrightarrow{ON} , eg. $\overrightarrow{ON} = \overrightarrow{OA} + \overrightarrow{AN}$, may be written, partially or fully, in terms of a and b , e.g. $(\overrightarrow{ON} =)$ $\mathbf{a} + \frac{2}{3} \overrightarrow{AB}$ M1 for showing answer requires $\overrightarrow{AN} = \frac{2}{3} \overrightarrow{AB}$ or $\overrightarrow{BN} = \frac{1}{3} \overrightarrow{BA}$ A1 $\frac{1}{3}\mathbf{a} + \frac{2}{3}\mathbf{b}$ oe |
| | (b) | $\overrightarrow{OD} = \overrightarrow{OA} + \overrightarrow{AC} + \overrightarrow{CD}$ = a + b + b = a + 2 b $\overrightarrow{OD} = 3\left(\frac{1}{3}\mathbf{a} + \frac{2}{3}\mathbf{b}\right)$ $\overrightarrow{OD} = 3 \overrightarrow{ON}$ | Proof | 3 | M1 for a correct vector statement for \overrightarrow{OD} or \overrightarrow{ND} in terms of a and b , e.g. $\overrightarrow{OD} = \mathbf{a} + \mathbf{b} + \mathbf{b}$ oe or $\overrightarrow{ND} = \frac{2}{3}(-\mathbf{b} + \mathbf{a}) + \mathbf{b} + \mathbf{b}$ oe A1 for correct and fully simplified vectors for \overrightarrow{ON} (may be seen in (a)) and for \overrightarrow{OD} (= $\mathbf{a} + 2\mathbf{b}$) or \overrightarrow{ND} (= $\frac{2}{3}\mathbf{a} + \frac{4}{3}\mathbf{b}$) C1 (dep on A1) for statement that \overrightarrow{OD} or \overrightarrow{ND} is a multiple of \overrightarrow{ON} (+ common point) |



| Que | stion | Working | Answer | Mark | Notes |
|-----|------------|------------------------|------------------|------|---|
| 214 | (a) | (4,0)(3,0)(3,-1)(2,-1) | Correct position | 2 | B2 for correct shape in correct position |
| | | (2, 2) (4, 2) | | | (B1 for any incorrect translation of correct shape) |
| | <i>a</i> > | | D | | |
| | (b) | | Rotation | 3 | BI for rotation |
| | | | 180° | | B1 for 180° (ignore direction) |
| | | | (0,1) | | B1 for (0, 1) |
| | | | | | |
| | | | | | OR |
| | | | | | |
| | | | | | B1 for enlargement |
| | | | | | B1 for scale factor -1 |
| | | | | | B1 for (0, 1) |
| | | | | | |
| | | | | | (NB: a combination of transformations gets B0) |
| | | | | | |



| Ques | stion | Working | Answer | Mark | Notes |
|------|-------|---------|--------|------|--|
| 215 | | | 1.5 | 4 | M1 for correct expression for perimeter eg. $4 + 3x + x + 6 + 4 + 3x + x + 6$ oe M1 for forming a correct equation eg. $4 + 3x + x + 6 + 4 + 3x + x + 6 = 32$ oe M1 for $8x = 12$ or $12 \div 8$ A1 for 1.5 oe OR M1 for correct expression for semi-perimeter eg. $4 + 3x + x + 6$ oe M1 for forming a correct equation eg. $4 + 3x + x + 6 = 16$ oe M1 for $4x = 6$ or $6 \div 4$ A1 for 1.5 oe |



| Que | stion | Working | Answer | Mark | Notes |
|-----|-------|---------|----------------|------|--|
| 438 | | | 1 hour 45 mins | 6 | M1 for method to find volume of pond, |
| | | | | | eg $\frac{1}{2}(1.3 + 0.5) \times 2 \times 1 \ (= 1.8)$ |
| | | | | | M1 for method to find the volume of water emptied in 20 minutes, $ag 1 \times 2 \times 0.2 = 0.4$ |
| | | | | | $100 \times 200 \times 20 (= 400000)$ |
| | | | | | A1 for correct rate $eg 0.8 \text{ m}^3/\text{hr} 0.4 \text{ m}^3$ in 30 minutes |
| | | | | | M1 for correct method to find total time taken to empty the |
| | | | | | pond, |
| | | | | | eg "1.8" ÷ "0.8" |
| | | | | | M1 for method to find extra time, |
| | | | | | eg 2 hrs 15 minutes – 30 minutes |
| | | | | | A1 for 1.75 hours, $1\frac{5}{4}$ hours, 1 hour 45 mins or 105 mins |
| | | | | | OR |
| | | | | | M1 for method to find volume of water emptied |
| | | | | | in 30 minutes, eg. $1 \times 2 \times 0.2 (= 0.4)$, |
| | | | | | $100 \times 200 \times 20 (= 400000)$ |
| | | | | | M1 for method to work out rate of water loss a_{2} "0.4" \times 2 |
| | | | | | eg. 0.4×2 |
| | | | | | M1 for correct method to work out remaining volume of water |
| | | | | | eg. $\frac{1}{2}(1.1+0.3) \times 2 \times 1$ (= 1.4) |
| | | | | | M1 for method to work out time, eg " 1.4 " ÷ " 0.8 " |
| | | | | | A1 for 1.75 hours, $1\frac{3}{4}$ hours, 1 hour 45 mins or 105 mins |
| | | | | | NB working could be in 3D or in 2D and in metres or cm throughout |



| Que | estion | Working | Answer | Mark | Notes |
|-----|-----------|---------|---|--------|---|
| 439 | | | 5 <i>x</i> ² | 4 | M1 for $4x \times 4x$ M1 for $(2x \times 4x)/2$ or $(2x \times x)/2$ or $(3x \times 4x)/2$ M1(dep M2) for "16 x^{2*} – "4 x^{2*} – " x^{2*} – "6 x^{2*} " A1 for $5x^2$ OR M1 for $\sqrt{(2x)^2 + (4x)^2} (= \sqrt{20x^2} = \sqrt{20} x)$ M1 for $\sqrt{(x)^2 + (2x)^2} (= \sqrt{5x^2} = \sqrt{5} x)$ M1(dep M2) for $\frac{\sqrt{5}x^* \times \sqrt{20}x^*}{2} (= \frac{\sqrt{100}}{2} x^2)$ A1 for $5x^2$ |
| 43: | (a (b) | | $\mathbf{a} - \mathbf{b}$ $\frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{b}$ | 1 3 | B1 for $\mathbf{a} - \mathbf{b}$ oe M1 for a correct vector statement for \overrightarrow{NR} eg. $(\overrightarrow{NR} =) \overrightarrow{NQ} + \overrightarrow{QR}$ or $(\overrightarrow{NR} =) \overrightarrow{NS} + \overrightarrow{SR}$ M1 for $\frac{2}{5}SQ (+QR)$ or $\frac{3}{5}QS (+SR)$ (SQ, QR, QS, SR may be written in terms of a and b) A1 for $\frac{2}{5}(\mathbf{a} - \mathbf{b}) + \mathbf{b}$ oe or $\frac{3}{5}(\mathbf{b} - \mathbf{a}) + \mathbf{a}$ oe |



| Ques | tion | Working | Answer | Mark | Notes |
|------|------|--|---------|------|--|
| *43; | | Angle <i>AED</i> = 38 <u>alternate angles</u> are <u>equal</u> | x = 109 | 4 | B1 for angle $AED = 38$ or $AEF = 142$ |
| | | Angle $ADE = (180 - 38) \div 2 = 71$ | | | M1 for a complete method to find one of the base angles of the |
| | | x = 180 - 71 | | | isosceles triangle |
| | | base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> | | | C2 (dep M1) for $x = 109$ with complete reasons |
| | | angles in a triangle add up to 180 | | | (C1 (dep M1) for one reason correctly used and stated) |
| | | angles on a straight line sum to 180 | | | |
| | | OR | | | |
| | | angle <i>AEF</i> = 142 <u>allied angles/co-interior</u> | | | |
| | | angles add up to <u>180</u> | | | |
| | | $ADE = 142 \div 2 = 71$ | | | |
| | | base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> | | | |
| | | exterior angle of a triangle is equal to the sum | | | |
| | | of the <u>interior opposite angles</u> , | | | |
| | | x = 180 - 71 | | | |
| | | <u>angles in a straight line add to 180</u> | | | |
| | | OR | | | |
| | | Angle $AED = 38$ <u>alternate angles</u> are <u>equal</u> for | | | |
| | | angles <i>BAE</i> and <i>AED</i> and <i>BAD</i> and <i>ADC</i> (x) | | | |
| | | Angle $DAE = (180 - 38) \div 2 = 71$ | | | |
| | | base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> | | | |
| | | angles in a triangle add up to 180 | | | |
| | | | | | |
| | | Angle $AED = 38$ <u>alternate angles</u> are <u>equal</u> | | | |
| | | Alight $ADL = (180 - 38) \div 2 = 71$ | | | |
| | | ord angles in a triangle sum to 190 | | | |
| | | and <u>angles in a triangle</u> sum to 180 | | | |
| | | $\lambda = 30 \pm 71$ alternate angles BAD and $ADC(x)$ are equal | | | |
| | | and $angles DAD$ and $ADC(x)$ are equal | | | |
| | | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 442 | | 54 | 3 | M1 for $180 - 360 \div 5$ or 108 seen as the interior angle of a pentagon M1 (dep on previous M1) for $360 - 2 \times (108' - 90)$ A1 for 54 cao |
| | | | | OR M1 for $180 \times (5-2)$ (= 540) ÷ 5 or 108 given as the interior angle of a pentagon M1 (dep on previous M1) for $360 - 2 \times '108' - 90$ A1 for 54 cao |



| Question | Working | Answer | Mark | Notes |
|----------|---|--------------------------------|------|--|
| 443 | Q at (-3, 1), (-6, 1) (-5, 3) (-3, 3) R at (-3, -1), (-6, -1), (-5, -3) (-3, -3) | Rotation 180° about (–1, 0) | 3 | M1 for showing R correctly on the grid without showing Q or for showing Q and R correctly on the grid A1 for rotation of 180° A1 for (centre) (-1, 0) Or M1 for showing R correctly on the grid without showing Q or for showing Q and R correctly on the grid A1 for Enlargement Scale Factor -1 A1 for centre (-1, 0) NB Award no marks for any correct answer from an incorrect diagram or any Accuracy marks if more than one transformation is given |
| 444 | | 68 | 3 | M1 for angle $OBC = 90^{\circ}$ or angle $OAC = 90^{\circ}$ (may be marked on the diagram or used in subsequent working) M1 for correct method to find angle BOC or AOC or AOB e.g. angle $BOC = 180 - 90 - 34$ (= 56) or angle $AOC = 180 - 90 - 34$ (= 56) or angle $AOB = 180 - 2 \times 34$ (= 112) A1 cao NB (68 must be clearly stated as an answer and not just seen on diagram) |
| 445 | Vertices at (-2, -4), (-4, -4), (-4, -6), (-2, -5) | Correct diagram | 3 | M1 for a similar shape in the correct orientation in the third quadrant M1 for an image in the correct orientation of the correct size A1 cao |












223.

| Que | estion | Working | Answer | Mark | Notes |
|-----|--------|---------|-------------------------|------|--|
| 446 | | | 75π | 3 | M1 for $(4 \times \pi \times 5^2) \div 2$ oe |
| | | | | | M1 for $\pi \times 5^{\circ}$ oe |
| | | | | | A1 for 75π accept 235.5 |
| | | | | | Condone the use of $\pi = 3.14$ |
| | | | | | |
| 447 | (a | | 6 b – 3 a | 1 | B1 for $6\mathbf{b} - 3\mathbf{a}$ oe |
| | | | | | |
| | (b) | | | 4 | M1 for $\overrightarrow{AX} = \frac{1}{3} \overrightarrow{AB}$ or $\frac{1}{3}$ '(6b - 3a)' or ft to 2b - a |
| | | | | | |
| | | | | | WI1 IOF OI = OD + DI - OD + 3a - D(-3b + 3a) Oe |
| | | | | | M1 for $\overrightarrow{OX} = 3\mathbf{a} + \mathbf{2b} - \mathbf{a}^2 = 2\mathbf{a} + 2\mathbf{b}$ oe |
| | | | | | Or → |
| | | | | | $OX = 6\mathbf{b} - \frac{2}{3}$ '(6 $\mathbf{b} - 3\mathbf{a}$)' (= 2 $\mathbf{a} + 2\mathbf{b}$) oe |
| | | | | | C1 for $\frac{2}{5}\overrightarrow{OY} = \frac{2}{5} \times 5(\mathbf{a} + \mathbf{b}) = 2(\mathbf{a} + \mathbf{b}) = \overrightarrow{OX}$ |
| | | | | | |



| Questi | on Working | Answer | Mark | Notes |
|--------|--|---|------|--|
| 448 | | Enlargement, scale factor 2.5, centre (0,0) | 3 | B1 for enlargement B1 for scale factor 2.5 oe B1 for (0,0); accept origin or O NB: if two different transformations are stated then 0 marks. |
| 449 | $\frac{9}{2} \times (12 + 18) = 135$ 135 ÷ 20 = 6.75 (=7 bags) 7 × 4.99 OR 18 × 9 - $\frac{1}{2}(6 \times 9)$ = 135 135 ÷ 20 = 6.75 (=7 bags) 7 × 4.99 | 34.93 | 4 | M1 for $\frac{9}{2} \times (12+18)$ or $18 \times 9 - \frac{1}{2}(6 \times 9)$ or $9 \times 12 + \frac{1}{2} \times (18-12) \times 9$ or 135 seen M1 (dep) for '135'÷ 20 or 6 or 7 seen M1 (dep on previous M1) for '6' × 4.99 or '7' × 4.99 A1 cao [SC: M1 for $(12 \times 9 + 6 \times 9) \div 20$ (= 162÷20) or 8 or 9 seen M1 (dep) for '8' × 4.99 or '9' × 4.99 OR M1 for $(18 \times 9 - 6 \times 9) \div 20$ (= 108÷20) or 5 or 6 seen M1 (dep) for '5' × 4.99 or '6' × 4.99] |
| 44: | | 380 | 3 | $ \begin{array}{lll} \text{M1} & \text{fo} \ 4 \times 7 + 5 \times 2 \ (=38) \ \text{or} \ 9 \times 2 + 5 \times 4 \ (=38) \ \text{or} \ 4 \times 7 \times 10 \ \text{or} \\ & (7 \times 9 - 5 \times 5) \ \text{or} \ 5 \times 2 \times 10 \ (=100) \ \text{or} \ 9 \times 2 \times 10 \ (=180) \\ & \text{or} \ 5 \times 4 \times 10 \ (=200) \ \text{or} \ 9 \times 7 \times 10 \ (=630) \ \text{or} \ 5 \times 5 \times 10 \ (=250) \\ \text{M1} & (\text{dep}) \ \text{or} \ `38' \times 10 \ \text{or} \ 380 \ \text{or} \ 4 \times 7 \times 10 + 5 \times 2 \times 10 \\ & \text{or} \ 9 \times 2 \times 10 + 5 \times 4 \times 10 \ \text{or} \ \times 10 \\ \text{A1} & \text{ca} \end{array} $ |
| 44; | | 36 – 9π | 3 | M1 fo $\pi \times 6 \times 6$ or 36π seen value 113.03-113.2 M1 for $12 \times 12 - (\pi \times 6 \times 6) \div 4$ or value 7.7-7.8 A1 for $36 - 9\pi$ oe OR M1 fo $\pi \times 6 \times 6 \div 4$ or 9π seen or value 28.2-28.3 M1 fo $6 \times 6 - (\pi \times 6 \times 6 \div 4)$ or value 7.7-7.8 A1 for $36 - (\pi \times 6 \times 6 \div 4)$ or value 7.7-7.8 A1 for $36 - (\pi \times 6 \times 6) \div 4$ or value 7.7-7.8 A1 for $36 - (\pi \times 6) \times 6)$ or value 7.7-7.8 A1 for $36 - (\pi \times 6) \times 6)$ or value 7.7-7.8 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 452 | | 230 | 2 | M1 for $180 + 50$ A1 cao OR M1 for $360 - (180 - 50)$ or $360 - 130$ A1 cao OR M1 for $50 + (90 - 50) + 90 + 50$ or $50 + 40 + 90 + 50$ A1 cao OR M1 for a suitable diagram (sketch) with bearing of lighthouse from ship indicated and 50° marked at lighthouse; diagram only intended to indicate position of 50° ; ignore other labels and markings unless they create ambiguity. A1 cao |
| 453 | | 84 | 4 | M1 for $x - 1 + 3x + 1 + 3x$ (= 56) or $7x = 56+1-1$ or $3x(x-1)$ oe 2 M1 for $7x = 56$ or 8 seen M1 for $0.5 \times (`8' - 1) \times (3 \times `8')$ A1 cao Ignore any statement of units. SC B2 for 8 as the answer or 7 identified as the height and 24 identified as the base of the triangle. |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 454 | | 12 | 4 | B1 for 60 seen M1 for $(360 - 60) \div 2 (=150)$ M1 for $360 \div (180 - 150)$ or $150 \times n=180(n-2)$ oe A1 cao OR B1 for 60 seen M1 for $60 \div 2 (=30)$ M1 for $360 \div (60 \div 2)$ A1 cao |
| | | | | OR M2 for 30 seen M1 for 360 ÷ 30 A1 cao |



| Qu | lestion | Working | Answer | Mark | Notes |
|-----|---------|---------|-----------------------|------|--|
| 455 | (a) | | a – 3 b | 1 | B1 for $\mathbf{a} - 3\mathbf{b}$ oe |
| | (b) | | | 4 | M1 for (NC =) $2a - 2b$ oe |
| | | | | | M1 for (NM =) $\mathbf{b} + \frac{1}{2}$ "($\mathbf{a} - 3\mathbf{b}$)" |
| | | | | | A1 for $\frac{1}{2}(\mathbf{a}-\mathbf{b})$ oe and $2\mathbf{a}-2\mathbf{b}$ oe |
| | | | | | C1 for NC is a multiple of NM (+ common point) |
| | | | | | OR |
| | | | | | M1 for (NC =) $2\mathbf{a} - 2\mathbf{b}$ oe |
| | | | | | M1 for (MC =) $\frac{1}{2}$ "(a-3b)"+a |
| | | | | | A1 for $\frac{3}{2}(\mathbf{a}-\mathbf{b})$ oe and $2\mathbf{a}-2\mathbf{b}$ oe |
| | | | | | C1 for NC is a multiple of MC (+ common point) |
| | | | | | OR |
| | | | | | M1 for (NM =) $\mathbf{b} + \frac{1}{2}$ "($\mathbf{a} - 3\mathbf{b}$)" |
| | | | | | M1 for (MC =) $\frac{1}{2}$ "(a-3b)"+a |
| | | | | | A1 for $\frac{1}{2}(\mathbf{a}-\mathbf{b})$ oe and $\frac{3}{2}(\mathbf{a}-\mathbf{b})$ oe |
| | | | | | C1 for $\mathbf{N}\mathbf{M}$ is a multiple to $\mathbf{M}\mathbf{C}$ (+ common point) |



| Qu | estion | Working | Answer | Mark | Notes |
|------------------|---------------|--|----------------------|-----------|--|
| <u>Qu</u> 456 | estion (a) | Working $360 \div 60 = 6$ $300 \div 60 = 5$ $6 \times 5 =$ | Answer Yes and 30 | Mark 3 | NotesM1 for dividing side of patio by side of paving slabeg. $360 \div 60$ or $300 \div 60$ or $3.6 \div 0.6$ or $3 \div 0.6$ or6 and 5 seen (may be on a diagram) or 6 divisions seen on length of diagram or 5divisions seen on width of diagramM1 for correct method to find number of paving slabseg. $(360 \div 60) \times (300 \div 60)$ oe or 6×5 or 30 squares seen on diagram(units may not be consistent)A1 for Yes and 30 (or 2 extra) with correct calculationsORM1 for correct method to find area of patio or paving slabeg 360×300 or 108000 seen or 60×60 or 3600 seen or 3.6×3 or 10.8 seen or 0.6×0.6 or 0.36 seenM1 for dividing area of patio by area of a paving slab eg. $(3.6 \times 3) \div (0.6 \times 0.6)$ oe(units may not be consistent)A1 for Yes and 30 (or 2 extra) with correct calculationsORM1 for method to find area of patio or area of 32 slabseg. $60 \times 60 \times 32$ or 360×300 M1 for method to find area of patio or area of 32 slabseg. $60 \times 60 \times 32$ and 360×300 M1 for method to find both area of patio and area of 32 slabseg. $60 \times 60 \times 32$ and 360×300 M1 for Yes and 115200 and 108000 ORYes and 11.52 and 10.8 NB : Throughout the question, candidates could be working in metres or |
| | | | | | centimetres |



| Quest | tion | Working | Answer | Mark | Notes |
|-------|------|---|--------|------|--|
| 456 | (b) | 1726 25890 27616 $2 8 6 3$ $7 16 1 2 6 3$ $7 16 1 2 6 2$ $1 6 1 2 6 2$ $1 6 1 2 6 3$ $2 1600 120 6$ $24000 1800 90$ $2 1600 120 6$ $24000 + 1800 + 90 + 1600 + 120 + 6 = 27616$ | 276.16 | 3 | M1 for complete correct method with relative place value correct. Condone 1 multiplication error, addition not necessary. OR M1 for a complete grid. Condone 1 multiplication error, addition not necessary. OR M1 for sight of a complete partitioning method, condone 1 multiplication error. Final addition not necessary. A1 for digits 27616 A1 ft (dep on M1) for correct placement of decimal point after addition (of appropriate values) (SC: B1 for attempting to add 32 lots of 8.63) |



| Question | Working | Answer | Mark | Notes |
|----------|---------|-----------------|------|---|
| 457 | | Rotation | 3 | B1 for rotation |
| | | 180° | | B1 for 180° |
| | | Centre (3, 3) | | B1 for (3, 3) |
| | | or | | OR |
| | | | | B1 for enlargement |
| | | Enlargement | | B1 for scale factor -1 |
| | | Scale factor -1 | | B1 for (3, 3) |
| | | Centre (3, 3) | | |
| | | | | B0 for a combination of transformations |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|-------------------------------------|--------|------|--|
| 458 | 3x-15 = 2x+24 | 39 | 3 | M1 for forming an appropriate equation eg. |
| | x = 39 | | | 3x - 15 = 2x + 24 |
| | | | | |
| | OR | | | OR |
| | 2x+3x-15+2x+2x+24 = 360 | | | 2x + 3x - 15 + 2x + 2x + 24 = 360 |
| | 9x + 9 = 360 | | | |
| | 9x = 351 | | | OR |
| | x = 39 | | | 2x + 2x + 24 = 180 |
| | OB | | | OP |
| | OR | | | OK 2 <i>n</i> + 2 <i>n</i> - 15 - 190 |
| | 2x + 2x + 24 - 180 4x + 24 = 180 | | | 2x + 3x - 13 - 180 |
| | 4x + 24 = 180 4x = 156 | | | OR |
| | r = 39 | | | 2r + 3r - 15 = 2r + 2r + 24 |
| | X 57 | | | $2\lambda + 5\lambda + 15 + 2\lambda + 2\lambda + 2\pi$ |
| | OR | | | M1 (dep) for correct operation(s) to isolate x and |
| | 2x + 3x - 15 = 180 | | | non-x terms in an equation to get to $ax = b$ |
| | 5x - 15 = 180 | | | A1 cao |
| | 5x = 195 | | | |
| | x = 39 | | | OR |
| | | | | 351 195 156 |
| | | | | M2 for $-\frac{1}{9}$ oe or $-\frac{1}{5}$ oe or $-\frac{1}{4}$ oe |
| | | | | |
| | | | | 111 000 |



| Question | Working | Answer | Mark | Notes |
|----------|------------------------------|--------|------|--|
| 459 | $6 \times 10 \times 8 = 480$ | 4 | 3 | M1 for $6 \times 10 \times 8$ or 480 seen |
| | $480 \div (6 \times 20) =$ | | | M1 (dep) for '480' \div (6 \times 20) oe |
| | | | | A1 cao |
| | | | | O.D. |
| | | | | |
| | | | | M1 for $20 \div 10$ (=2) or $10 \div 20$ (= $\frac{1}{2}$) or $\frac{8}{20}$ or $\frac{20}{8}$ or |
| | | | | M1 (dep) for $8 \div 2'$ or $8 \times \frac{1}{2}$ or $\frac{8}{20} \times 10$ oe or |
| | | | | $10 \div \frac{20}{8}$ |
| | | | | A1 cao |
| | | | | |
| | | | | SC : B2 for answer of 16 coming from $\frac{20 \times 8 \times 6}{10 \times 6}$ oe |



| Question | Working | Answer | Mark | Notes |
|----------|---|--------|------|--|
| 45: | $180 - (360 \div 6) = 120$ $180 - (360 \div 8) = 135$ 360 - 120 - 135 = OR $360 \div 6 = 60$ $360 \div 8 = 45$ 60 + 45 = | 105 | 4 | NB. Do remember to look at the diagram when marking this question. Looking at the complete method should confirm if interior or exterior angles are being calculated M1 for a correct method to work out the interior angle of a regular hexagon eg. $180 - (360 \div 6)$ oe or $(6 - 2) \times 180 \div 6$ oe or 120 as interior angle of the hexagon M1 for a correct method to work out the interior angle of a regular octagon $180 - (360 \div 8)$ oe or $(8 - 2) \times 180 \div 8$ oe or 135 as interior angle of the octagon M1 (dep on at least M1) for a complete method eg. $360 - "120" - "135"$ A1 cao |
| | | | | OR M1 for a correct method to work out an exterior angle of a regular hexagon eg. $360 \div 6$ or 60 as exterior angle of the hexagon M1 for a correct method to work out an exterior angle of a regular hexagon $360 \div 8$ or 45 as exterior angle of the octagon M1 (dep on at least M1) for a complete method eg. " 60 " + " 45 " A1 cao SC : B1 for answer of 255 |



| Qu | estion | Working | Answer | Mark | Notes |
|-----|--------|---|-----------------------------|------|---|
| 45; | (a) | | 35 | 1 | B1 for 34 – 36 |
| | (b) | | 110 | 1 | B1 for 108 – 112 |
| | (c) | | Position of <i>B</i> marked | 2 | B1 for a point marked on a bearing of $40^{\circ} (\pm 2^{\circ})$ from <i>H</i> or for a line on a bearing of $40^{\circ} (\pm 2^{\circ})$ (use straight line guidelines on overlay) B1 for a point 4 cm (\pm 0.2cm) from <i>H</i> or for a line of length 4 cm (\pm 0.2cm) from <i>H</i> (use circular guidelines on overlay) NB. No label needed for point |
| 462 | | $\frac{1}{2} \times 4 \times 3 = 6$ $\left(\frac{1}{2}\right)^2 \times 6 =$ | 1.5 | 3 | M1 for $\frac{1}{2} \times 4 \times 3$ oe M1 for $\left(\frac{1}{2}\right)^2 \times "6"$ A1 cao OR M2 for $\frac{1}{2} \times 2 \times 1.5$ oe (M1 for triangle with all lengths $\frac{1}{2}$ corresponding lengths of triangle <i>ABC</i> seen in any position or vertices seen at (1, 1) (3,1) and (2.5, 2.5) or stated) A1 cao |



| Que | estion | Working | Answer | Mark | Notes |
|------|--------|--|--------|------|--|
| 261* | | $ABO = ADO = 90^{\circ}$ | 65° | 4 | B1 for $ABO = 90$ or $ADO = 90$ (may be on diagram) |
| | | (Angle between tangent and radius is | | | B1 for $BCD = 65$ (may be on diagram) |
| | | 90°) | | | |
| | | DOB = 360 - 90 - 90 - 50 | | | C2 for $BCD = 65^{\circ}$ stated or $DCB = 65^{\circ}$ stated or angle C = 65° stated |
| | | (Angles in a quadrilateral add up to | | | with all reasons: |
| | | 360°) | | | angle between <u>tangent</u> and <u>radius</u> is <u>90°</u> ; |
| | | $BCD = 130 \div 2$ | | | <u>angles in a quadrilateral sum to 360°;</u> |
| | | (Angle at centre is twice angle at | | | <u>angle</u> at <u>centre</u> is <u>twice</u> angle at <u>circumference</u> |
| | | circumference) | | | (accept angle at circumference is half (or $\frac{1}{2}$) the angle at the centre) |
| | | OR (100 TO) | | | (C1 for one correct and appropriate circle theorem reason) |
| | | $ABD = (180 - 50) \div 2$ | | | QWC: Working clearly laid out and reasons given using correct |
| | | (Base angles of an isosceles triangle) | | | language |
| | | BCD = 65 | | | |
| | | (Alternate segment theorem) | | | OR |
| | | | | | B1 for $ABD = 65$ or $ADB = 65$ (may be on diagram) |
| | | | | | B1 for $BCD = 65$ (may be on diagram) |
| | | | | | C2 for $BCD = 65^{\circ}$ stated or $DCB = 65^{\circ}$ stated or angle C = 65° stated |
| | | | | | with all reasons: |
| | | | | | base <u>angles</u> of an <u>isosceles triangle</u> are <u>equal</u> ; |
| | | | | | <u>angles</u> in a <u>triangle</u> sum to <u>180°</u> ; |
| | | | | | tangents from an external point are equal; |
| | | | | | alternate segment theorem |
| | | | | | (C1 for one correct and appropriate circle theorem reason) |
| | | | | | QWC: Working clearly laid out and reasons given using correct |
| | | | | | language |
| | | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|--|------------|------|---|
| 464 | Vol cylinder = $\pi \times (2x)^2 \times 9x$ | 3 <i>x</i> | 3 | M1 for sub. into πr^2 h eg. $\pi \times (2x)^2 \times 9x$ oe |
| 404 | $= 36\pi x^{3} = \frac{4}{3}\pi r^{3}$ $r^{3} = 27x^{3}$ | 54 | | M1 for $\pi \times (2x)^2 \times 9x = \frac{4}{3}\pi r^3$ oe A1 oe eg. $\sqrt[3]{\frac{36x^3}{\frac{4}{3}}}$ |
| | | | | NB : For both method marks condone missing brackets around the $2x$ |



| Question | Working | Answer | Mark | Additional Guidance |
|-----------|---|---------------------|------|--|
| 243 FE | No of tiles around room = 2 × lengths of room = 8, 16, 16, 12 Total number of tiles = $8 \times 16 + 8 \times 12 = 224$ Cost = 4×224 OR Area of the room = $4 \times 8 + 4 \times 6 = 56$ Area of a tile = $0.5 \times 0.5 = 0.25$ Number of tiles = $56 \div 0.25$ = 224 Cost = 4×224 | £ 896 | 6 | M1 for doubling each length to show number of tiles for each side B1 for 8, 16, 16 and 12 M1 for a full method of finding the number of tiles $(12 \times 16 + 8 \times 4)$ A1 for at least one 'section' correct M1 for 4 × '224' A1 cao OR M1 for full method for finding the area of the room A1 at least one area correct B1 for area of tile = $0.25m^2$ or 2500 cm^2 or 4 tiles = 1 m^2 M1 for area of room \div area of a tile M1 for 4 × number of tiles A1 cao |
| 244 | $\frac{x}{5} = \frac{2}{4}$ $\frac{y}{x+5} = \frac{9}{6} \text{ or } \frac{y}{9} = \frac{x+5}{6}$ | x = 2.5 y =11.25 | 4 | M1 a correct expression for x involving ratios of sides, e.g. $\frac{x}{5} = \frac{2}{4}$ oe A1 cao M1 $\frac{y}{x+5} = \frac{9}{6}$ or $\frac{y}{9} = \frac{x+5}{6}$ oe A1 cao OR $\frac{y}{5} = \frac{9}{4}$ A1 cao |



| Question | Working | Answer | Mark | Additional Guidance |
|----------|--|---------------|------|--|
| 245 | Let $AB = x$, $AD = y$ Area of rectangle = xy Area $AXD = \frac{xy}{4}$ Area $CYZ = \frac{xy}{8}$ Shaded area = $\frac{5xy}{8}$ | $\frac{5}{8}$ | 4 | M1 a full method to find the unshaded area and subtracting from 1 B1 area of AXD = area of $ABCD \div 4$ B1 area of CYZ = area of $ABCD \div 8$ A1 cao OR Diagram M1 for dividing left into 2 congruent triangles for dividing right into 4 congruent triangles B1 left = $2A$ and $2A$ or shaded = $\frac{1}{2}$ of $\frac{1}{2} = \frac{1}{4} = \frac{2}{8}$ B1 right = $2A$ and A and A or shaded = $\frac{3}{4}$ of $\frac{1}{2} = \frac{3}{8}$ A1 cao Substitution M1 for deciding upon suitable side lengths for AD and AB and calculating dimensions of internal shapes B1 for area of DZX B1 for area of $ZXBY$ A1 cao OR M1 for deciding upon suitable side lengths for AD and AB and calculating dimensions of internal shapes B1 for area ADX B1 for area ADX B1 for area ZCY A1 cao |





| Ques | tion | Working | Answer | Mark | Additional Guidance |
|------|------------|--|---|------|---|
| 246 | (a) (i) | $\vec{BC} = \vec{CO} + \vec{OB}$ | 12a – 4b | 4 | $ \overrightarrow{BC} = \overrightarrow{CO} + \overrightarrow{OB} $ A1 cao $ M1 - 4a + 4b + \frac{1}{2} $ |
| | (ii) | AQ = AO + OB + BQ = -4a + 4b + $\frac{1}{4}$ (12a - 4b) | JU – a | | (12 a – 4 b)' A1 cao |
| | (b) | \overrightarrow{OX} = 12b , \overrightarrow{AX} =-4a + 12b = 4(-a + 3b) | Correct reason, with correct working | 3 | B1 \overrightarrow{OX} = 12b B1 \overrightarrow{AX} =-4a + 12b C1 convincing explanation |



| Question | Working | Answer | Mark | Notes |
|----------|---------|-------------------------------------|------|---|
| *469 | | x = 30° with complete reasons | 4 | M1 for a correct first step, eg angle $GED = 55$ or angle $GAD = 55$ or angle $EGA = 180 - 55$ (= 125) A1 for 30 C2 for 30 with full reasons, appropriate to their given method eg <u>alternate angles</u> are equal and <u>corresponding angles</u> are equal and <u>angles</u> on a straight <u>line</u> add up to <u>180</u> eg <u>corresponding angles</u> are equal and <u>angles</u> in a <u>triangle</u> add up to <u>180</u> and <u>alternate angles</u> are equal (C1 (dep on at least M1) for one appropriate reason relating to parallel lines or <u>opposite angles</u> of a <u>parallelogram</u>) |
| 46: | | Correct position of <i>C</i> | 3 | M1 for line drawn or point marked on a bearing of 130° from <i>A</i> M1 for line drawn or point marked on a bearing of 245° from <i>B</i> A1 for correct position of <i>C</i> |
| *46; | | No (supported) | 5 | M1 for $\pi \times 9 \div 2$ (=14.137) or $\pi \times 5 \div 2$ (=7.85) or for $\pi \times 9$ (=28.27) or $\pi \times 5$ (=15.7) M1 for complete method to work out perimeter eg 2 + 2 + ($\pi \times 9 \div 2$) + ($\pi \times 5 \div 2$) (= 25.99) M1 (dep M1) for method to find number of rolls required for their perimeter, eg "their total perimeter" $\div 2.4$ eg 25.99 $\div 2.4$ (=10.8), "47.97" $\div 2.4$ (=19.9) or "43.47" $\div 2.4$ (=18.3) M1 for method to work out cost eg $3 \times 10 + 2 \times 3.99$ (= 37.98) or 11×3.99 (=43.89), 20 \rightarrow 67.98, 19 \rightarrow 63.00 or for method to find how many rolls can be bought for £35 (= 10) C1 for a conclusion supported by fully correct answers eg 37.98 (for comparing with 35) e.g 10.8 and 10 OR M1 for $\pi \times 9 \div 2$ (=14.137) or $\pi \times 5 \div 2$ (=7.85) or for $\pi \times 9$ (=28.27) or $\pi \times 5$ (=15.7) M1 for complete method to work out perimeter eg 2 + 2 + ($\pi \times 9 \div 2$) + ($\pi \times 5 \div 2$) (= 25.99) M1 for a method to find how many rolls can be bought for £35 (=10) M1 for a method to find how many rolls can be bought for £35 (=10) M1 for a method to find how many rolls can be bought for £35 (=10) C1 for a conclusion supported by fully correct answers eg 25.9() and 24 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|------------------------------------|------|---|
| 472 | | 100 | 4 | M1 for $360 \div 9 (= 40)$ or $(9 - 2) \times 180 (= 1260)$ M1 (dep) for $180 - "40"$ or "1260" $\div 9 (= 140)$ oe M1 (dep M2) for a complete method to find the required angle, eg "140" - $(360 - "140" - "140") \div 2$ or $("140" \div 7) \times 5$ A1 for 100 supported by working |
| *473 | | No with correct calculations | 5 | M1 for splitting the cross section into separate areas and a method to find the area of one part OR for splitting up the pool into smaller prisms and a method to find the volume of one prism, e.g. a cuboid M1 (dep) for a complete method to find the cross-sectional area OR for a method to find the volume of more than on prism M1 (dep) for a complete method to find the vol of the pool (= 70 (m ³) OR for a complete method to find the depth of 60000L of water M1 for method to find figure for comparison, eg distance between surface and top of pool ("70" – "60") ÷ (5 × 10) C1 No, with correct calculations, eg water level is 20cm below top of pool |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 474 | | 41.6 | 6 | M1 for $0.5 \times 5.4 \times 7.3 \times \sin B = 19$ |
| | | | | M1 for $(B =) \sin^{-1} \left(\frac{19}{0.5 \times 5.4 \times 7.3} \right)$ oe (= 74.6) |
| | | | | M1 for $(AC^2 =) 5.4^2 + 7.3^2 - 2 \times 5.4 \times 7.3 \times \cos "74.6"$ |
| | | | | M1 (dep) for correct order of evaluation or 61.(479) |
| | | | | M1 for $\frac{\sin C}{5.4} = \frac{\sin "74.6"}{"7.84"}$ oe or $0.5 \times 7.3 \times "7.84" \times \sin C = 19$ |
| | | | | A1 for answer in the range 41.55 to 41.65 from correct working OR |
| | | | | (with perpendicular from C meeting AB at a point X) M1 for $0.5 \times 5.4 \times CX = 19$ |
| | | | | M1 for (<i>CX</i> =) $\frac{19}{0.5 \times 5.4}$ (= 7.037) |
| | | | | M1 for $BCX = \cos^{-1} \frac{"7.04"}{7.3} (= 15.425)$ |
| | | | | M1 for $(BX =) \sqrt{7.3^2 - "7.04"^2} (= 1.94)$ |
| | | | | M1 for $ACX = \tan^{-1} \frac{5.4^{-1}.94^{+1}}{"7.04"} (= 26.17)$ |
| | | | | A1 for answer in the range 41.55 to 41.65 from correct working |
| | | | | OR |
| | | | | (with perpendicular from A meeting BC at a point Y) |
| | | | | M1 for $AY = \frac{19}{7.3 \div 2} = 5.20547$ |
| | | | | M1 for $BY = \sqrt{5.4^2 - 5.20547''^2} (= 1.43630)$ |
| | | | | M1 for CY= 7.3–"1.43630" (= 5.86369) |
| | | | | M1 for tan $C = \frac{"5.20547"}{"5.86369"} (= 0.8877)$ |
| | | | | M1 for $C = \tan^{-1} "0.8877"$ |
| | | | | A1 for answer in the range 41.55 to 41.65 from correct working |



| Question | Working | Answer | Mark | Notes |
|----------|--|--------|------|---|
| 473 | | 26 | 3 | M1 for $(360 - 90) \div 2 (= 135)$ M1 for $4x + 31 = "135"$ or $6x - 21 = "135"$ A1 cao OR M1 for forming an appropriate equation eg $4x + 31 = 6x - 21$ or $6x - 21 + 4x + 31 + 90 = 360$ oe M1 (dep) for isolating terms in <i>x</i> and number terms A1 cao |
| 476 | | 180 | 3 | M1 for a correct start to the process, eg $300 \div 5 (= 60)$ or $300 \div (5 \times 1.5) (= 40)$ or $8 \div 5 (= 1.6)$ or $5 \div 8 (= 0.625)$ M1 for a complete method that will lead to the number of bricks needed to build the wall (= 480) or for a complete method that will lead to the number of extra bricks needed to build the wall, eg $300 \div 5 \times 3$ A1 cao |
| 477 | | 6.56 | 4 | M1 for $200^2 + 60^2$ (= 43600) M1 for $\sqrt{40000 + 3600}$ or $\sqrt{43600}$ (= 208.8) M1 for a complete method eg ("208.8" + 2 × 200 + 2 × 60) ÷ 100 × 0.9 oe A1 for 6.55 - 6.561 |
| 478 | $\pi \times 6^2 - 2 \times 6 \times 6$ | 41.1 | 4 | M1 for correct method to work out the area of the circle or quarter circle or semi-circle eg $\pi \times 6^2$ (=113(.09)); $\pi \times 6^2 \div 2 = 56.5(4)$; $\pi \times 6^2 \div 4 = 28.2(7)$ M1 for method to work out the area of the square (=72) oe or a triangle eg $\frac{1}{2} \times 6 \times 6$ (=18) M1 for complete method to find shaded area. A1 for value in the range 41.04 - 41.112 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 479 | | 126 | 3 | M1 for $180 - (360 \div 5) (= 108)$ or $(5 - 2) \times 180 \div 5 (= 108)$ |
| | | | | M1 for a complete method og $\frac{360 - 108''}{360 - 180} = \frac{180}{108''}$ |
| | | | | $\frac{1}{2} = \frac{1}{2} = \frac{1}{2}$ |
| | | | | A1 cao |
| | | | | |
| 47: | | 28.9 | 5 | M1 for $\sin 62 = \frac{BD}{15}$ or $\frac{BD}{\sin 62} = \frac{15}{\sin 90}$ oe |
| | | | | M1 for $(BD =)$ 15 × sin 62 or $\frac{15}{\sin 90}$ × sin 62 oe (= 13.24) |
| | | | | M1 for $\tan BCD = \frac{"13.24"}{24}$ oe or $\tan BDC = \frac{24}{"13.24"}$ with <i>BDC</i> |
| | | | | clearly identified |
| | | | | M1 for $BCD = \tan^{-1} \frac{"13.24"}{24}$ or $BDC = \tan^{-1} \frac{24}{"13.24"}$ with BDC |
| | | | | clearly identified |
| | | | | A1 for 28.8 – 28.9 |
| | | | | OR |
| | | | | M1 for $\cos(90 - 62) = \frac{BD}{15}$ |
| | | | | M1 for $(BD =)$ 15 × cos(90 – 62) (= 13.24) |
| | | | | M1 for tan $BCD = \frac{"13.24"}{24}$ oe or tan $BDC = \frac{24}{"13.24"}$ with BDC |
| | | | | clearly identified |
| | | | | M1 for $BCD = \tan^{-1} \frac{"13.24"}{24}$ or $BDC = \tan^{-1} \frac{24}{"13.24"}$ with BDC |
| | | | | clearly identified |
| | | | | A1 for 28.8 – 28.9 |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---|------|--|
| *47; | | 28° | 4 | M1 for angle $ABD = 62^{\circ}$ M1 for angle $ADB = 90^{\circ}$ C2 for angle $ADB = 28^{\circ}$ with full, appropriate reasons given <u>angles</u> in the <u>same segment</u> are <u>equal</u> ; <u>angles</u> in a <u>semicircle</u> are <u>90^{\circ}</u> ; <u>angles</u> in a <u>triangle</u> add up to <u>180^{\circ}</u> (C1 (dep on relevant M1) for one correct and appropriate reason relating to a circle theorem) OR M1 for angle $AOD = 62^{\circ} \times 2$ (= 124°) M1 for ($180^{\circ} - 124^{\circ}$) $\div 2$ C2 for angle $ADB = 28^{\circ}$ with full, appropriate reasons given the <u>angle</u> at the <u>centre</u> of a circle is <u>twice</u> the <u>angle</u> at the <u>circumference</u> ; base <u>angles</u> of an <u>isosceles</u> triangle are <u>equal</u> ; <u>angles</u> in a <u>triangle</u> add up to <u>180^{\circ}</u> (C1 (dep on relevant M1) for one correct and appropriate reason relating to a circle theorem) |
| *482 | | No with explanation and supportive working | 4 | M1 for method to find the volume of compost needed to fill one or more baskets eg $\frac{2}{3} \times \pi \times 20^3$ (= 16755(.16)) Or $\frac{4}{3} \times \pi \times 20^3$ (= 33510(.32)) M1 for appropriate use of 1 litre = 1000 cm ³ , eg $4 \times 50 \times 1000$ (= 200000) or "16755" ÷ 1000 M1 for complete method to find values needed to make decision C1 for conclusion supported by correct values, eg 200000 and 201061(.92) (accept 201000 to 201120) or 16666(.66) and 16755(.16) or 11.9(36) NB Calculations can be in litres or cm ³ |

| Question | Working | Answer | Mark | Notes |
|----------|---------|---|------|---|
| 483 | | Correct conclusion from correct working | 4 | B1 for $\overrightarrow{AB} = -5\mathbf{a} + 2\mathbf{b}$ or $\overrightarrow{BA} = 5\mathbf{a} - 2\mathbf{b}$ M1 for a correct vector statement for \overrightarrow{OT} eg $\overrightarrow{OA} + \overrightarrow{AT}$ or $\overrightarrow{OB} + \overrightarrow{BT}$ or $\overrightarrow{OA} + \frac{5}{6}$ \overrightarrow{AB} or $\overrightarrow{OB} + \frac{1}{6}$ \overrightarrow{BA} , may be written partially or fully in terms of \mathbf{a} and \mathbf{b} M1 for $5\mathbf{a} + \frac{5}{6}$ (-5 \mathbf{a} + 2 \mathbf{b}) oe or 2 $\mathbf{b} + \frac{1}{6}$ (5 \mathbf{a} - 2 \mathbf{b}) oe A1 for $\frac{5}{6}$ (\mathbf{a} + 2 \mathbf{b}) is parallel to \mathbf{a} + 2 \mathbf{b} |



| Question | Working | Answer | Mark | Notes |
|----------|---------|----------------------|------|---|
| 484 | | 9.25 | 3 | M2 for $x + x + 4 + x + x + 4 = 45$ oe or $x + x + 4 = 22.5$ oe (M1 for $x + x + 4 + x + x + 4$ oe) A1 for 9.25 or $\frac{37}{4}$ oe OR M1 for $45 - 8 (= 37)$ or $22.5 - 4 (= 18.5)$ M1 for $(45 - 8) \div 4$ or $(22.5 - 4) \div 2$ A1 for 9.25 or $\frac{37}{4}$ oe |
| 485 | | 124° with reasons | 4 | M1 for a method to find any angle, eg. angle $DEF = 180 - 70 - 54$ (= 56) or angle $AEB = 70$ or angle $EAB = 54$ or angle GEB = 180 - 70 (= 110) A1 for $x = 124$ NB: angles may be just shown on the diagram C2 for full reasons, appropriate to their given method, with no additional reasons (C1 for one appropriate reason relating to parallel lines) Possible reasons: <u>corresponding angles are equal; alternate angles</u> are equal; <u>co-interior angles (allied)</u> add up to <u>180</u> <u>angles on a straight line add up to <u>180</u>; <u>angles in a triangle</u> add up to <u>180; <u>vertically opposite angles</u> are equal ; the <u>exterior angle of a triangle</u> is equal to the sum of the <u>interior opposite angles;</u> <u>angles at a point</u> add up to <u>360</u>;</u></u> |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 486 | | 3 | 5 | M1 for a complete method to find the area of the cross section, eg. $15 \times 2 + "(12 - 4)" \times 2 + 15 \times 2$ (= 76) or for finding the volume of a relevant prism, eg. $15 \times 2 \times 120$ (= 3600) "(12 - 4)" maybe just seen on the diagram M1 for a method to find the volume of the bar, eg. "76" × 120 (= 9120) or ft "area of cross section"×120 provided "area of cross section" includes a method to find the area of at least two relevant rectangles M1 for "volume" × 8, eg. "9120" × 8 (= 72960) or 250 × 1000 ÷ 8 (= 31250) NB "volume" must be dimensionally correct M1 (dep on previous M1) for 250 ÷ ("volume" × 8) ÷ 1000, eg. 250 ÷ "72960 ÷ 1000" (= 3.4265) or "31250" ÷ "9120" A1 for an answer of 3 with correct working |
| 487 | | 30.1 | 4 | M1 for a correct trigonometric statement to find an unknown angle, eg. sin(30+x) or cos $A = \frac{10.4 + 5.2}{18}$ or $\frac{\sin ADC}{18} = \frac{\sin 30}{10.4}$ M1 for a complete method to find the angle, eg. sin ⁻¹ $\left(\frac{10.4+5.2}{18}\right)$ (= 60.07) or cos ⁻¹ $\left(\frac{10.4+5.2}{18}\right)$ (= 29.92) or sin ⁻¹ $\left(\frac{18 \times \sin 30}{10.4}\right)$ (= 59.92 or 180 – 59.92 = 120.07) M1 (dep on M2) for a fully complete method to find angle x, eg. "60.07.". – 30 or 60 – "29.92" or 90 – "59.92" A1 for answer in the range 30.07 to 30.1 OR M1 for $(BC^2=)$ 18 ² – $(10.4 + 5.2)^2$ or $BC^2 + (10.4 + 5.2)^2 = 18^2$ M1 for $(BC =) \sqrt{18^2 - (10.4 + 5.2)^2}$ (= 8.97) M1 (dep on M2) for a fully complete method to find angle x, eg. tan ⁻¹ $\left(\frac{5.2}{"8.97"}\right)$ A1 for answer in the range 30.07 to 30.1 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 488 | | 28.9 | 3 | M2 for $\frac{75}{360} \times 2 \times \pi \times 6$ oe $+ \frac{75}{360} \times 2 \times \pi \times 10$ oe (= 7.85 + 13.08 = 20.94) (M1 for $\frac{75}{360} \times 2 \times \pi \times 6$ oe or $\frac{75}{360} \times 2 \times \pi \times 10$ oe) A1 for 28.9 to 28.95 |



| Que | stion | Working | Answer | Mark | Notes |
|-----|-------|---------|--------|------|--|
| 489 | | | 80.4 | 6 | M1 for $0.5 \times 7 \times 8 \times \sin x = 18$ |
| | | | | | M1 (dep) for (x =) $\sin^{-1}\left(\frac{18}{0.5 \times 7 \times 8}\right)$ oe (= 40) |
| | | | | | M1 (dep on at least M1) for $(AC^2 =) 7^2 + 8^2 - 2 \times 7 \times 8 \times \cos \text{``40''}$ M1 (dep on previous M1) for correct order of evaluation or 27.2(03) or 5.2(15) |
| | | | | | M1 (dep) for sin $A = \frac{8 \times \sin^{4} 40^{"}}{"5.2(15)"}$ or sin $A = \frac{18}{0.5 \times 7 \times "5.2(15)"}$ |
| | | | | | or $\cos A = \frac{"5.2(15)"^2 + 7^2 - 8^2}{2 \times "5.2(15)" \times 7}$ A1 for answer in the range 80.3 to 80.4 from correct working |
| | | | | | OR III III III III IIII |
| | | | | | (with perpendicular from A meeting BC at a point X) |
| | | | | | M1 for $0.5 \times 8 \times h = 18$ |
| | | | | | M1 (dep) for (<i>h</i> =) $\frac{18}{0.5 \times 8}$ (= 4.5) |
| | | | | | M1 (dep on at least M1) for $BAX = \cos^{-1} \frac{"4.5"}{7} (= 49.99 \dots)$ |
| | | | | | M1 (dep) for $(BX =) \sqrt{7^2 - "4.5"^2} (= 5.3619)$ |
| | | | | | M1 (dep) for $CAX = \tan^{-1} \frac{8 - "5.3619"}{"4.5"} (= 30.38)$ |
| | | | | | A1 for answer in the range 80.3 to 80.4 from correct working |
| | | | | | NB Similar method applies for use of perpendicular from <i>C</i> to <i>AB</i> |



| Que | estion | Working | Answer | Mark | Notes |
|------|------------|---------|--------------------------------------|------|--|
| 48: | | | 40 000 | 2 | M1 for 100×100 isolated or $4 \times 100 \times 100$ A1 cao |
| | | | | | |
| *48; | | | No not enough | 5 | M1 for substituting into Pythagoras' theorem M1 for complete correct use of Pythagoras' theorem M1 for a complete method to find the perimeter of their trapezium A1 51.(20655) C1 (dep on correct first 2 M marks) for correct conclusion dependent upon supporting calculations |
| 492 | | | Correct line drawn | 2 | M1 for two pairs of relevant arcs drawn A1 correct line drawn (with arcs) SC B1 Correct line no arcs visible |
| 493 | | | Rotation about (2,1) through 180° | 3 | B1 rotation B1 about (2,1) B1 through 180° Or B2 enlargement scale factor -1 B1 about (2,1) Note Award no marks if more than one transformation is given |
| *494 | (a) (b) | | 2.75 | 1 | C1 for a complete reason eg <u>Angles</u> in a <u>semicircle</u> are <u>90°</u> , <u>alternate</u> <u>segment</u> theorem M1 for $7 \times \sin 35$ M1 for $7 \times \sin 35 \times 2$ M1 (indep) for " <i>DB</i> "× cos 70 A1 2.74 - 2.75 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 495 | | 31.1 | 5 | M1 for $\frac{1}{2} \times 8.4 \times x \times \sin 40 = 100$ M1 for $100 \div (0.5 \times 8.4 \times \sin 40)$ (= 37.(041)) M1 (dep on 1 st M1) for substituting the appropriate figures into the cosine rule eg 8.4^{2+} '37.041' ² -2× $8.4 \times$ '37.041'cos40° M1 (dep on previous M1) for correct order of evaluation or (c^{2} =) 965.(897) A1 31.07 - 31.1 |



| Que | stion | Working | Answer | Mark | Notes |
|------|-------|---|-------------------------------|------|---|
| 496 | | | Enlargement | 2 | B2 for fully correct triangle (B1 for 2 vertices correct or enlargement scale factor 2 in the wrong position or enlargement, centre <i>A</i> , with a different scale factor) |
| *497 | | | No supported by working | 4 | M1 for $\pi \times 7$ (= 21.9 to 22) or $\pi \times 7 \times 2.54$ = (55.5 to 56) M1 (dep) for a complete method that could lead to two figures that are comparable eg $\pi \times 7 \times 2.54$; $\pi \times 7$ and $50 \div 2.54$ A1 for correct comparable figures eg 55.5 to 56 (cm); 21.9 to 22 (in) and 19.6 to 19.7 (in) C1 (dep M2) for a correct conclusion based on their comparable figures OR M1 for eg 50 $\div \pi$ (= 15.9 to 15.92) or 50 $\div 2.54\pi$ (=6.26 to 6.27) M1 (dep) for a complete method that could lead to two figures that are comparable eg (50 $\div \pi$) $\div 2.54$; 50 $\div \pi$ and 7 $\times 2.54$ A1 for correct comparable figures eg 6.26 to 6.27 (in); 15.9 to 15.92 (cm) and 17.7 to 17.8 (cm) C1 (dep M2) for a correct conclusion based on their comparable figures |
| 498 | | | 245 | 2 | M1 for method to identify the angle required, including on a diagram A1 cao |
| 499 | | $BC = \frac{12}{\tan 60} = 6.92(8)$ $DE = 6.92() \times \tan 30 = 4$ $CE = 12 + 4$ $AC = \frac{12}{sin60} = 13.8(5)$ $CE = \frac{13.8(5)}{cos30}$ | 16 with supporting working | 4 | M1 for a method to find BC or AC or AD B1 for angle $EAD = 30^{\circ}$ or $AED = 60^{\circ}$ or $ACD = 30^{\circ}$ or $CAD = 60^{\circ}$ M1 for a method to find CE A1 for 15.9-16.1 with supporting working |



| Questi | on Working | Answer | Mark | Notes |
|--------|--|--|------|---|
| 49: | | 22.5 | 3 | M1 for $\frac{1}{2} \times 7 \times 5 \times \sin 40$ or $\frac{1}{2} \times 7 \times 5 \times \sin(180 - 40)$ M1 (dep M1) for doubling the area of the triangle A1 for 22.4 - 22.5 OR M1 for complete method to find height of parallelogram, eg 5 sin40° M1 (dep M1) for complete method to find the area of the parallelogram, eg 7 × 5sin40° A1 for 22.4 - 22.5 |
| 49; | $\overrightarrow{AB} = \overrightarrow{AO} + \overrightarrow{OB}$ $= \mathbf{a} + \mathbf{b}$ $\overrightarrow{AC} = \frac{7}{2} \overrightarrow{AB}$ $\overrightarrow{OC} = \overrightarrow{OA} + \overrightarrow{AC}$ $= 2\mathbf{a} + \mathbf{b} + \frac{7}{2} (\mathbf{a} + \mathbf{b})$ | $\frac{11}{2}\mathbf{a} + \frac{9}{2}\mathbf{b}$ | 4 | M1 for $\overrightarrow{AB} = \overrightarrow{AO} + \overrightarrow{OB} (= -(2\mathbf{a} + \mathbf{b}) + (3\mathbf{a} + 2\mathbf{b}))$ or $\mathbf{a} + \mathbf{b}$ M1 for $\overrightarrow{AC} = \frac{7}{2} \overrightarrow{AB}$ or $\overrightarrow{BC} = \frac{5}{2} \overrightarrow{AB}$, may be in terms of \mathbf{a} and \mathbf{b} M1 (dep M2) for complete method to find \overrightarrow{OC} in terms of \mathbf{a} and \mathbf{b} A1 for $\frac{11}{2}\mathbf{a} + \frac{9}{2}\mathbf{b}$ or equivalent simplest form (SCB2 for $\frac{11}{2}\mathbf{a} + \frac{23}{2}\mathbf{b}$ or $\frac{11}{2}\mathbf{a} + \frac{19}{2}\mathbf{b}$) |



| Que | estion | Working | Answer | Mark | Notes |
|-------|------------|---------|--|------|---|
| 4:2 | (a) (b) | | Correct shape Translation by $\begin{pmatrix} 4\\ -1 \end{pmatrix}$ | 2 | B2 cao (B1 for shape in the correct orientation below the line $y = x$ or for 2 vertices correct) with vertices at (2, 1), (4, 1), (4, 0), (3, 0) B1 for translation B1 for $\begin{pmatrix} 4 \\ -1 \end{pmatrix}$ NB: B0 if more than one transformation given |
| *4: 3 | | | No + reason | 4 | M1 for intention to find the circumference eg 140 × π (= 439.82) A1 for circumference = 439 - 440 M1 (dep on M1) for a complete method shown that could arrive at two figures that are comparable eg "C"÷60×12 (=87.96), 90÷12×60 (=450), 90×60÷"C" (=12.27), "C"÷90×12 (=58.64) C1 (dep on both M marks) for No and explanation that shows a correct comparison eg only 84 people could sit around the tables or that 13 tables are needed or that 480 cm is needed. |
| 4:4 | (a) (b) | | 65 С | 5 | M1 for splitting up the cross section into separate areas and a method to find the area of one part OR for splitting up the pool into smaller prisms and a method to find the volume of one small prism, e.g. a cuboid M1 (dep) for a complete method to find the area of the cross section [with correct dimensions] OR for a method to find the total volume of more than one correct prism M1 (dep) for a complete method to find the volume of the pool [with correct dimensions] (= 195) M1 for "195" × 1000 ÷ 50 (=3900) oe where "195" comes from a volume A1 cao |
| | (0) | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---|--------|------|--|
| 4:5 | $AC^{2} = 5^{2} + 3^{2}$ $AC = \sqrt{25 + 9} (=5.83)$ $\frac{5}{5.83} = \frac{DB}{3}$ $DB = \frac{5}{5.83} \times 3 (= 2.57)$ $5 + 3 + 5.83 + 2.57 =$ OR $AC = \sqrt{25 + 9} (=5.83)$ $\tan A = \frac{3}{5}$ $A = 30.96$ $\sin 30.96 = \frac{DB}{5}$ $DB = 5 \times \sin 30.96 (= 2.57)$ $5 + 3 + 5.83 + 2.57 =$ | 16.4 | 5 | M1 for $(AC^2) = 5^2 + 3^2 = 34$) M1 for $\sqrt{25 + 9}$ or $\sqrt{34}$ (=5.83) M1 for $\frac{5}{5.83'} = \frac{DB}{3}$ or $DB \times AC = 5 \times 3$ M1 for $(DB =) \frac{5}{5.83'} \times 3$ A1 for 16.4 to 16.41 OR M1 for $(AC^2) = 5^2 + 3^2$ (=34) M1 for $\sqrt{25 + 9}$ or $\sqrt{34}$ (=5.83) M1 for using a correct trig ratio in an attempt to find angle <i>A</i> or angle <i>C</i> , e.g. $\tan A = \frac{3}{5}$, $\sin A = \frac{3}{5.83'}$, $\cos C = \frac{3}{5.83'}$ M1 for using <i>DB</i> in a a correct trig ratio, e.g. $\sin^3 30.96' = \frac{DB}{5}$ A1 for 16.4 to 16.41 |
| 4: 6 | | 35° | 4 | M1 for $ABC = 90$ M1 for $(ACB =) 180 - 90 - 25 (= 65)$ M1 for $(DBC =) 180 - '65' - 80 (= 35)$ A1 cao supported by working OR M1 for $(AOB =) 180 - 2 \times 25 (= 130)$ M1 for $(ADB =) 130 \div 2 (= 65)$ M1 for $(DAC =) 180 - 65 - 80$ A1 cao supported by working. |


| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 4: 7 | | 8.52 | 5 | M1 for $\frac{BD}{\sin 45} = \frac{7.4}{\sin 80}$ oe M1 for $(BD =) \frac{7.4}{\sin 80} \times \sin 45 (= 5.3133)$ M1 for $5.8^2 + 5.31^2 - 2 \times 5.8 \times 5.31$ cos100 M1 (dep) for correct order of evaluation or 72.5(73) A1 for $8.51 - 8.52$ OR M1 for $\frac{AD}{\sin(180 - 80 - 45)} = \frac{7.4}{\sin 80}$ oe M1 for $(AD =) \frac{7.4}{\sin 80} \times \sin(180 - 80 - 45) (= 6.15)$ M1 for $7.4^2 + (6.15^2 + 5.8)^2 - 2 \times 7.4 \times (6.15^2 + 5.8) \times \cos 45$ M1 (dep) for correct order of evaluation or 72.5(7398) A1 for $8.51 - 8.52$ |



| Question Working Answer Mark | | Notes | | |
|------------------------------|--|--|---|--|
| 4: 8 | | 28.3 | 2 | M1 for $\pi \times 9$ or $2 \times \pi \times 4.5$ oe A1 for $28.25 - 28.3$ |
| 4:9 | | Translation $\begin{pmatrix} 5\\ -3 \end{pmatrix}$ | 2 | B1 for translation B1 for $\begin{pmatrix} 5 \\ -3 \end{pmatrix}$ NB No marks if more than one transformation given. |
| *4:: | | 54 with reasons | 3 | M1 for angle <i>RWY</i> or angle TWZ = $180 - 126$ (= 54) or angle <i>TWR</i> or angle <i>WRS</i> = 126 (may be marked on diagram) A1 for 54 C1 for appropriate reasons for method shown eg. <u>Angles</u> on a straight <u>line</u> add up to <u>180</u> and <u>Alternate</u> angles are equal OR <u>Corresponding</u> angles are equal and <u>Angles</u> on a straight <u>line</u> add up to <u>180</u> OR Vertically <u>opposite</u> angles are equal and <u>Allied</u> angles / <u>Co-interior</u> angles add up to <u>180</u> OR OR <u>Angles</u> at a <u>point</u> add up to <u>360</u> with other reasons as above. |
| 4:; | | $5\frac{2}{3}$ | 4 | M1 for $AB = 2x$ or $DC = 2x + 4$ or for $38 - 4$ M1(dep) for $x + "x" + "2x" + "2x + 4"$ or for " $38 - 4" \div 6$ M1 for " $6x + 4" = 38$ A1 for $5\frac{2}{3}$ oe NB: Accept answers in the range 5.6 to 5.7 if M3 scored. SC if M0 then B2 for answer in range 5.6 - 5.7 |



| Que | stion | Working | Answer | Mark | Notes |
|------|-------|---------|--------|------|---|
| 4; 2 | | | 186.20 | 5 | M1 for use of consistent units to find volume, $11 \times 4 \times 0.06$ (=2.64) or $1100 \times 400 \times 6$ (=2640000) M1 (dep on vol calculation) for attempt to find number of bags needed, eg "2.64" $\div 0.4$ (=6.6 \rightarrow 7) M1 for the cost of gravel before discount eg "6.6" \times 38 or "7" \times 38 M1 for attempt to find the total cost after discount"266" $\times 0.7$ oe A1 for 186.2(0) OR M1 for cost of gravel per bag after discount, 38 $\times 0.7$ (=26.60) M1 for use of consistent units to find volume, $11 \times 4 \times 0.06$ (=2.64) or $1100 \times 400 \times 6$ (=2640000) M1 (dep on vol calculation) for attempt to find number of bags needed, eg "2.64" $\div 0.4$ M1 for total cost of gravel after discount "7" \times "26.6" A1 for 186.2(0) |
| 4; 3 | (a) | | 7.5 | 3 | M1 for $4.5^2 + 6^2$ (=56.25) M1 for $\sqrt{56.25}$ or $\sqrt{(4.5^2 + 6^2)}$ A1 for 7.5 |
| | (b) | | 217 | 4 | M1 for use of appropriate trig ratio eg tan $CAB = \frac{4.5}{6}$ (= 0.75), sin $CAB = \frac{4.5}{"7.5"}$ (= 0.6), cos $CAB = \frac{6}{"7.5"}$ (= 0.8) M1 for inverse trig shown correctly eg $CAB = \tan^{-1} \frac{4.5}{6}$ (= 0.75), $CAB = \sin^{-1} \frac{4.5}{"7.5"}$ (= 0.6), $CAB = \cos^{-1} \frac{6}{"7.5"}$ (= 0.8) A1 for 36.8 to 37 (or 53 to 53.2 if identified as ACB) B1ft for bearing 180 + "36.8" if "36.8" is not 40-50 eg 216.8 to 217 |



| Que | estion | Working | Answer | Mark | Notes |
|------|--------|---------|--------|------|--|
| 4;4 | (a) | | 7.5 | 2 | M1 for sight of $\frac{9}{6}$ (=1.5) oe or $\frac{6}{9}$ (=0.66) oe or $\frac{5}{6}$ (=0.83) oe or $\frac{6}{5}$ (=1.2) oe or a ratio, eg 6:9 oe or decimal, eg 1.5 oe A1 cao |
| | (b) | | 8 | 2 | M1 for $12 \times \frac{6}{9}$ oe or $12 \div \frac{9}{6}$ oe or $\frac{12}{"7.5"} \times 5$ oe A1 cao |
| 4; 5 | | | 302 | 3 | M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times 4^3$ oe (= 133.9 - 134.2) M1 for $\frac{1}{3} \times \pi \times 4^2 \times 10$ oe (= 167.4 - 167.7) A1 for 301 - 302 (or 96 π or $\frac{288}{3}\pi$) |



| Questio | on Working | Answer | Mark | Notes |
|---------|------------|--------|------|---|
| 4; 6 | | 43.9 | 5 | M1 for $\frac{11}{\sin 100} = \frac{9}{\sin D}$ oe M1 for $\sin D = \frac{9\sin 100}{11}$ (=0.80575) or $D = 53.68$ M1 for angle DCA= 180 - 100 - "D" (=26.317) M1 for area of $ABCD = 2 \times \frac{1}{2} \times 11 \times 9 \times \sin^{\circ}26.317$ " A1 for 43.8 - 43.9 OR M1 for $\frac{11}{\sin 100} = \frac{9}{\sin D}$ oe M1 for $\sin D = \frac{9\sin 100}{11}$ (=0.80575) or $D = 53.68$ M1 for (height=) $9 \times \sin(180 - 100 - "D")$ or height = 3.990 M1 for area of $ABCD = (2 \times \frac{1}{2}) \times 11 \times$ "height" A1 for 43.8 - 43.9 OR M1 for $11^2 = AD^2 + 9^2 - 2 \times AD \times 9 \times \cos 100$ M1 for $AD = \frac{18\cos 100 + \sqrt{(18\cos 100)^2 - 4(1)(-40)}}{2(1)}$ M1 for $AD = \frac{18\cos 100 + \sqrt{(169.7(69795)}}{2(1)}$ (= 4.95195()) M1 for area of $ABCD = 2 \times \frac{1}{2} \times$ "4.95195" $\times 9 \times \sin 100$ A1 for 43.8 - 43.9 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|--|
| 4;7 | | | 2 | M1 for a 5cm by 5 cm square or a 5cm by 3 cm rectangle or a 5 cm by 2 cm rectangle A1 for correct elevation with dividing line NB: diagrams which appear to have a 3D element get 0 marks |
| 4; 8 | | 115 | 4 | M1 for $360 - 4 \times 25$ (=260) M1 (dep) for '260'÷4 (=65) M1 for $180 - '65'$ or $(360 - 2 \times '65') \div 2$ A1 for 115 with working OR M1 for $360 \div 4$ (=90) M1 (dep) for '90' - 25 (=65) M1 for $180 - '65'$ or $(360 - 2 \times '65') \div 2$ A1 for 115 with working |
| 4;9 | | 440 | 2 | M1 for $140 \times \pi$ oe or 439 A1 for $439.6 - 440$ |
| 4;: | | 80.1 | 3 | M1 for $39^2 + 70^2$ M1 for $\sqrt{"1521" + "4900"}$ or $\sqrt{"6421"}$ A1 for 80.1 - 80.2 |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 4;; | | 49.5 | 4 | M1 for $\tan 54 = \frac{\text{height}}{6}$ |
| | | | | M1 for (height =) $6 \times \tan 54$ (=8.2-8.3) |
| | | | | M1 for $\frac{1}{2} \times 8.258 \times 12$ |
| | | | | A1 for 49.2 - 50 |
| | | | | OR |
| | | | | M1 for $\cos 54 = \frac{6}{AC}$ |
| | | | | M1 for $(AC =) \frac{6}{\cos 54}$ (=10.2(07)) |
| | | | | M1 for $\frac{1}{2} \times 12 \times 10.207' \times \sin 54$ |
| | | | | A1 for 49.2 - 50 |
| | | | | OR |
| | | | | M1 for $\frac{AC}{\sin 54} = \frac{12}{\sin 72}$ |
| | | | | M1 for $(AC =) \frac{12}{\sin 72} \times \sin 54 (=10.2(07))$ |
| | | | | M1 for $\frac{1}{2} \times 12 \times 10.207' \times \sin 54$ |
| | | | | A1 for 49.2 – 50 |



| Ques | tion | Working | Answer | Mark | Notes |
|------|------|----------------|--------|------|---|
| 522 | (a) | | 'show' | 2 | M1 for $\frac{1}{2} \times (x - 4 + x + 5) \times 2$ or |
| | | | | | $2x \times (x-4) + \frac{1}{2} \times 2x \times 9$ |
| | | | | | A1 for completion with correct processes seen |
| | | | | | |
| | (b) | | 13 | 3 | M1 for $\frac{-1 \pm \sqrt{1^2 - 4 \times 2 \times -351}}{2 \times 2}$ condone incorrect sign for 351 |
| | | | | | M1 for $\frac{-1\pm\sqrt{2809}}{4}$ |
| | | | | | A1 for 13 NB for either M mark accent + only in place of + |
| | | | | | OR |
| | | | | | M2 for $(2x + 27)(x - 13)$ |
| | | | | | (M1 for $(2x \pm 27)(x \pm 13)$) A1 for 13 |
| | | | | | |
| 523 | | | 14.4 | 3 | M1 for $\pi \times 6.5^2 \times 11.5$ (=1526.42) |
| | | | | | M1 (dep) for $\frac{1526.42}{2}$ |
| | | | | | $\frac{\pi \times 5.8^2}{14.5}$ |
| | | | | | AT 101 14.4 - 14.5 |
| | | | | | OR |
| | | | | | M1 for $\frac{5.8}{6.5}$ or $\frac{6.5}{5.8}$ or $0.89(23)$ or $1.12(06896)$ |
| | | | | | M1 for $11.5 \div \left(\frac{5.8}{5.7}\right)^2$ or $11.5 \div \left(\frac{6.5}{7.9}\right)^2$ |
| | | | | | A1 for 14.4 - 14.5 |
| 524 | | 180-136-"34.4" | 3.73 | 5 | M1 for $\frac{\sin L}{\log 2} = \frac{\sin 136}{127}$ |
| | | -9.304 | | | 12.8 15.7 M1 for $L = \sin^{-1}\left(\frac{\sin^{-1}36}{\sin^{-1}6} \times 12.8\right)$ or or $\sin^{-1}0.566$ |
| | | | | | A1 for $344 - 345$ |
| | | | | | M1 for $\frac{LN}{LN} = \frac{15.7}{100}$ or $\frac{LN}{LN} = \frac{12.8}{100}$ or |
| | | | | | $\sin(180-136-'34.4')$ $\sin(180-136-'34.4')$ $\sin'34.4'$ |
| | | | | | $(LN^2 =)$ 15.7 ² + 12.8 ² - 2×15.7×12.8×cos(180 - 136 - '34.4') |
| | | | | | A1 for 3.73 - 3.74 |
| | | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|----------|--|
| *525 | working | Proof | <u>3</u> | M1 for one pair of equal angles or sides with reason M1 for second pair of equal angles or sides with reason C1 for proof completed correctly with full reasons and reason for congruence Acceptable reasons: AD common (oe eg both same) Angle BAD = angle CDA (angles in a semicircle are 90°) Angle ABO = angle DCA (angles in the same segment are equal) Triangle ABD and triangle DCA are congruent - ASA OR BD = CA (diameters of the circle) Angle BAD = angle CDA (angles in a semicircle are 90°.) AD common Triangle ABD and triangle DCA are congruent - RHS OR BD = CA (diameters of the circle) AD common Triangle ABD and triangle DCA are congruent - RHS OR BD = CA (diameters of the circle) AD is common Angle ABB = angle CAD (base angles of an isosceles triangle are equal.) Triangle ABD and triangle DCA are congruent - SAS |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|---------|--------|------|---|
| 526 | | 40.5 | 3 | M1 for 1.5×6 or 1.5×1.5 M1 for adding area of 5 or 6 faces provided at least 3 are the correct area A1 cao NB: anything that leads to a volume calculation 0 marks. |
| 527 | | 10752 | 4 | M1 for splitting the pentagon (or show the recognition of the "absent" triangle) and using a correct method to find the area of one shape M1 for a complete and correct method to find the total area M1 (dep on at least one prev M1) for multiplying their total area by 2.56 (where total area is a calculation involving at least two areas) A1 cao |
| 528 | | 55 | 4 | M1 for a correct method to find a different angle using 35° M1 for setting up a complete process to calculate angle <i>x</i> A1 cao B1 states one of the following reasons relating to their chosen method: <u>Alternate angles are equal;</u> <u>Corresponding angles are equal;</u> <u>Allied angles / Co-interior angles add up to 180;</u> the <u>exterior angle</u> of a triangle is <u>equal</u> to the sum of the <u>interior</u> <u>opposite angles</u> . |



| Questio | on Working | Answer | Mark | Notes |
|---------|--|--------|------|---|
| *52: | Angle $POT = 180 - 90 - 32 = 58$ | 29 | 5 | M1 for $1.35^2 + 3.25^2$ M1 (dep) for $\sqrt{(1.35^2 + 3.25^2)}$ (= $\sqrt{12.385}$) A1 for answer in the range 3.51 to 3.52 B1 for angle OTP = 90°, quoted or shown on the diagram |
| | (angle between <u>radius</u> and $\tan gent = 90^{\circ}$ and sum of <u>angles</u> in a <u>triangle</u> = <u>180^{\circ}</u>) Angle <i>OST</i> = angle <i>OTS</i> = 58÷2 (<u>ext angle</u> of a triangle <u>equal</u> to sum of <u>int opp angles</u> and base angles of an <u>isos</u> triangle are equal) or (<u>angle</u> at <u>centre</u> = <u>2x</u> angle at circumference) OR Angle <i>SOT</i> = 90 + 32 = 122 (<u>ext angle</u> of a triangle <u>equal</u> to sum of <u>int opp angles</u>) (180 - 122) ÷ 2 (base <u>angles</u> of an <u>isos</u> triangle are <u>equal</u>) | | | M1 for a method that leads to $180 - (90 + 32)$ or 58 shown at <i>TOP</i> M1 for completing the method leading to "58"÷2 or 29 shown at <i>TSP</i> A1 cao C1 for "angle between <u>radius</u> and <u>tangent</u> = <u>90</u> °" and one other correct reason given from theory used NB: C0 if inappropriate rules listed OR B1 for angle OTP = 90°, quoted or shown on the diagram M1 for a method that leads to 122 shown at <i>SOT</i> M1 for (180 – "122") ÷ 2 or 29 shown at <i>TSP</i> A1 cao C1 for "angle between <u>radius</u> and <u>tangent</u> = <u>90</u> °" and one other correct reason given from theory used NB: C0 if inappropriate rules listed |



| Ques | stion | Working | Answer | Mark | Notes |
|------|-------|--|---|------|--|
| 52; | | $cos y = 2.25 \div 6y = cos-1 (2.25 \div 6)$ OR 6cos 75 = 1.55 | The ladder is not safe because y is not near to 75 | 3 | M1 for $\cos y = 2.25 \div 6$ oe M1 for $\cos^{-1} (2.25 \div 6)$ C1 for sight of 67-68 and a statement eg this angle is NOT (near to) 75° and so the ladder is not steep enough and so not safe. OR M1 for $\cos 75 = x \div 6$ M1 for $6\cos 75$ C1 for sight of 1.55(29) and a statement eg that 2.25 NOT (near to) 1.55 and so the ladder is not steep enough and so not safe. |
| 532 | (a) | | 18.2 | 2 | M1 for $\frac{1}{2} \times 6 \times 7 \times \sin 60$ A1 for answer in range 18.1 to 18.2 |
| | (b) | | 6.56 | 3 | M1 for $6^2 + 7^2 - 2 \times 6 \times 7 \times \cos 60$ M1 for correct order of operation eg 36 + 49 - 42 (=43) A1 for answer in range 6.55 to 6.56 |



| Que | stion | Working | Answer | Mark | Notes |
|-----|------------|----------------------------|--|------|---|
| 533 | | $\pi \times 5 \times 1.80$ | 28.27 | 3 | M1 for use of $\pi \times x$ (with $x = 5$ or $x = 2.5$) or $2 \times \pi \times x$ (with $x = 5$ or $x = 2.5$) M1 for $\pi \times 5 \times 1.8(0)$ or $2 \times \pi \times 2.5 \times 1.8(0)$ A1 for 28.26 or 28.27 or 28.28 or 28.3(0) or 28.8(0) |
| 534 | | | 1180 | 3 | M1 for a correct method to find the area of the cross section M1 (dep) for a complete correct method for the volume of the prism A1 cao OR M1 for a correct method to find the volume of one cuboid M1 (dep) for a complete correct method for the volume of the prism A1 cao |
| 535 | | | Translation; $\begin{pmatrix} 6\\-1 \end{pmatrix}$ | 2 | B1 for translation B1 for $\binom{6}{-1}$ NB: B0 if more than one transformation given |
| 536 | (a) (b) | | 11.5 47.2 | 3 | M1 for $13^2 - 6^2$ or $169 - 36$ or 133 M1 (dep on M1) for $\sqrt{"13^2 - 6^{2"}}$ or $\sqrt{133}$ A1 for answer in the range $11.5 - 11.6$ M1 for $\cos (RPQ) = \frac{17}{25}$ oe OR $\sin PQR = \frac{17}{25}$ with <i>PQR</i> clearly identified M1 for $(RPQ = +) \cos^{-1} \frac{17}{25}$ oe OR $PQR = \sin^{-1} \frac{17}{25}$ with <i>PQR</i> clearly identified A1 for answer in the range $47.1 - 47.2$ SC : B2 for an answer of $0.823(033)$ or $52.3(95)$ or 52.4 |



| Que | stion | Working | Answer | Mark | Notes | | |
|-----|-------|---|--------|------|---|--|--|
| 537 | (a) | $\frac{1}{2} \times (4+12) \times 10$ | 80 | 2 | M1 for a fully correct method for area of <i>QRST</i> A1 cao | | |
| | (b) | For example $\frac{PT+10}{PT} = \frac{12}{4} 3$ $PT+10 = 3PT$ $2PT = 10$ | 5 | 3 | M1 for a correct scale factor or ratio using two corresponding sides from two similar triangles or two sides within the same triangle (may be seen within an equation) eg. $\frac{12}{4}$ oe or 4 : 12 oe or $\frac{PT}{4}$ or $\frac{PS}{12}$ or $\frac{12}{12-4}$ etc. M1 for a correct equation with <i>PT</i> or <i>PS</i> as the only variable or complete correct method using scale factor A1 cao | | |
| 538 | | $\frac{30}{360} \times \pi \times 15^2$ | 58.8 | 2 | M1 for a correct method to find the area of sector OAB A1 for answer in range $58.8 - 58.9125$ | | |
| 539 | | | 15.0 | 3 | M1 for $8^2 + 8^2 - 2 \times 8 \times 8 \times \cos 140$ M1 (dep) for correct order of evaluation or 226.(05) A1 for answer in range 15.0 - 15.04 OR M1 for $\frac{PR}{\text{SIN } 140} = \frac{8}{\sin\left(\left(\frac{180-140}{2}\right)\right)}$ M1 for $PR = \frac{8}{\sin\left(\left(\frac{180-140}{2}\right)\right)} \times \sin 140$ A1 for answer in range 15.0 - 15.04 OR M1 for $8 \times \sin 70$ or $8 \times \cos 20$ M1 for $2 \times 8 \times \sin 70$ or $2 \times 8 \times \cos 20$ A1 for answer in range 15.0 - 15.04 | | |



| Question | n Working | Answer | Mark | Notes |
|----------|---|--------|------|--|
| 53: | $\frac{\frac{1}{3} \times \pi \times 15^2 \times 40}{-\frac{1}{3} \times \pi \times 7.5^2 \times 20}$ | 8250 | 4 | B1 for 15cm as diameter or 7.5 cm as radius of smaller cone (may be marked on diagram or used in a formula) M1 for a numerical expression for the volume of one cone eg. $\frac{1}{3} \times \pi \times 15^2 \times 40$ (=9424) or $\frac{1}{3} \times \pi \times 7.5^2 \times 20$ (=1178) M1 for $\frac{1}{3} \times \pi \times 15^2 \times 40$ oe $-\frac{1}{3} \times \pi \times 7.5^2 \times 20$ oe A1 for answer in the range 8240 - 8250 OR B1 for 2 ³ M1 for a numerical expression for the volume of the large cone eg. $\frac{1}{3} \times \pi \times 15^2 \times 40$ (=9424) M1 volume of frustrum $= \frac{7}{8} \times \frac{1}{3} \times \pi \times 15^2 \times 40$ oe A1 for answer in the range 8240 - 8250 |
| 53; | | 1 + √5 | 5 | M1 for $\frac{1}{2} \times x \times x \times \sin 30^\circ$ oe M1 for $\frac{1}{2}(x-2)(x+1)$ oe or $\frac{1}{2} \times (x-2) \times (x+1) \times \sin 90$ M1 (dep on at least one previous M1) for formation of equation from equating areas with x as the only variable A1 for $x^2 - 2x - 4 = 0$ oe in the form $ax^2 + bx + c = 0$ or $ax^2 + bx = c$ A1 cao |



| Question | Working | Answer | Mark | Notes |
|----------|---------|---|------|---|
| 542 (a) | | Triangle with vertices (1, 5) (4, 5) (4,7) | 2 | B2 correct reflection (B1 a translation of the correct answer with the final shape above $y = x$ or any two correct vertices) SC : B1 for a triangle with vertices at (2, 5) (4, 5) (4, 8) |
| (b) | | Translation by $\begin{pmatrix} -2 \\ -4 \end{pmatrix}$ | 2 | B1 Translation B1 $\begin{pmatrix} -2 \\ -4 \end{pmatrix}$ NB. Award no marks for a combination of transformations |







| Questio | on Working | Answer | Mark | Notes |
|---------|--|----------------------|------|---|
| 543 | Angle $DEC = 180 - 41 = 139$ | $x = 19^{\circ}$ and | 4 | M1 for $DBC = 38^{\circ}$ or |
| | <u>Angles</u> on a straight <u>line</u> sum to <u>180°</u> | reasons | | $ADC = 60^{\circ}$ (can be implied by $BDC = 22^{\circ}$) or $ABC =$ |
| | Angle $EDC = 60 - 38$ or | | | 60° or |
| | Angle $ABD = 180 - 120 - 38$ (=22) | | | $DCB = 120^{\circ}$ or |
| | <u>Co-interior/allied angles</u> of parallel lines sum to | | | (ABD =) 180 - 120 - 38 (=22) |
| | 180° or | | | |
| | <u>Angles in a triangle sum to 180° and Alternate</u> | | | M1 for $(BDC =) 60 - 38 (=22)$ or |
| | angles | | | BDC = '22' or |
| | x =)180 - '139' - '22' (=19) | | | (DEC =) 180 - 41 (=139) or |
| | <u>Angles in a triangle sum to 180°</u> | | | (BCE =) 180 - 41 - 38 (=101) |
| | OP | | | M1 (day on both marriage M1) for complete compat |
| | OR | | | mathed to find r or |
| | Angle $ADC = 180^{\circ} - 120^{\circ} - 60^{\circ}$ | | | (x -) 10 |
| | Aligie $ADC = 180^{\circ} = 120^{\circ} = 00^{\circ}$ | | | $(\lambda -)$ 19 |
| | $\frac{CO-interior/ained angles}{180^{\circ}}$ of parametrines sum to 180° Angle $EDC = 22^{\circ}$ | | | C1 for $r = 10^{\circ}$ AND |
| | Angle $ECD = 41^{\circ} - 22^{\circ} = 19^{\circ}$ | | | Co-interior/allied angles of parallel lines sum to 180° |
| | Exterior angle of triangle equals sum of the two | | | or |
| | opposite interior angles | | | Opposite angles of a parallelogram are equal |
| | opposite interior wildred | | | or |
| | OR | | | Alternate angles |
| | | | | AND |
| | Angle $DBC = 38^{\circ}$ <u>Alternate angles</u> | | | <u>Angles</u> on a straight <u>line</u> sum to <u>180°</u> |
| | Angle $BCE = 101^{\circ}$ Angle sum of a triangle | | | or |
| | is <u>180°</u> | | | <u>Angles</u> in a <u>triangle</u> sum to <u>180°</u> |
| | Angle $BCD = 120^{\circ}$ <u>Opposite angles</u> of a | | | or |
| | parallelogram are equal | | | Exterior angle of triangle equals sum of the two |
| | Angle $ECD = 120^{\circ} - 101^{\circ} = 19^{\circ}$ | | | opposite interior angles |
| | | | | or |
| | | | | <u>Angles</u> in a <u>quadrilateral</u> sum to <u>360°</u> |



| Question | Working | Answer | Mark | Notes |
|----------|---|-----------|------|---|
| 544 | $17.8 \div 160 \times 210 = 0.11125 \times 210 = 23.3625 \text{ g}$ OR $210 \div 160 \times 17.8 = 1.3125 \times 17.8 = 23.3625 \text{ g}$ OR $210 - 160 (=50)$ $\frac{17.8}{160} \times '50' (= 5.5625)$ $17.8 + 5.5625$ | 23.3(625) | 3 | M1 17.8 ÷ 160 (=0.11125) or 17.8 × 210 (=3738) or 210 ÷ 160 (=1.3125) M1 (dep) '0.11125' × 210 or '3738'÷160 or '1.3125'× 17.8 A1 for answer in range 23.3 - 23.4 OR M1 for $\frac{17.8}{160}$ × (210–160) (= 5.5625) M1 (dep) for 17.8 + '5.5625' A1 for answer in range 23.3 - 23.4 OR M1 for correct method to find weight of 2 cm or 5 cm or 10 cm M1 (dep) for complete method A1 for answer in range 23.3 - 23.4 |



| Qu | estion | Working | Answer | Mark | Notes |
|-----|------------|--|-------------|------|--|
| 545 | (a) (b) | $x = 1 \qquad -9$ | show 5.4 | 2 | M1 for $x \times x \times x$ or $2 \times 5 \times x$ or vol of cube = x^3 or vol cuboid = $10x$ A1 correct completion leading to $x^3 - 10x = 100$ B2 for a trial $5 \le x \le 6$ evaluated correctly (B1 for any two trials evaluated correctly for |
| | | $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$ | | | positive values of x) B1 for a different trial $5.3 < x < 5.4$ evaluated correctly B1 (dep on at least one previous B1) for 5.4 Accept trials correct to the nearest whole number (rounded or truncated) if the value of x is to 1 d.p., but correct to 1 d.p. (rounded or truncated) if the value of x is to 2 or more d.p. NB. Allow 100 for a trial of $x = 5.355$ |
| 546 | | 9-3 = 6 $10^{2}-6^{2} = 64$ BC = 8 $AC^{2} = 9^{2} + 8^{2} = 145$ | 12.0 | 5 | M2 $10^2 - (9 - 3)^2$ (=64) or $BC = 8$ (M1 $9 - 3$ (= 6) may be seen on diagram) M1 (indep) $9^2 + 'BC'^2$ where <i>BC</i> is a numerical value M1 (dep on previous M1) $\sqrt{81 + '64'}$ A1 $12.0 - 12.042$ |



| Question | Working | Answer | Mark | Notes |
|----------|--|--------|------|---|
| 547 | $\sin 60^\circ = \frac{x}{32} \ x = 32 \times \sin 60 (=27.712)$ | 27.7 | 3 | M1 $\sin 60 = \frac{x}{32}$ or $\frac{x}{\sin 60} = \frac{32}{\sin 90}$ oe M1 $(x =) 32 \times \sin 60$ or $(x =) \frac{32}{\sin 90} \times \sin 60$ A1 $27.7 - 27.72$ OR M1 $\cos(90 - 60) = \frac{x}{32}$ M1 $(x =) 32 \times \cos(90 - 60)$ A1 $27.7 - 27.72$ Radians : -9.7539398 Gradians : 25.888554 SC : B2 for an answer in the range (-) 9.75 to (-)9.754 or 25.8 to 25.9 |



| Qu | estion | Working | Answer | Mark | Notes |
|------------------|--------|--|---------------|-----------|---|
| Qu 548 | (a) | WorkingLet O be the centre of the base. $OB^2 + OC^2 = 10^2$; $OB^2 = 50$ $AO^2 = AB^2 - OB^2 = 50$ $Vol = \frac{1}{3} \times 10^2 \times \sqrt{50}$ $Vol = \frac{1}{3} \times 10^2 \times \sqrt{50}$ Let M be the midpt of side BC andlet O be the centre of the base. $AM^2 + MC^2 = 10^2$; $AM^2 = 75$ $AO^2 = AM^2 - MO^2 = 50$ $Vol = \frac{1}{3} \times 10^2 \times \sqrt{50}$ | Answer 236 | Mark 4 | Notes M1 correct method to start to find <i>BD</i> or <i>BO</i> using triangle <i>OBC</i> or triangle <i>BCD</i> (oe) Eg. <i>OB</i> ² + <i>OC</i> ² = 10 ² or <i>BO</i> ² = 50 or $BO = \sqrt{50}$ (=7.07) or $BO = \frac{\sqrt{200}}{2}$ or $10^2 + 10^2 = BD^2$ or $BD^2 = 200$ or $BD = \sqrt{200}$ (=14.1) M1 (dep) correct method to find height of pyramid using triangle <i>AOB</i> Eg. $AO^2 = 10^2 - \sqrt{50}$ '2 or $AO^2 = 50$ or $AO = \sqrt{50}$ (=7.07) M1 (indep) $\frac{1}{3} \times 10^2 \times \sqrt{50}$ ' (but not $\frac{1}{3} \times 10^2 \times 10$) A1 235 - 236 OR M1 correct method to start to find height of a face using triangle <i>AMC</i> (oe) Eg. $AM^2 + 5^2 = 10^2$ or $AM^2 = 75$ or $AM = \sqrt{75}$ (=8.66) M1 (dep) correct method to find height of pyramid using triangle <i>AOM</i> Eg. $AO^2 = \sqrt{75}$ ' ² - 5 ² or $AO^2 = 50$ or $AO = \sqrt{50}$ (=7.07) |
| | | | | | M1 (indep) $\frac{1}{3} \times 10^2 \times \sqrt{50}$ (but not $\frac{1}{3} \times 10^2 \times 10$) A1 235 - 236 |



| Question | | Working | Answer | Mark | Notes |
|---------------------|---------------|---------|--------|------|---|
| Que 548 cont. | estion (a) | Working | Answer | Mark | Notes OR M1 for sin 45 = $\frac{x}{10}$ or cos 45 = $\frac{x}{10}$ M1 for $h = 10 \times \sin 45$ or $h = 10 \times \cos 45$ (=7.07) M1 (indep) $\frac{1}{3} \times 10^2 \times 7.07'$ (but not $\frac{1}{3} \times 10^2 \times 10$) |
| | | | | | A1 235 – 236 |



| Question | Working | Answer | Mark | Notes |
|----------|---|--------|------|--|
| 548 (b) | Angle $ABO = 45^{\circ}$ Angle $DAB = 180 - 45 - 45$ | 90 | 2 | M1 Angle $DAB = 180 - 2 \times 45^{\circ}$ A1 89.98 - 90 |
| | OR | | | OR |
| | In ΔBAD , $\cos A = \frac{10^2 + 10^2 - \sqrt{200}}{2 \times 10 \times 10} = 0$ | | | M1 $\cos BAD = \frac{10^2 + 10^2 - \sqrt{200}}{2 \times 10 \times 10}$ |
| | OR | | | A1 89.98 - 90 OR |
| | In $\triangle BOA$, $\cos B = \frac{\sqrt{50'}}{10}$ Angle $BAD = 180 - 45' - 45'$ | | | M1 $\sin A = \frac{\sqrt{50}}{10}$ A1 89.98 - 90 |
| | OR | | | |
| | $\sin A = \frac{\sqrt{50}}{10}$ $A = 45$ Angle $BAD = 2 \times 45$ | | | |



| Question | Working | Answer | Mark | Notes |
|----------|--|-----------------------|------|--|
| 549 | $A = \frac{1}{2} \times x \times 2x \times \sin 30^{\circ}$ | $x = \sqrt{2A}$ shown | 3 | M1 $(A=)\frac{1}{2} \times x \times 2x \times \sin 30^{\circ}$ |
| | $A = \frac{1}{2} \times 2x^2 \times 0.5$ | | | A1 $A = x^2 \times 0.5$ or $A = \frac{x^2}{2}$ |
| | | | | C1 for completion with all steps shown |
| | OR | | | OR M1 height = $2x\sin 30 (= x)$ |
| | Height = $2x \sin 30^\circ = x$ | | | A1 $A = x^2 \times 0.5$ or $A = \frac{x^2}{2}$ |
| | $A = \frac{x \times x}{2} = \frac{x}{2}$ | | | C1 for completion with all steps shown |
| | OR | | | OR |
| | Height = $x \sin 30 = \frac{x}{2}$ | | | M1 for height = $x \sin 30 \left(=\frac{x}{2}\right)$ |
| | $A = \frac{1}{2} \times 2x \times \frac{x}{2} = \frac{x^2}{2}$ | | | A1 $A = x^2 \times 0.5$ or $A = \frac{x^2}{2}$ |
| | | | | C1 for completion with all steps shown |



| Question | Working | Answer | Mark | Notes |
|----------------|----------|--|--------|---|
| 54: | 180 – 47 | 133 | 3 | M1 for $180 - 47$ A1 for 133 C1(dep on M1) for full reasons e.g. <u>angles</u> on a straight <u>line</u> add up to <u>180°</u> and <u>alternate</u> <u>angles</u> are equal OR <u>corresponding angles</u> are equal and <u>angles</u> on a straight <u>line</u> add up to <u>180°</u> OR vertically <u>opposite angles</u> (or <u>vertically opposite</u> angles) are equal and <u>allied angles</u> (or <u>co-interior</u> <u>angles</u>) add up to <u>180°</u> |
| 54; (a) (b) | | Triangle with vertices (2,-1) (4, -1) (4, -4) Triangle with vertices (7, 2) (13, 2) (7, 11) | 2 3 | B2 for triangle with vertices (2,-1) (4, -1) (4, -4) (B1 for triangle in correct orientation or rotated 90° anticlockwise centre <i>O</i> B3 for triangle with vertices (7, 2) (13, 2) (7, 11) (B2 for 2 vertices correct or enlargement scale factor 3 in wrong position or enlargement, centre (1,2), with different scale factor) (B1 for 1 vertex correct or enlargement, not from (1,2), different scale factor) |



| Question | Working | Answer | Mark | Notes |
|----------|-----------------------------------|--------|------|---|
| 552 | $\cos x = \frac{6.4}{9.6}$ | 48.2 | 3 | M1 for $\cos x = \frac{6.4}{9.6}$ or $\cos x = 0.66(6)$ or $\cos x = 0.67$ |
| | $x = \cos^{-1} \frac{6.4}{9.6} =$ | | | M1 for $\cos^{-1}\frac{6.4}{9.6}$ or $\cos^{-1} 0.66(6)$ or $\cos^{-1} 0.67$ |
| | | | | A1 for 48.1 – 48.2 |
| | | | | OR |
| | | | | Correct use of Pythagoras and then trigonometry, no |
| | | | | marks until 17, 1551 |
| | | | | M1 for sin $x = \frac{7.155}{9.6}$ or tan $x = \frac{7.155}{6.4}$ |
| | | | | or $\sin x = \frac{'7.155'}{9.6} \times \sin 90$ |
| | | | | or $\cos x = \frac{6.4^2 + 9.6^2 - 7.155'^2}{2 \times 6.4 \times 9.6}$ |
| | | | | M1 for $\sin^{-1}\frac{'7.155'}{9.6}$ or $\tan^{-1}\frac{'7.155'}{6.4}$ |
| | | | | or $\sin^{-1}\left(\frac{'7.155'}{9.6} \times \sin 90\right)$ |
| | | | | or $\cos^{-1}\left(\frac{6.4^2 + 9.6^2 - 7.155'^2}{2 \times 6.4 \times 9.6}\right)$ |
| | | | | A1 for 48.1 – 48.2 |
| | | | | SC B2 for 0.841 (using rad) or 53.5 (using grad) |



| Quest | ion Working | Answer | Mark | Notes |
|-------|-----------------------------------|--------|------|---|
| 553 | $BD^2 + 12^2 = 16^2$ oe | 16.5 | 5 | M1 for $BD^2 + 12^2 = 16^2$ oe or $16^2 - 12^2$ or 112 seen |
| | $BD = \sqrt{256 - 144}$ | | | M1 for $\sqrt{256-144}$ or $\sqrt{112}$ (=10.58) |
| | (=10.58) | | | M1 for sin $40 = 10.58'$ or so $50 = 10.58'$ |
| | $\sin 40 = \frac{10.58'}{10.58'}$ | | | $\frac{1}{CD} = \frac{1}{CD} = \frac{1}{CD} = \frac{1}{CD}$ |
| | CD | | | M1 for $(CD =)$ '10.58' or '10.58' |
| | $CD = \frac{'10.58'}{'10.58'}$ | | | $\frac{1}{\sin 40} \frac{1}{\cos 50} \frac{1}{\cos 50}$ |
| | sin 40 | | | A1 for 16.4 – 16.5 |
| | | | | |
| | | | | OR $16^{2} + 12^{2$ |
| | | | | M1 for $BD^2 + 12^2 = 16^2$ oe or $16^2 - 12^2$ or 112 seen |
| | | | | M1 for $\sqrt{256}$ – 144 or $\sqrt{112}$ (=10.58) |
| | | | | M1 for $(BC =)$ '10.58' x tan 50 or $\frac{10.58'}{(=12.6)}$ |
| | | | | $\frac{1}{\tan 40}$ (BC -) 10.58 × $\frac{1}{\tan 40}$ (-12.0) |
| | | | | M1 for $\sqrt{12.6'^2 + 10.58'^2}$ |
| | | | | A1 for 16.4 – 16.5 |
| | | | | |



| Question | Working | Answer | Mark | Notes |
|----------|--|--------|------|--|
| 554 | AC 8.7 | 29.3 | 5 | M1 for AC = 8.7 |
| | $\frac{1}{\sin 49} = \frac{1}{\sin 64}$ | | | $\frac{1}{\sin 49} = \frac{1}{\sin 64}$ de |
| | AC 8.7 | | | $M1 \text{ for } (AC =) = \frac{8.7}{100} \text{ scin } 40$ |
| | $AC = \frac{1}{\sin 64} \times \sin 49$ | | | $\frac{1}{\sin 64} \times \sin 49$ |
| | (= 7.305) | | | A1 for 7.3(05) |
| | $1 \times 8.7 \times 7.205 \times \sin(180, 64, 40)$ | | | M1 for $\frac{1}{2} \times 8.7 \times 57.205^{2} \times \sin(180 - 64 - 40)$ |
| | $\frac{1}{2}$ $^{\circ}$ | | | $\frac{1}{2} = \frac{1}{2} = \frac{1}$ |
| | | | | A1 for 29.19 – 29.3 |
| | | | | |
| | | | | OR DC 07 |
| | | | | M1 for $\frac{BC}{\sin(180 - 64 - 49)} = \frac{8.7}{\sin 64}$ oe |
| | | | | M1 for $(BC =) \frac{8.7}{\sin 64} \times \sin' 67'$ |
| | | | | A1 for 8.9(10) |
| | | | | M1 for $\frac{1}{2} \times 8.7 \times 8.910' \times \sin 49$ |
| | | | | A1 for 29.19 – 29.3 |
| | | | | OR |
| | | | | (X is point such that AX is perpendicular to BC) |
| | | | | M1 for $AX = 8.7 \times \sin 49$ (= 6.565) or |
| | | | | $XB = 8.7 \times \cos 49 \ (= 5.707)$ |
| | | | | M1 for $XB = 8.7 \times \cos 49$ (= 5.707) and |
| | | | | $CX = 6.565' \div \tan 64 \text{ oe} (= 3.202)$ |
| | | | | A1 for 8.9(10) or 5.7(07) and 3.2(02) |
| | | | | M1 for $\frac{1}{2} \times 6.565 \times (5.707' + 3.202')$ oe |
| | | | | A1 for 29.19 – 29.3 |



| Que | stion | Working | Answer | Mark | Notes |
|-----|------------|--|---|------|---|
| 555 | (a) | | b – a | 1 | B1 for $\mathbf{b} - \mathbf{a}$ or $-\mathbf{a} + \mathbf{b}$ |
| 555 | (a) (b) | $\overrightarrow{OP} = \overrightarrow{OA} + \overrightarrow{AP}$ $\overrightarrow{AP} = \frac{3}{4} \times (\mathbf{b} - \mathbf{a})$ $\overrightarrow{OP} = \mathbf{a} + \frac{3}{4} \times (\mathbf{b} - \mathbf{a})$ OR $\overrightarrow{OP} = \overrightarrow{OB} + \overrightarrow{BP}$ $\overrightarrow{BP} = \frac{1}{4} \times (\mathbf{a} - \mathbf{b})$ $\overrightarrow{OP} = \mathbf{b} + \frac{1}{4} \times (\mathbf{a} - \mathbf{b})$ | $\mathbf{b} - \mathbf{a}$ $\frac{1}{4}(\mathbf{a} + 3\mathbf{b})$ | 3 | B1 for $\mathbf{b} - \mathbf{a}$ or $-\mathbf{a} + \mathbf{b}$ B1 for $\frac{3}{4} \times (\mathbf{b} - \mathbf{a})^{?}$ M1 for $(\overrightarrow{OP} =) \overrightarrow{OA} + \overrightarrow{AP}$ or $(\overrightarrow{OP} =) \overrightarrow{OA} + \frac{3}{4}\overrightarrow{AB}$ or $\mathbf{a} \pm \frac{3}{4} \times (\mathbf{b} - \mathbf{a})^{?}$ A1 for $\frac{1}{4}(\mathbf{a} + 3\mathbf{b})$ or $\frac{1}{4}\mathbf{a} + \frac{3}{4}\mathbf{b}$ OR B1 for $\frac{1}{4} \times (\mathbf{a} - \mathbf{b})^{?}$ M1 for $(\overrightarrow{OP} =) \overrightarrow{OB} + \overrightarrow{BP}$ or $(\overrightarrow{OP} =) \overrightarrow{OB} + \frac{1}{4}\overrightarrow{BA}$ or $\mathbf{b} \pm \frac{1}{4} \times (\mathbf{a} - \mathbf{b})^{?}$ A1 for $\frac{1}{4}(\mathbf{a} + 3\mathbf{b})$ or $\frac{1}{4}\mathbf{a} + \frac{3}{4}\mathbf{b}$ |
| | | | | | |

